

# **Empirical-Stochastic Ground Motion Prediction for Eastern North America**

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# **Types of Source Models for ENA**

- **Single-Corner Frequency Model (e.g., Frankel et al., 1996; Toro et al., 1997)**
- **Double-Corner Frequency Model (e.g., Atkinson and Boore, 1995; Silva et al., 2002)**
- **Hybrid-Empirical Model (e.g., Atkinson, 2001; Campbell, 2003)**
- **Finite-Source Model (e.g., Somerville et al., 2001)**

- The objective of this study is to revise the 2003 Campbell attenuation relationship for ENA, using **Hybrid-empirical** model, combining **single** and **double source spectra**, and changing **magnitude-dependent stress drop** in the WNA and ENA regions which have different seismological parameters.
- **Empirical** refers to the empirical attenuation models developed in WNA (a host region) and **Hybrid** refers to models that transform attenuation relationships to ENA (a target region) by using seismological parameters.

# Hybrid-Empirical Model

Earthquake Source Spectra

Geometrical Attenuation Factor

$$\frac{Y_{ENA}}{Y_{WNA}} = \frac{E_{ENA}(f_c)}{E_{WNA}(f_c)} \times \frac{A_{ENA}(f)}{A_{WNA}(f)} \times \frac{G_{ENA}(R)}{G_{WNA}(R)} \times \exp[R(\gamma_{WNA} - \gamma_{ENA}) + \pi f(\kappa_{WNA} - \kappa_{ENA})]$$

