

# Kappa, Conversion from Hard-Rock to 760 m/s

Norm Abrahamson

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# Kappa Scaling Approaches

- Will show an examples of approaches
  - Does not directly address the hard-rock -> 760 m/s kappa question
- Acknowledgments
  - Work by Linda Al-Atik, Albert Kotte, Justin Hollenback
  - Funding by Swissnuclear & PG&E

# Kappa Scaling Approaches

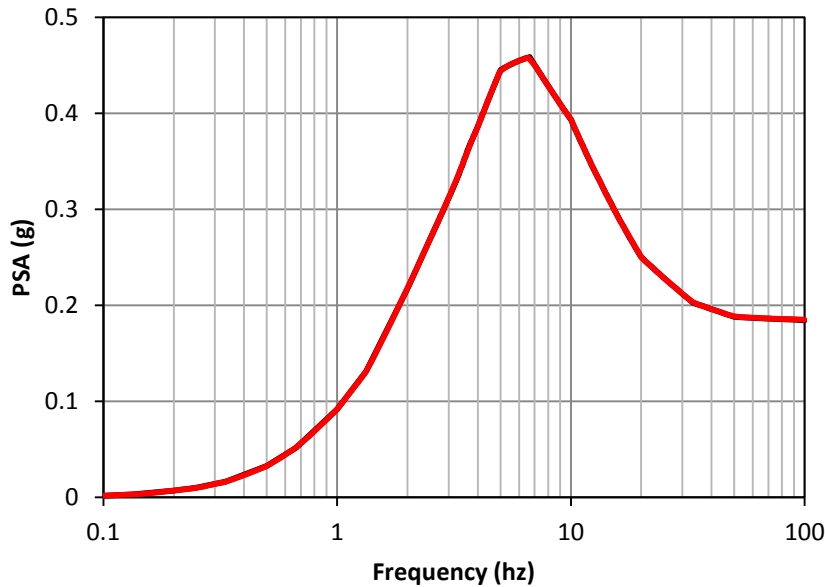
- IRVT
  - Different  $S_a$  scale factors for each GMPE
  - Use IRVT to convert  $S_a$  to FAS (for a given GMPE)
  - Apply kappa (and  $V_s$ ) scaling to FAS
  - Use RVT to convert back to  $S_a$
  - Compute  $S_a$  scale factors for the GMPE
  - Reference:
    - Al-Atik et al (2012). Kappa scaling of GMPEs using IRVT, submitted to BSSA, being revised to address review comments, resubmit in Jan 2013
- Empirical
  - Dependence of residual using kappa proxy
  - Reference:
    - Swissnuclear report

# Application Using IRVT Approach

- **Host GMPE:**
  - **Campbell & Bozorgnia (2008), CB08**
    - WUS generic rock profile with  $V_{s30}$  of 620 m/sec
    - Average host kappa based on the high frequency slope of IRVT-based FAS
- **Target region: Switzerland**
  - Generic Swiss rock conditions with  $V_{s30}$  of 1000 m/sec
  - Average target kappa based on the high frequency slope of IRVT-based FAS ( $\kappa_0 = 0.017$ )

# Vs-Kappa Scaling of CB08

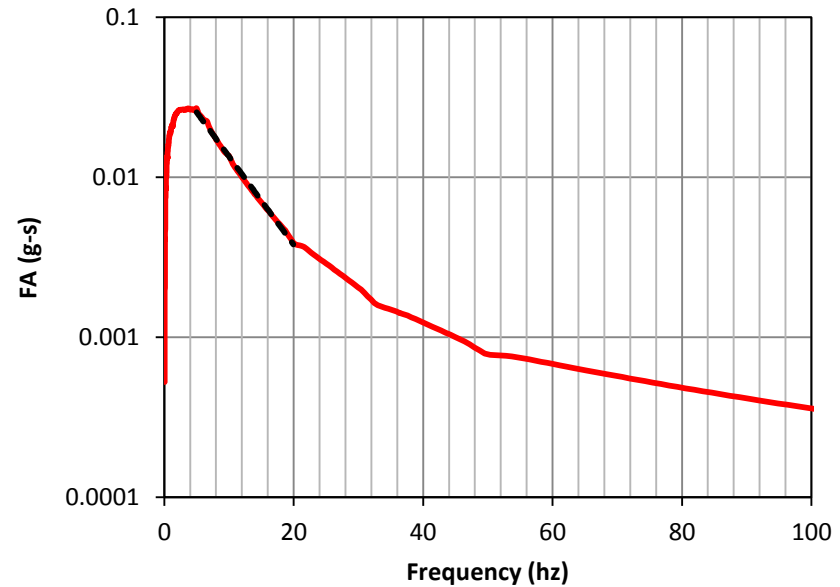
M6 - Rjb 10km - Vs 620m/sec



— Sa GMPE    — Sa RVT-Calc

IRVT  
➔

M6 - Rjb 10km - Vs 620m/sec



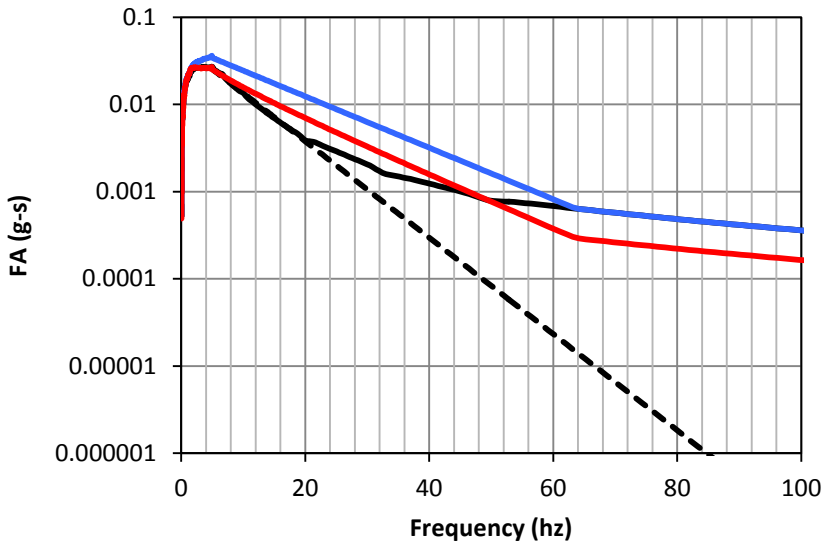
— FAS RVT-Calc    - - - Kappa Scaling

Average host kappa = 0.041 sec,    stdev = 0.0015

Average target kappa = 0.022 sec ( $\text{kappa}_0 = 0.017$ ),    stdev = 0.0019

# Vs-Kappa Scaling of CB08 (cont'd)

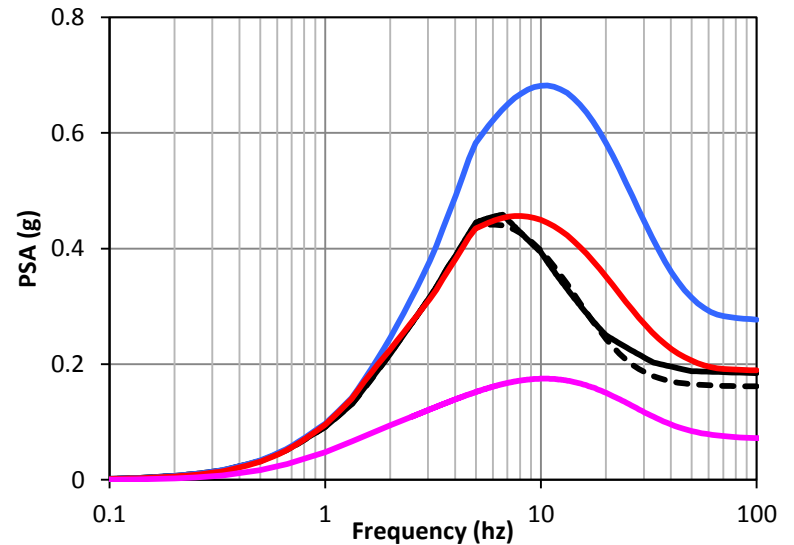
M6 - Rjb 10km - Vs 620m/sec



— FAS k=0.041      - - - FAS High Freq Mod  
 — FAS Scaled to k=0.022      — FAS Vs-k Scaled