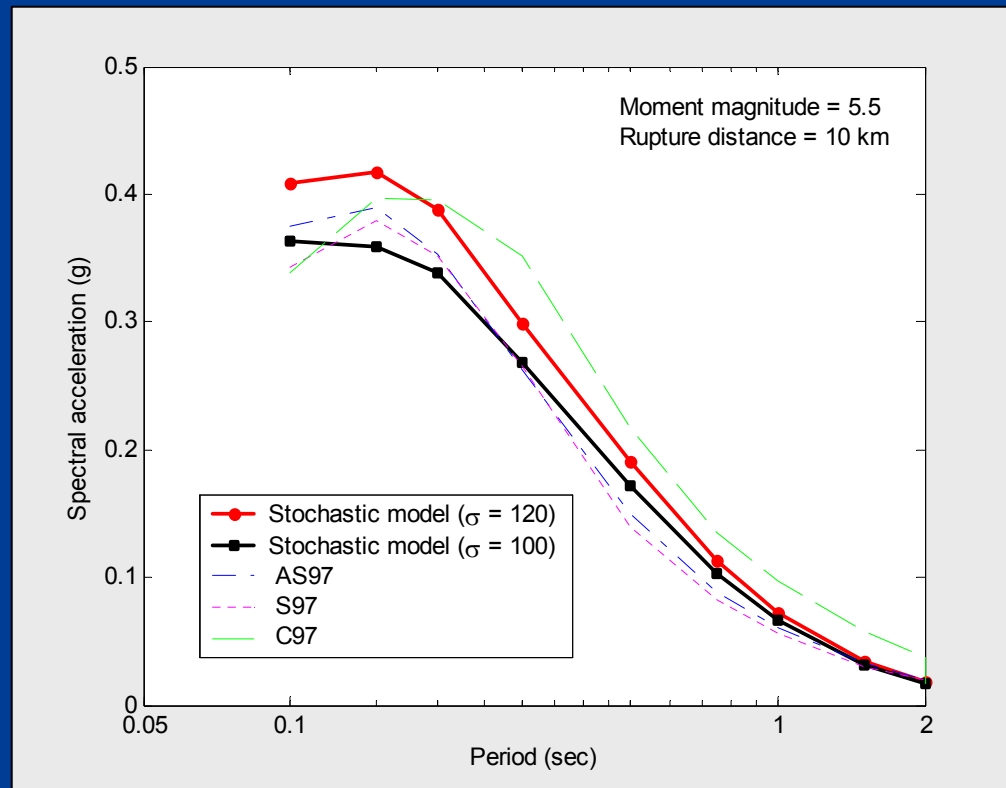
Crustal Amplification Factors

Filter Function of the Transfer Media  
and Local Site Conditions

# Hybrid-Empirical Attenuation Relationships

- **The 2001 Atkinson relation**
  - Sadigh et al., 1997 from WNA
  - Elimination of Source Model
- **The 2003 Campbell relation**
  - Four Attenuation Relationships from WNA
  - Single-Corner Source Model
  - Constant Stress drop of 100 bars for WNA
- **The 2005 Tavakoli-Pezeshk relation**
  - Three Attenuation Relationship from WNA
  - Single-Corner Source Model at Long Distances
  - Double-Corner Source Model at Short Distances ( $< 30\text{km}$ )
  - Magnitude-Dependent Stress drop for WNA

# Effect of Magnitude-Dependent Stress Drop in WNA

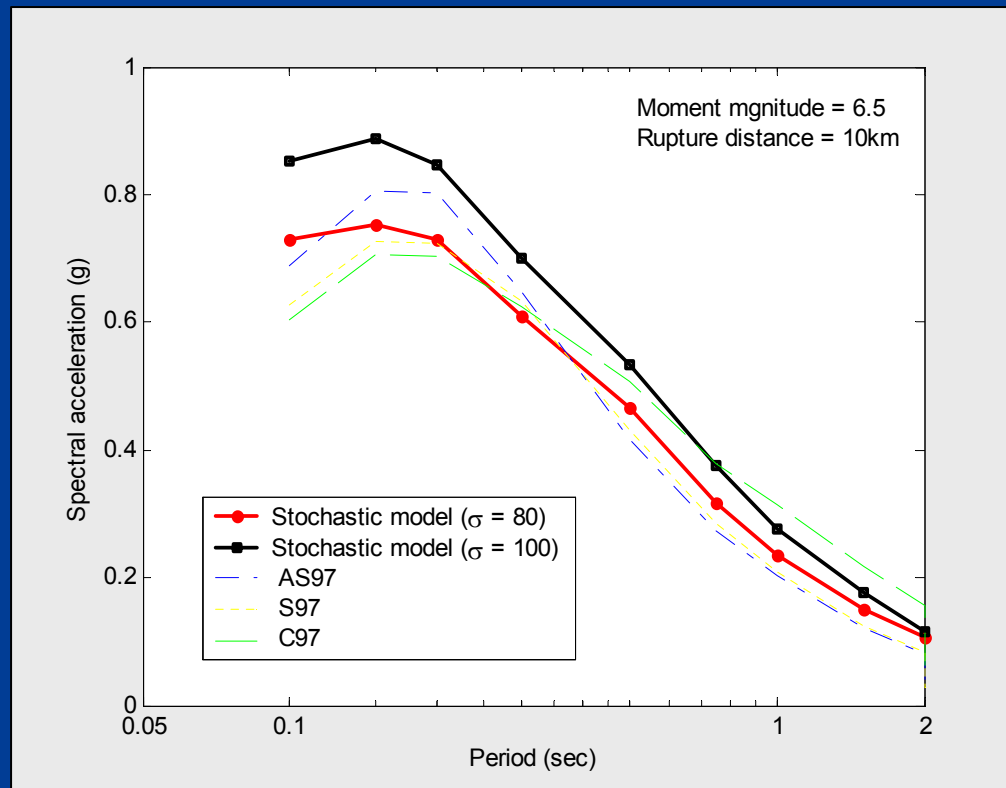


**AS97 - Abrahamson and Silva (1997)**

**S97 - Sadigh et al. (1997)**

**C97 - Campbell (1997)**

# Effect of Magnitude-Dependent Stress Drop in WNA

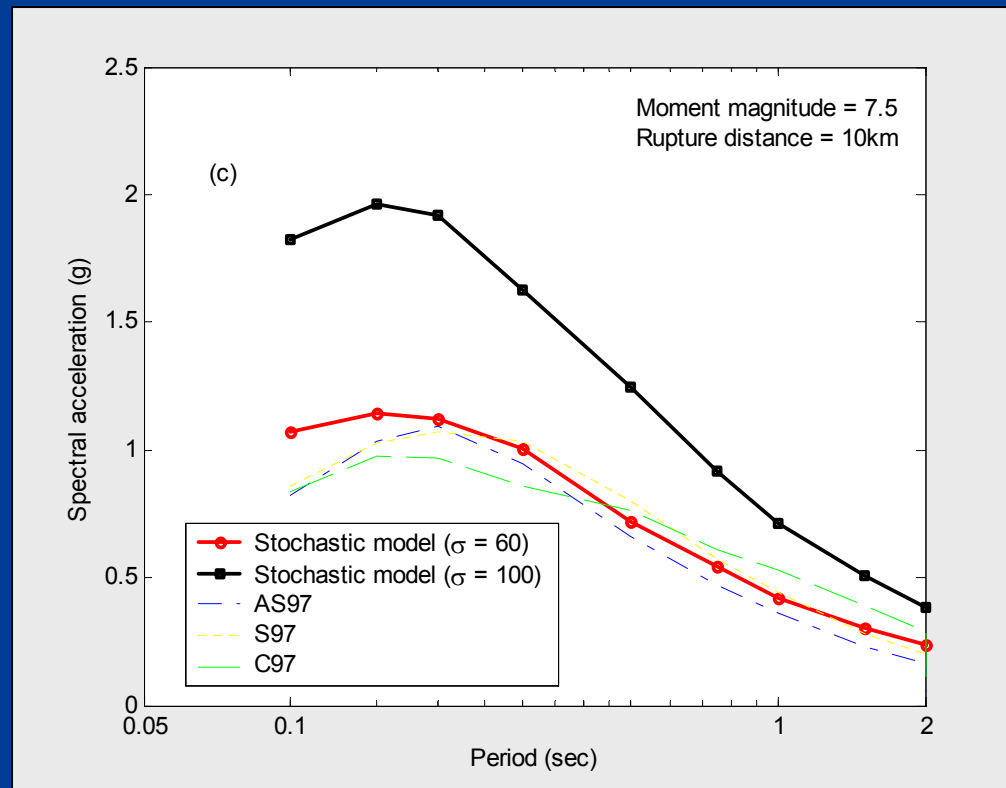


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# Effect of Magnitude-Dependent Stress Drop in WNA



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# Shape of Source Spectra and Model Parameters

- **Source Spectra**
  - Shape
  - Corner Frequencies

Atkinson and Boore (1995)

$$S(M_0, f) = \left[ \frac{1-\varepsilon}{1+\left(\frac{f}{f_a}\right)^2} + \frac{\varepsilon}{1+\left(\frac{f}{f_b}\right)^2} \right]$$

- **Model Parameters**
  - Geometrical Spreading
  - Quality Factor
  - Path Duration
  - Site Amplification
  - Site Diminution (Kappa)

$$Y_{ENA} = 0.00122f^{0.64}$$

$$Y_{WNA} = 0.00499f^{0.55}$$

# New Information to Incorporate into Ground Motion Simulation

- We considered the effects of **near field saturation, focal depth, and stress drop** on ground motions.
- We used the double corner-frequency source model to consider the effect of **finite-fault modeling** at short distances and large magnitudes.
- We used the single corner-frequency source model for the far-field ground motions.
- We used three empirical attenuation relationships from WNA.
- A composite functional form of the attenuation model for ENA based on the existing attenuation relationships in WNA.