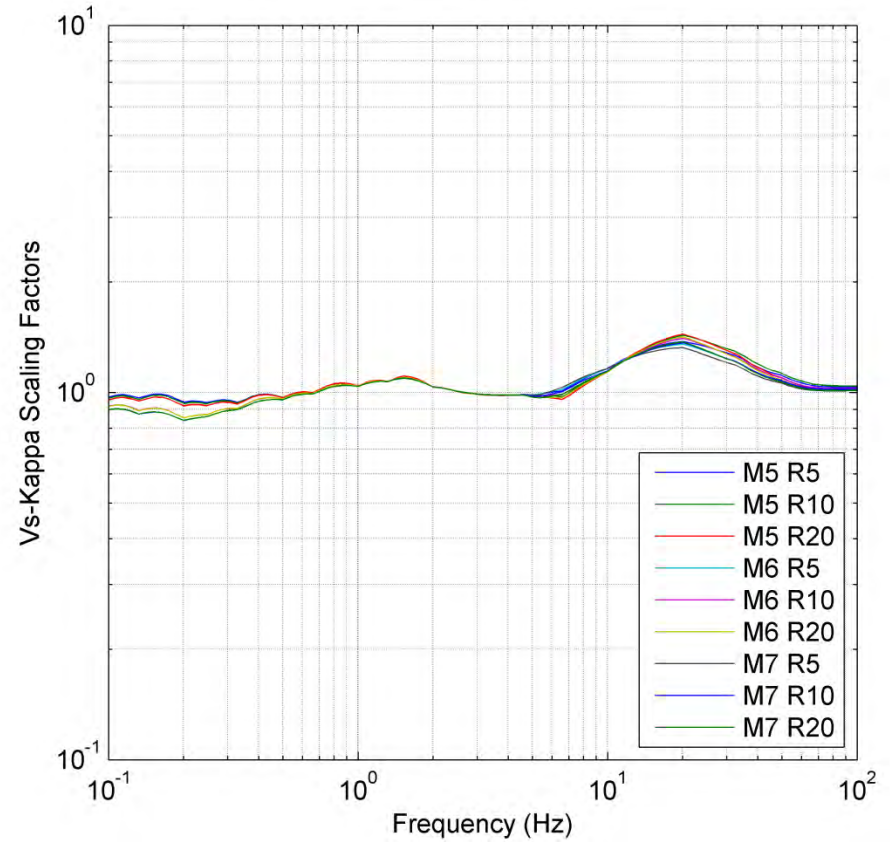
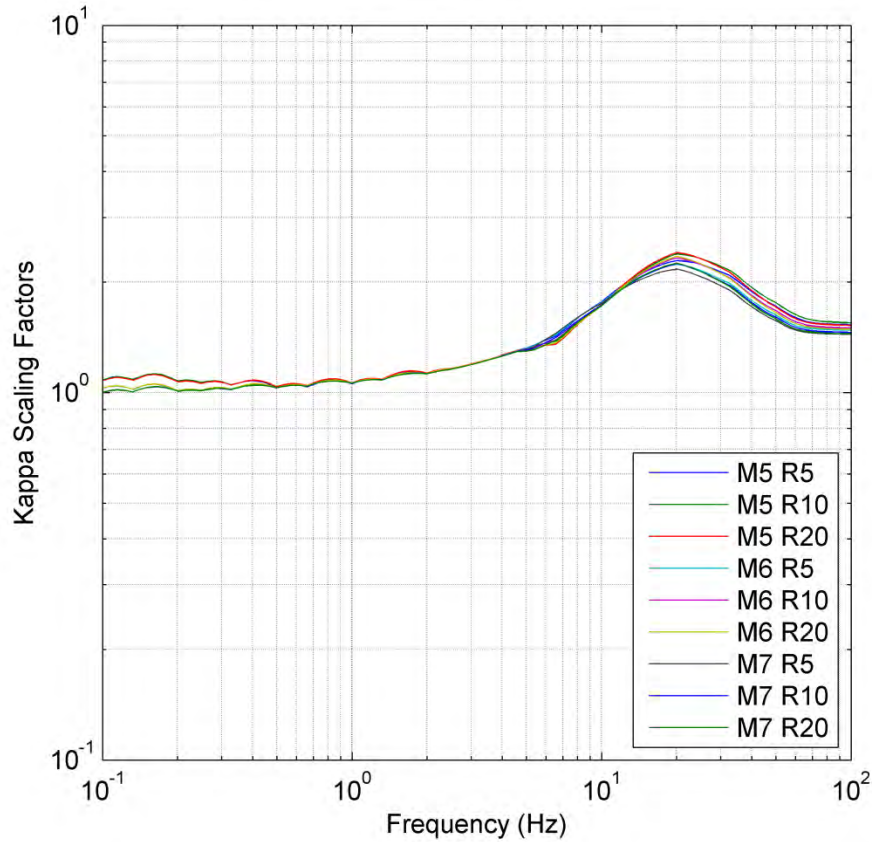
RVT

M6 - Rjb 10km - Vs 620m/sec



— SA GMPE      - - - Sa High Freq Mod  
 — Sa Scaled to k=0.022      — Sa Vs-k Scaled  
 — Sa Swiss Target