# Attenuation Relationship Developed for ENA

$$\ln(Y) = f_1(M_w) + f_2(r_{rup}) + f_3(M_w, r_{rup})$$

Magnitude Scaling

Distance Scaling

Magnitude-Distance Scaling

$$f_1(M_w) = C_1 + C_2 M_w + C_3 (8.5 - M_w)^{2.5}$$

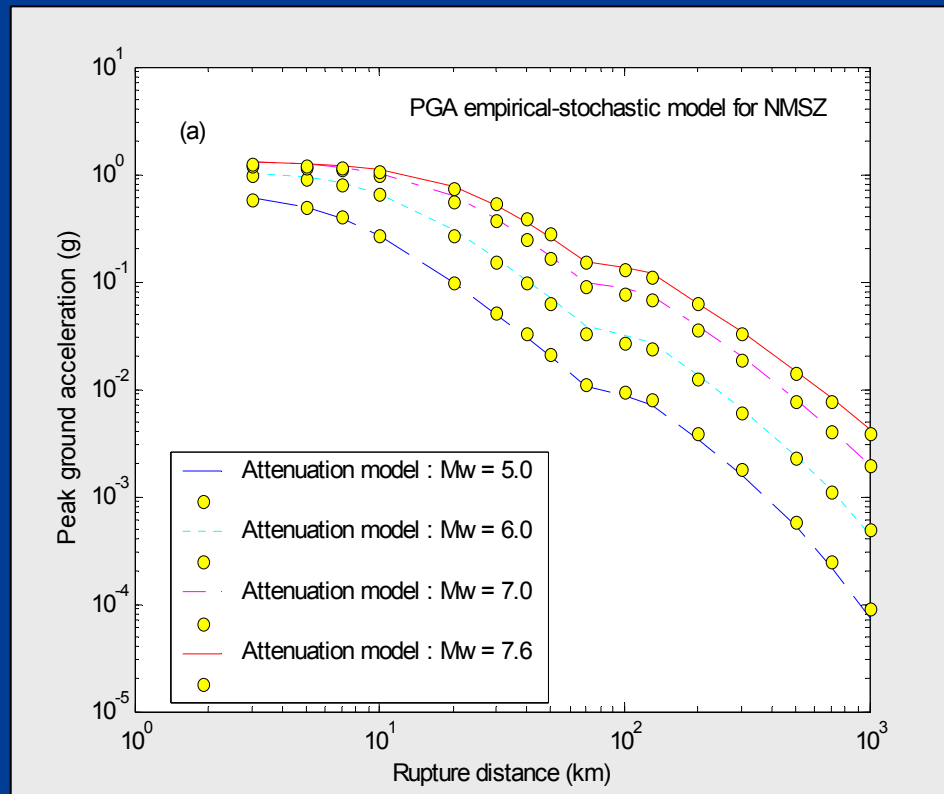
$$f_3(M_w, r_{rup}) = (C_4 + C_{13} M_w) \ln R + (C_8 + C_{12} M_w) R$$

$$f_2(r_{rup}) = \begin{cases} C_9 \ln(r_{rup} + 4.5) & r_{rup} < 70 \text{ km} \\ C_{10} \ln\left(\frac{r_{rup}}{70}\right) + C_9 \ln(r_{rup} + 4.5) & 70 < r_{rup} < 130 \text{ km} \\ C_{11} \ln\left(\frac{r_{rup}}{130}\right) + C_{10} \ln\left(\frac{r_{rup}}{70}\right) + C_9 \ln(r_{rup} + 4.5) & r_{rup} < 130 \text{ km} \end{cases}$$

$$R = \sqrt{r_{rup}^2 + \left( C_5 \exp \left[ C_6 M_w + C_7 (8.5 - M_w)^{2.5} \right] \right)^2}$$