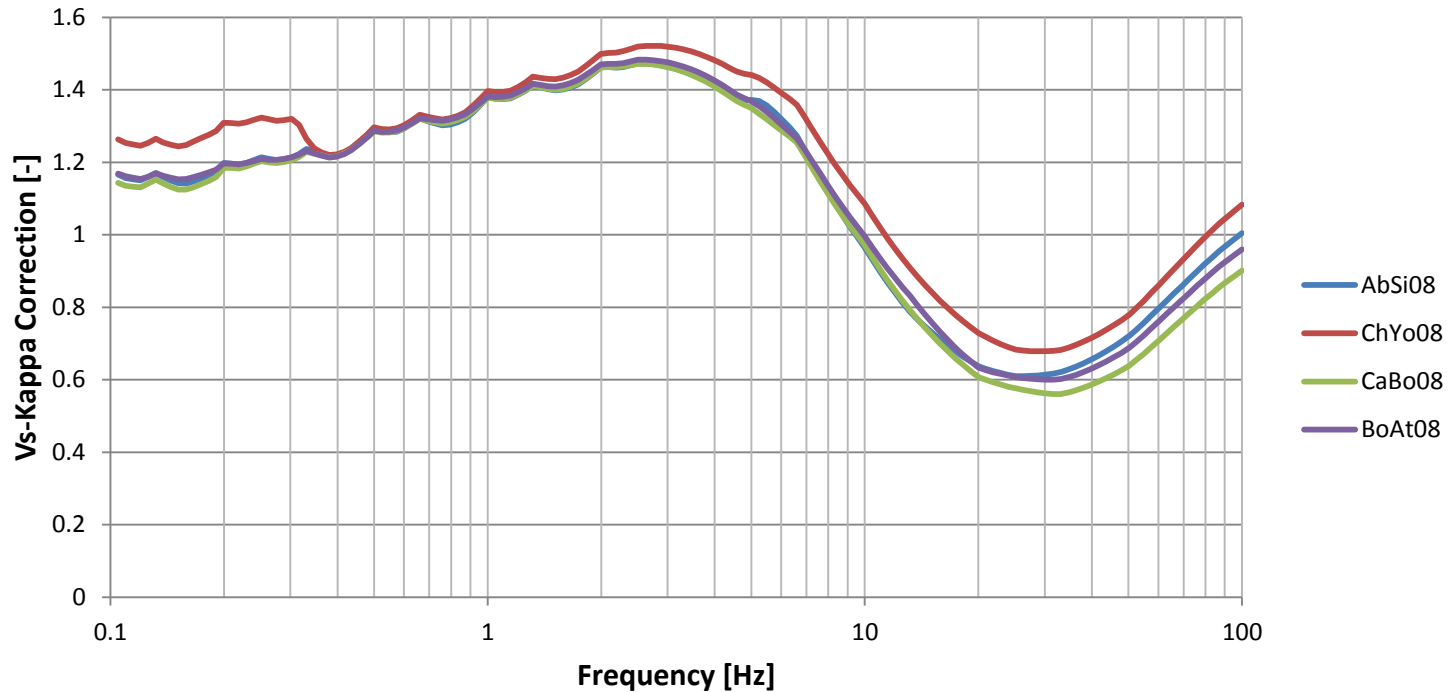
# Scaling Factors for CB08



# Example

(inverse of scale factor from WUS-CUES)

InverseRVT: Vs 2500 -> 620m/s, Kappa 0.006s -> 0.04s

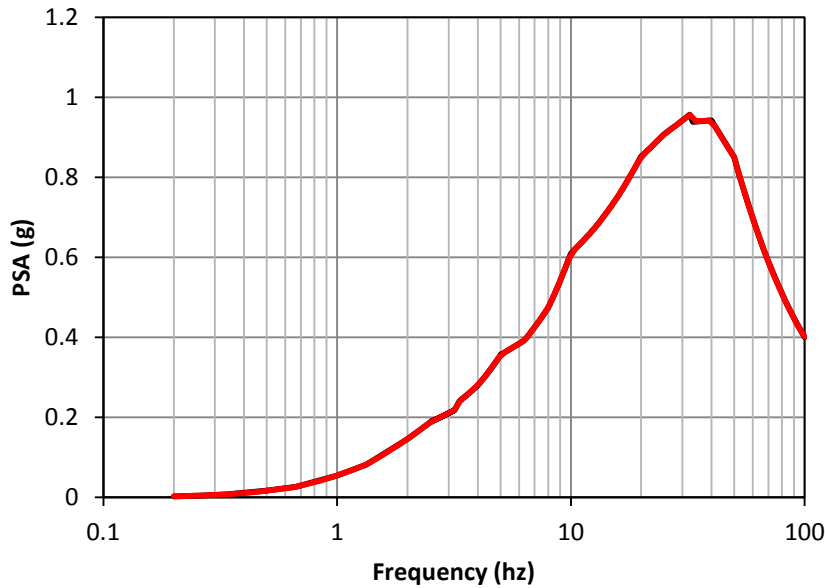


from: Philippe Renault, swissnuclear



# Vs-Kappa Scaling of AtBo06

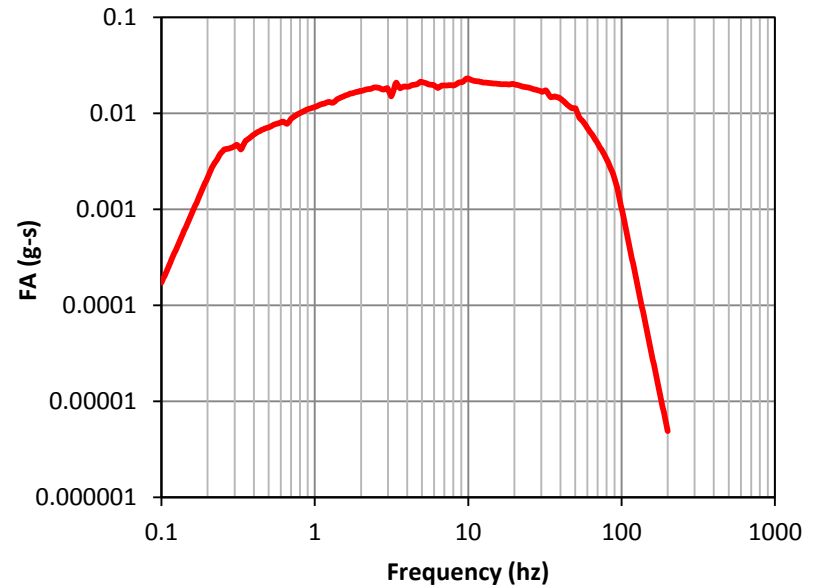
M6 - Rjb 10km - Vs 2200m/sec



— Sa GMPE — Sa RVT-Calc

IRVT  
➔

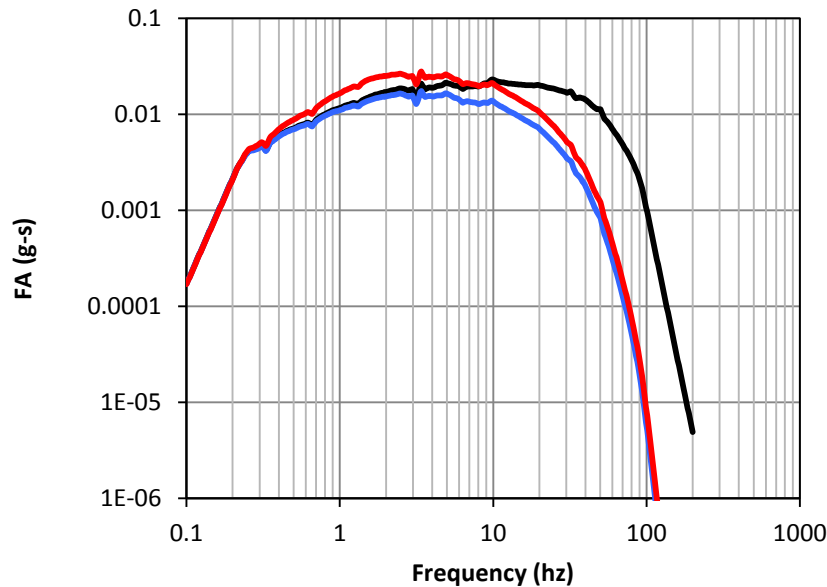
M6 - Rjb 10km - Vs 2200m/sec



— FAS RVT-Calc

# Vs-Kappa Scaling of AtBo06 (cont'd)

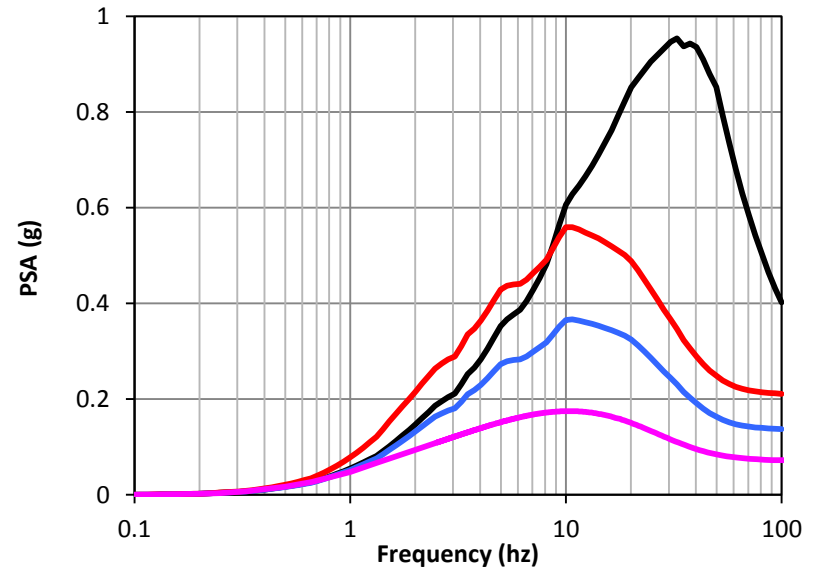
M6 - Rjb 10km - Vs 2200m/sec



— FAS  $k_0=0.0051$  — FAS Scaled to  $k=0.022$  — FAS Vs-k Scaled

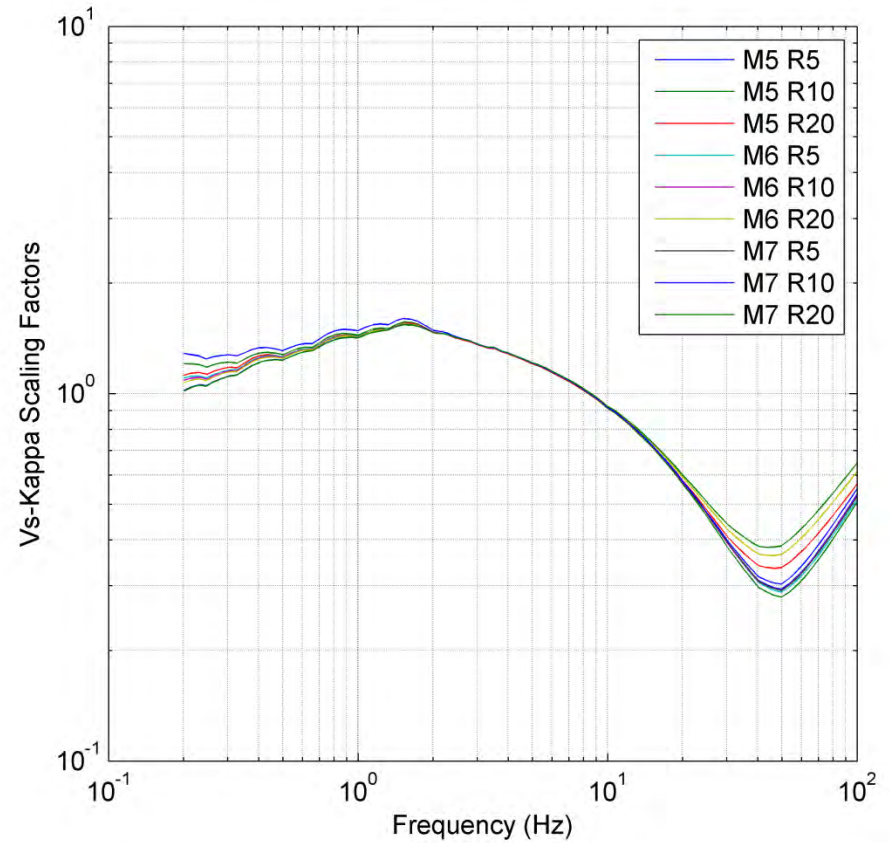
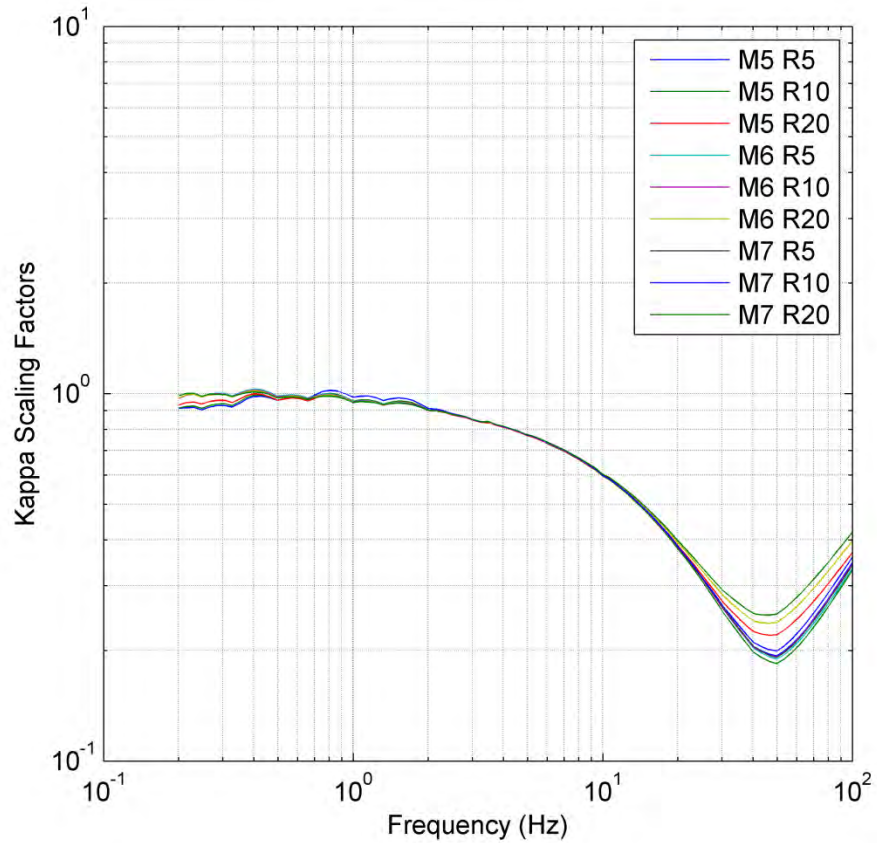
RVT  
→

M6 - Rjb 10km - Vs 2200m/sec



— SA GMPE — Sa Scaled to  $k=0.022$   
— Sa Vs-k Scaled — Sa Swiss Target

# Scaling Factors for AtBo06



# Potential Strengths of IRVT Approach

- Simple and transparent
- Applies scaling in Fourier domain as opposed to response spectra domain
- Does not require a full seismological model for stochastic parameters of host and target regions
- Does not assume that response spectral shape of GMPE is consistent with that of the point source stochastic model