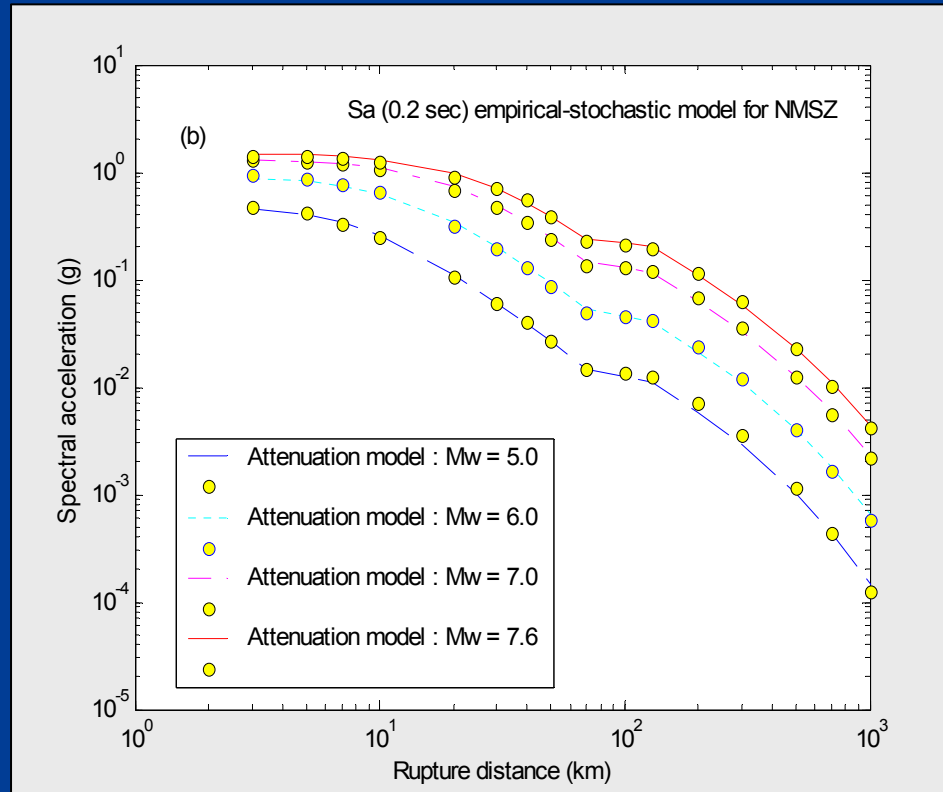
# Empirical-Stochastic attenuation relation developed in this study for the ENA/NMSZ

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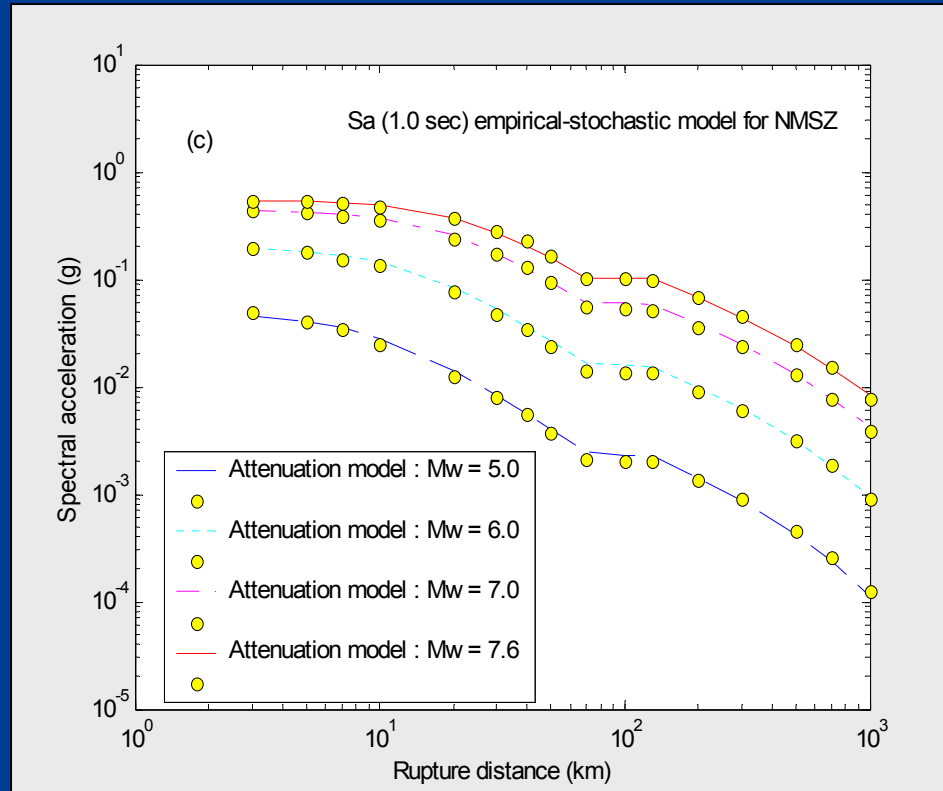
# Empirical-Stochastic attenuation relation developed in this study for the ENA/NMSZ