# Potential Weaknesses of IRVT Approach

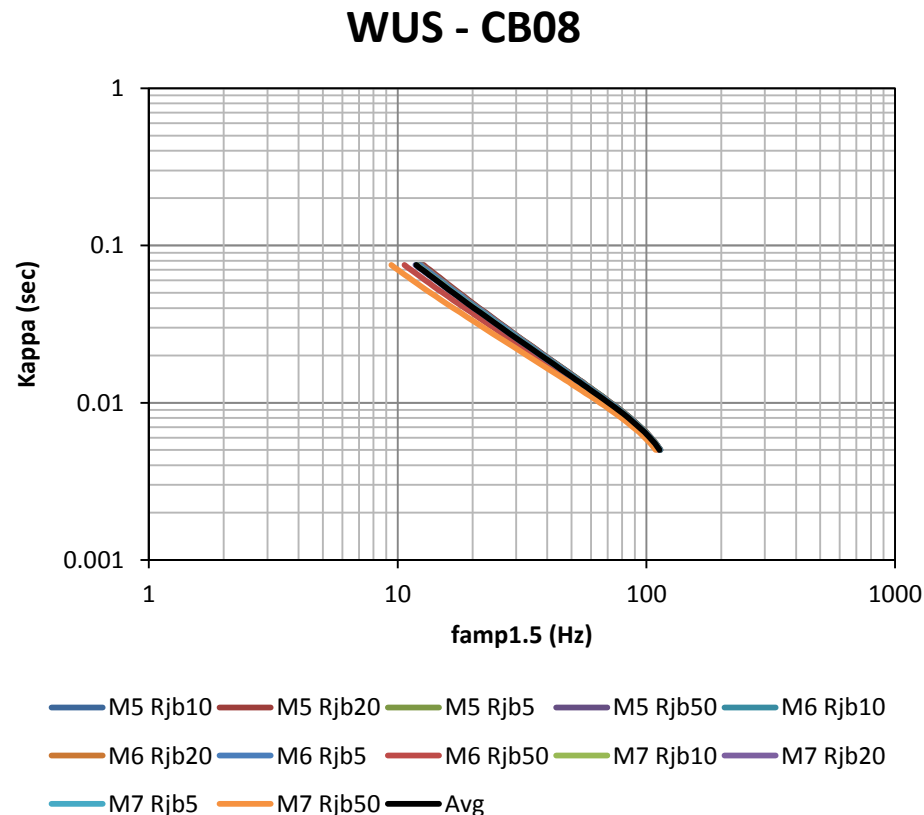
- Relies on IRVT to produce response spectra-compatible FAS
  - Saturation of response spectra with large kappa limits the ability to characterize high frequency content of ground motion
- Requires that Anderson & Hough (1984) kappa scaling fits reasonably well the high frequency FAS

# Empirical Approach

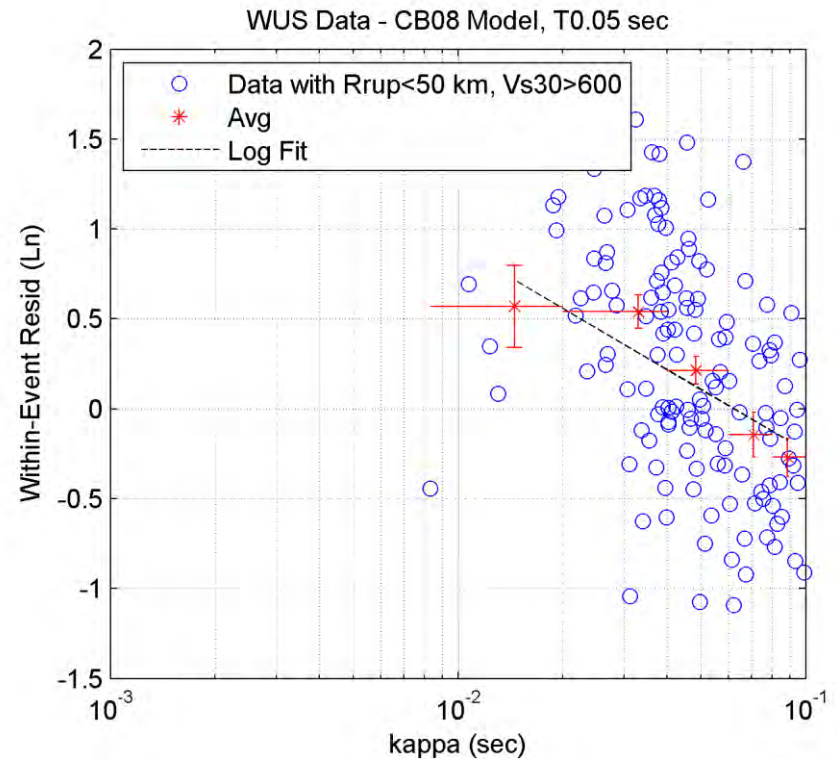
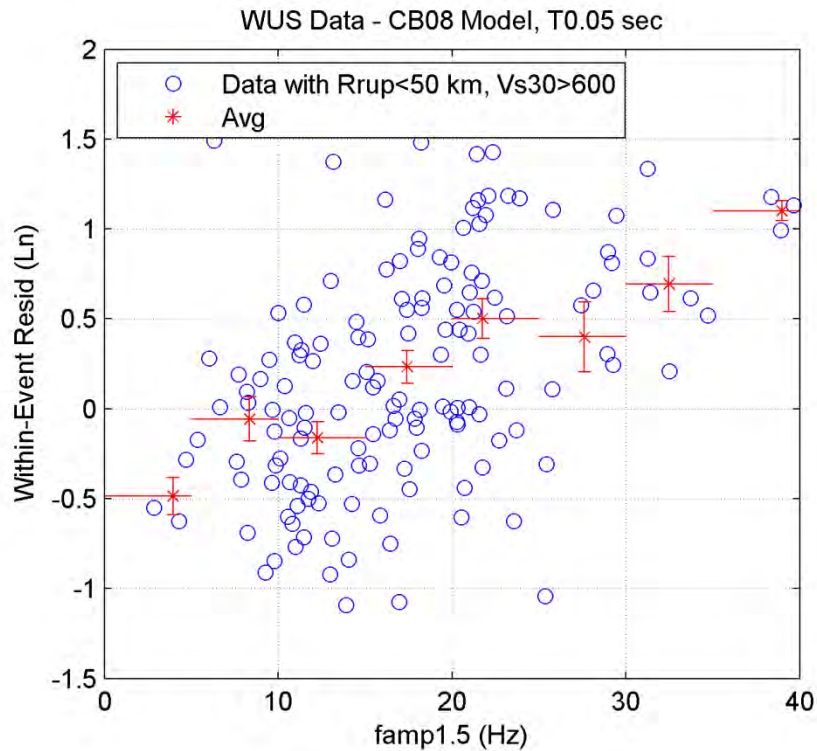
- Ideal approach
  - kappa estimates for each station in the data set
  - Evaluate within-event residuals dependence on kappa
- Proxy approach
  - Use the highest frequency at which the  $S_a$  is 1.5 times the PGA as a proxy for kappa
  - Develop conversion from the proxy to kappa based on the point source stochastic model
  - Evaluate within-event residuals dependence on kappa

# Kappa Estimates

Kappa-famp1.5 relationships developed from kappa-scaled GMPE response spectra using IRVT approach for a range of M-R scenarios