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# Empirical-Stochastic attenuation relation developed in this study for the CUS/NMSZ

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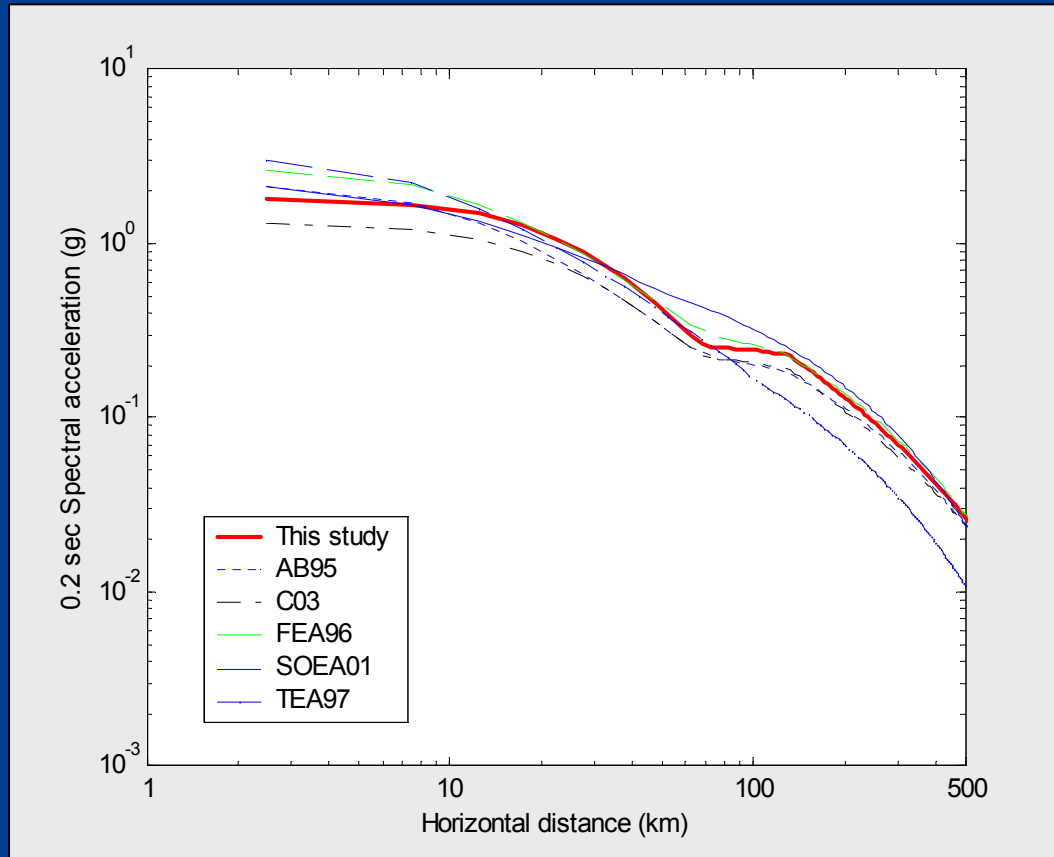