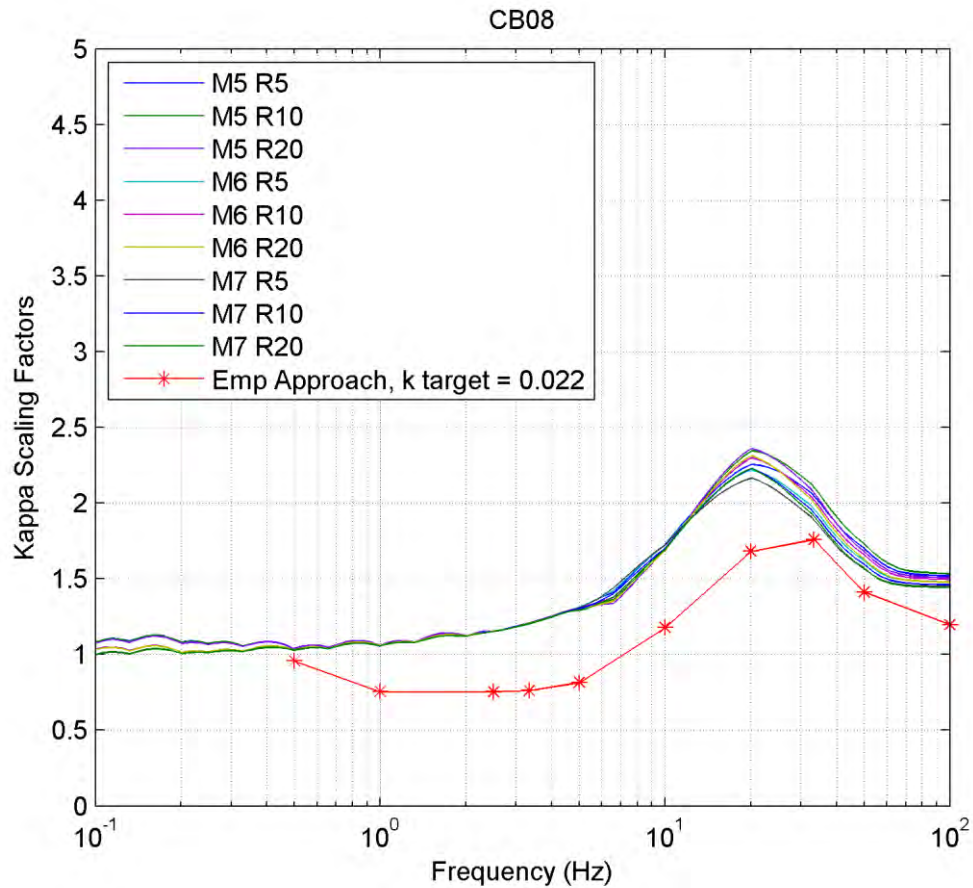
# Vs-Kappa Scaling of WUS Data – CB08



$$k \text{ Scaling Factor } (T \text{ 0.05 sec}) = \text{Exp}(-0.492\text{Ln}(k) - 1.368)$$



# Kappa Scaling Functions: WUS to Generic Swiss Rock Conditions



# Potential Strengths of Empirical Approach

- Relies on empirical ground motion data to evaluate  $V_s$ -kappa scaling
- Does not require seismological properties of host and target regions besides from target kappa value
- Simple and can be easily applied to evaluate scaling factors for a range of target kappa values

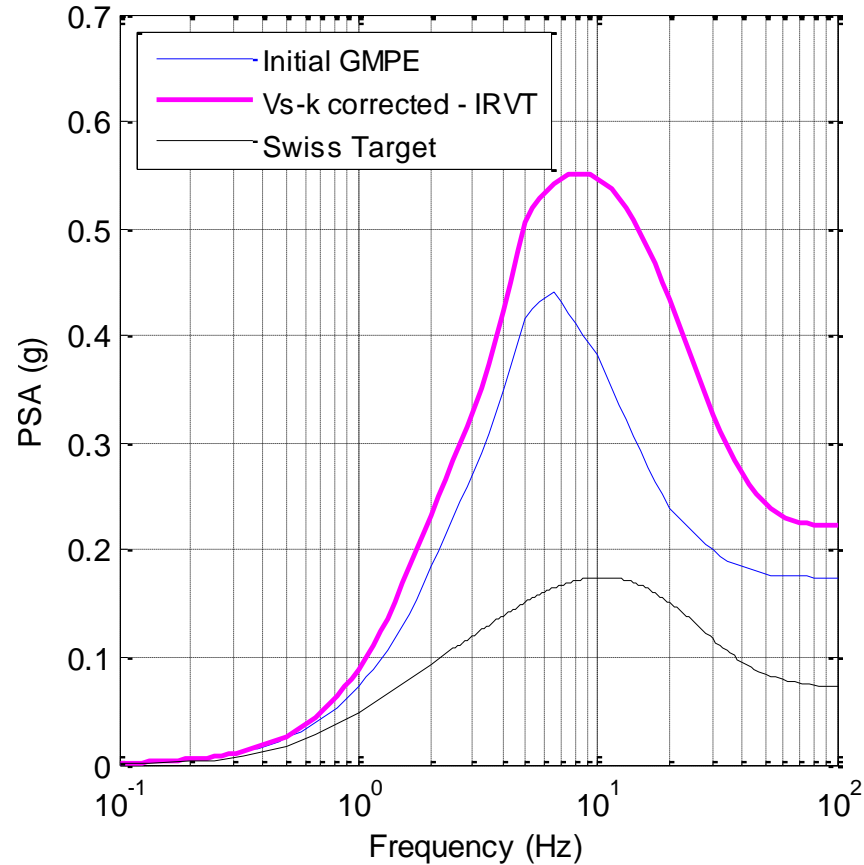
# Potential Weaknesses of Empirical Approach

- Few recordings available at short distance on stiff soil and rock sites to constrain kappa scaling
- Relies on kappa proxy
  - Different kappa values for a single station with multiple recordings
- Assumes GMPE scaling for high  $V_s30$  is correct

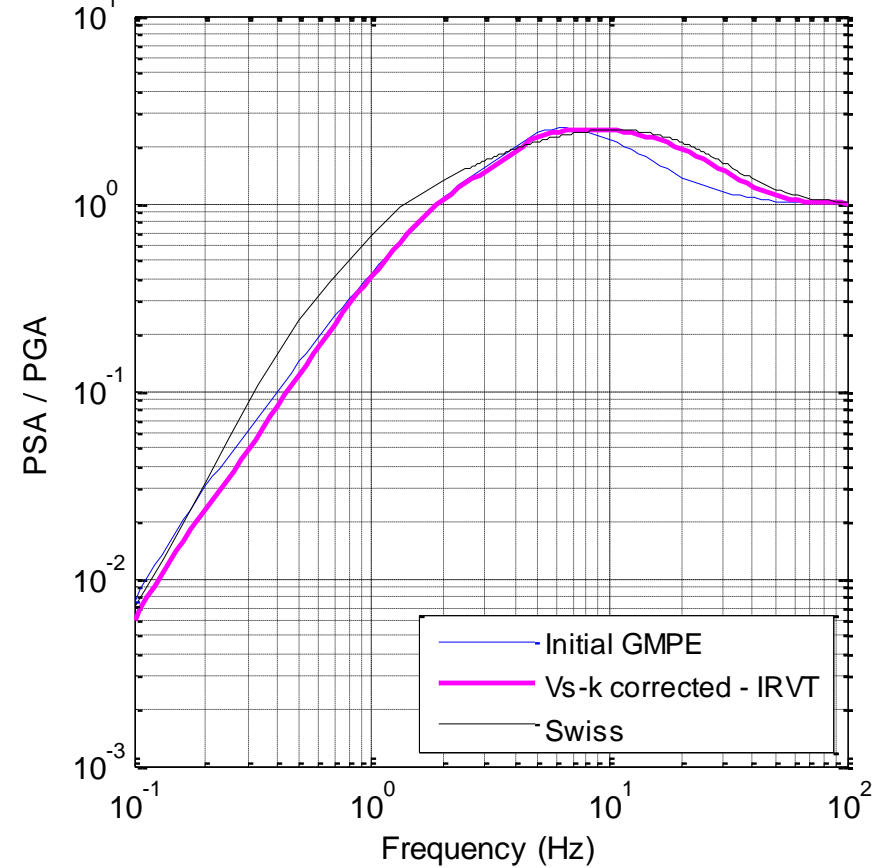


# Comparison of CB08 Corrected Spectra

CB08 - M6 - R10 - Vs800 - k0.04 to k0.022

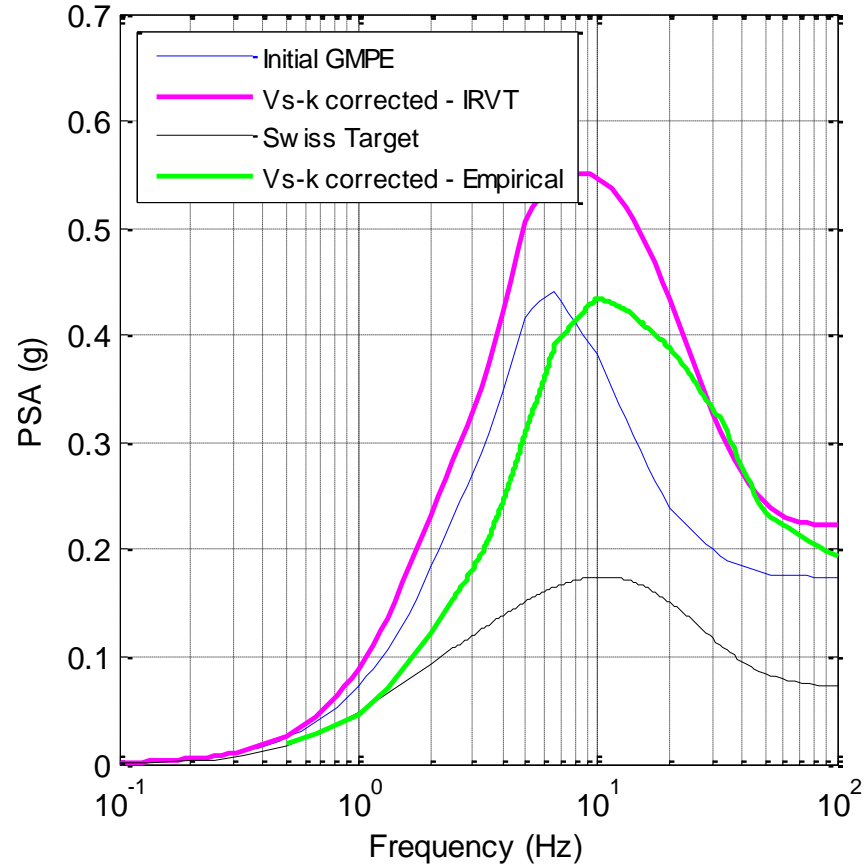


CB08 - M6 - R10 - Vs800 - k0.04 to k0.022

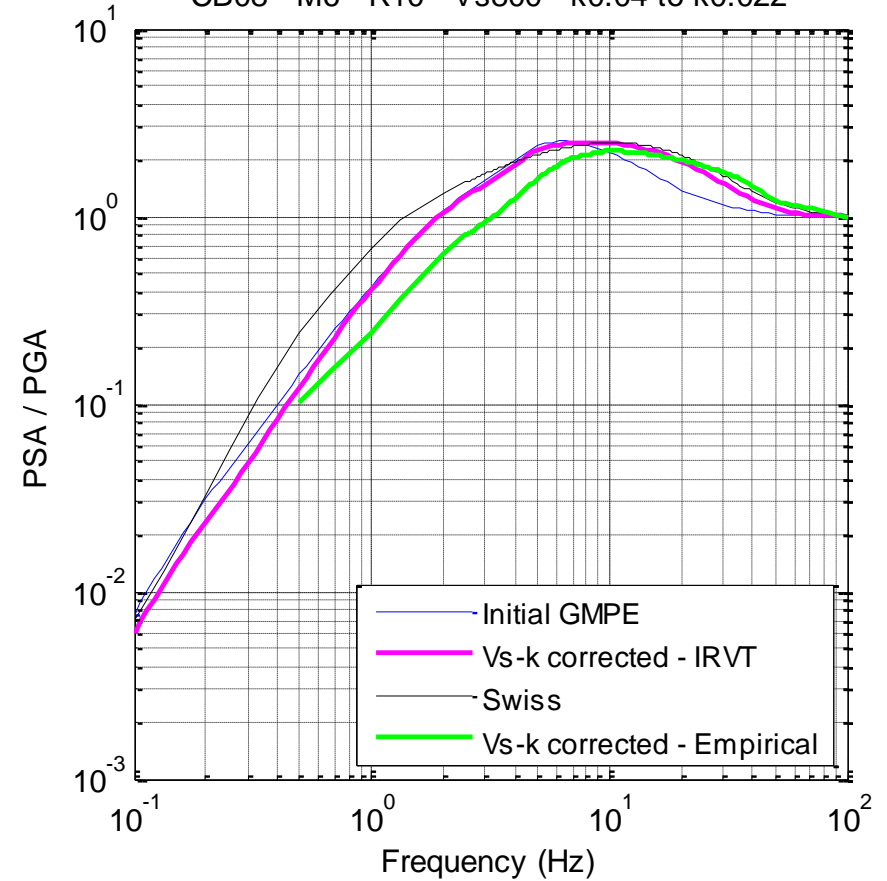


# Comparison of CB08 Corrected Spectra

CB08 - M6 - R10 - Vs800 - k0.04 to k0.022

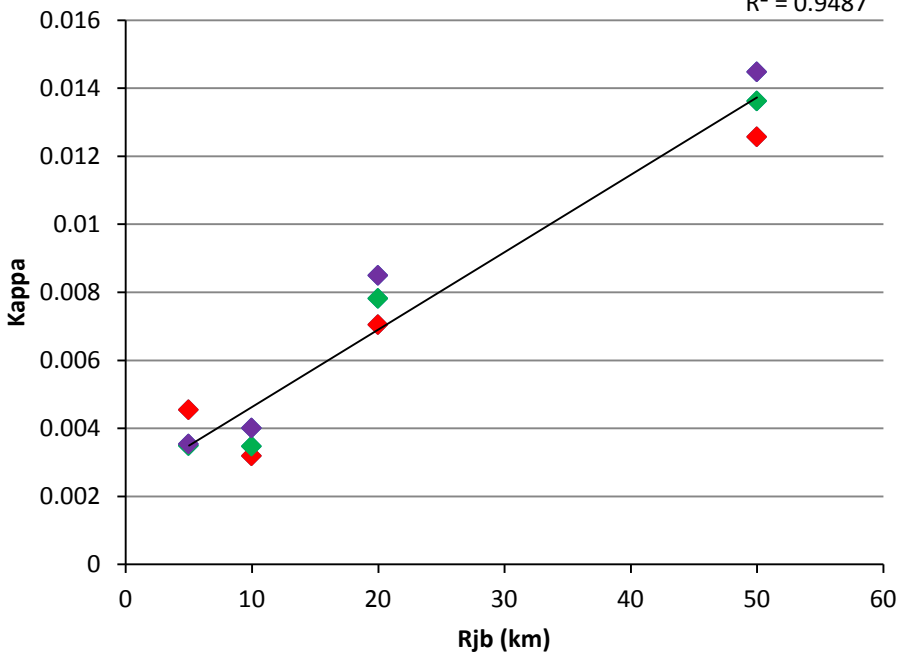


CB08 - M6 - R10 - Vs800 - k0.04 to k0.022



### AtBo06 - 2200m/sec

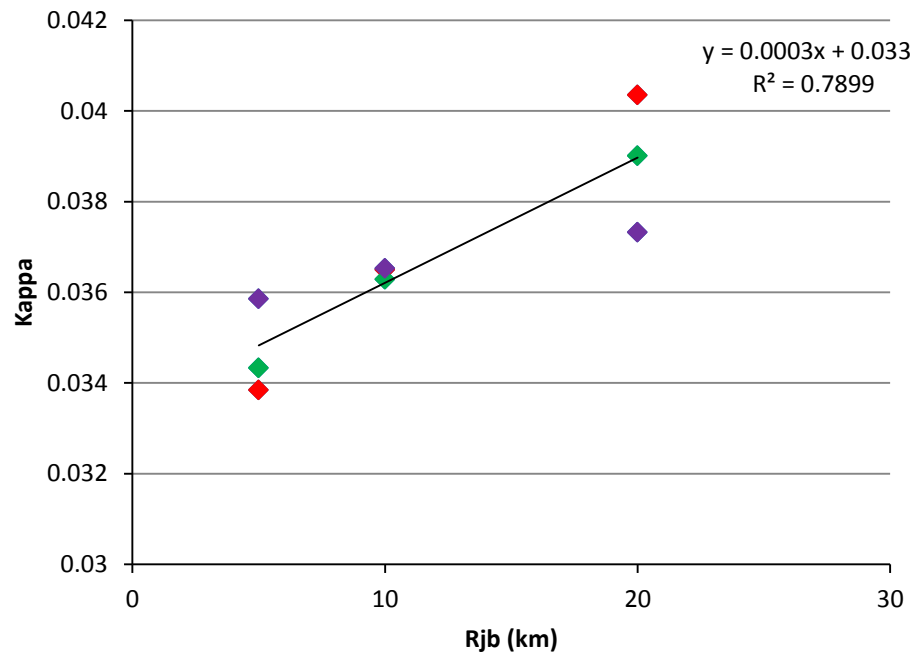
$$y = 0.0002x + 0.0024$$
$$R^2 = 0.9487$$



◆ M5    ◆ M6    ◆ M7    — Linear (All M)

### AkBo10 - 800m/sec

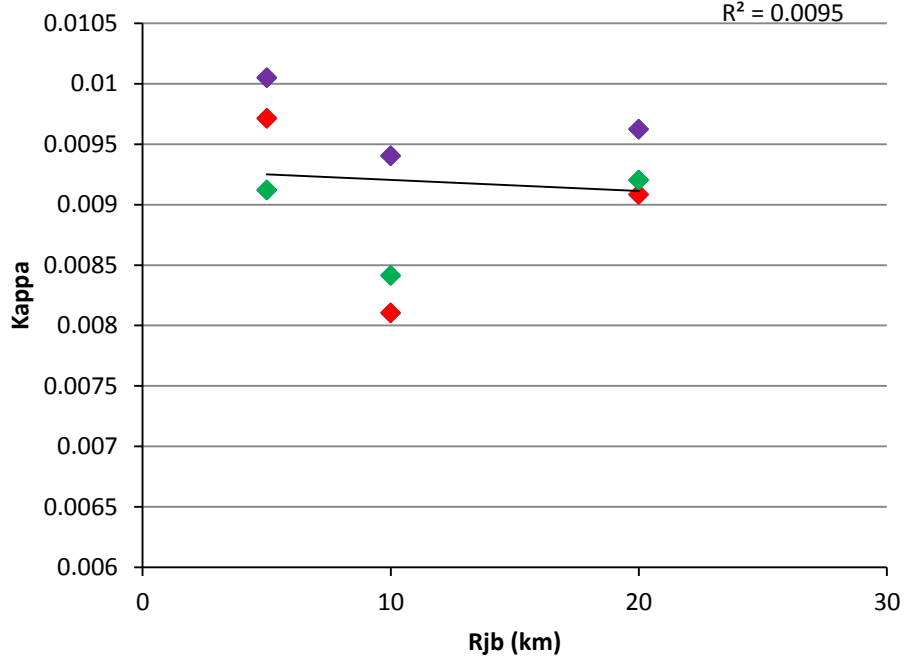
$$y = 0.0003x + 0.0334$$
$$R^2 = 0.7899$$



◆ M5    ◆ M6    ◆ M7    — Linear (All M)

### Toro02 - 2800m/sec

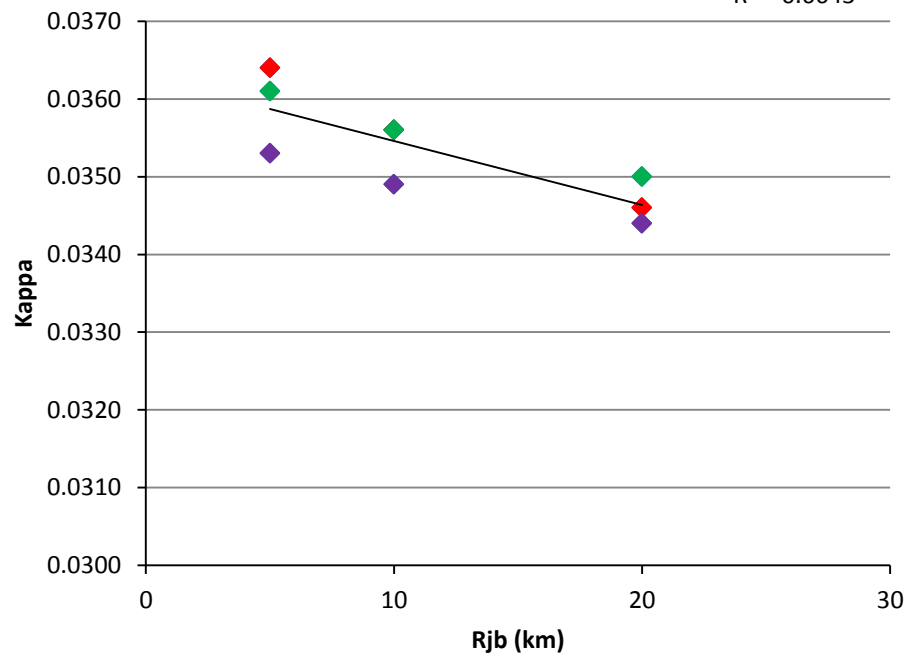
$$y = -9E-06x + 0.0093$$
$$R^2 = 0.0095$$



◆ M5    ◆ M6    ◆ M7    — Linear (All M)

### CY08 - 800m/sec

$$y = -8E-05x + 0.0363$$
$$R^2 = 0.6643$$



◆ M5    ◆ M6    ◆ M7    — Linear (All M)