# Optimization Using Hybrid Genetic Algorithm (HGA)

$$l(\theta|Y_{ij}) = \min \left\{ [Y_{ij} - f(x_{ij}, \theta)]^t [Y_{ij} - f(x_{ij}, \theta)] \right\}$$

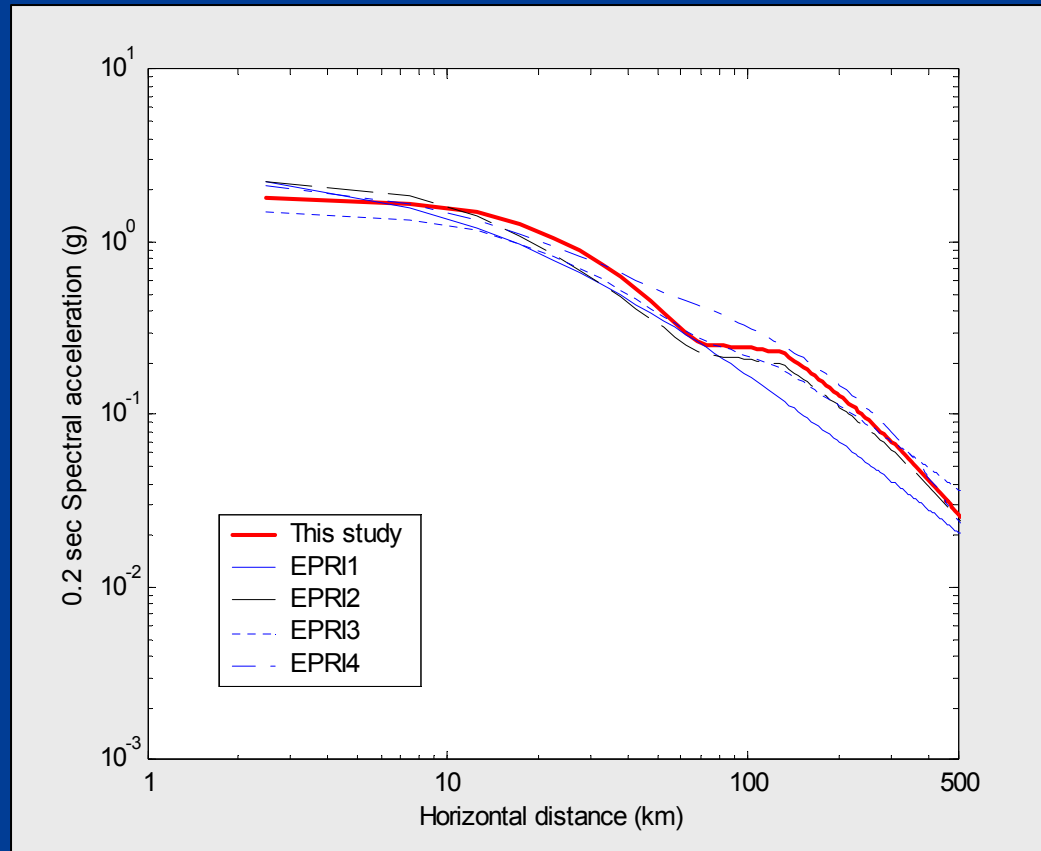
- HGA is a directed stochastic search technique (a **derivative-free approach**) that is able to provide an optimal solution to compute the vector of the model parameters in attenuation relationships.
- A HGA consists of **initialization, evaluation, reproduction/selection, crossover, and mutation**.
- The HGA can be applied to **complex attenuation models** with several **variance components**.

# Comparison of Results with Other Attenuation Relations for ENA

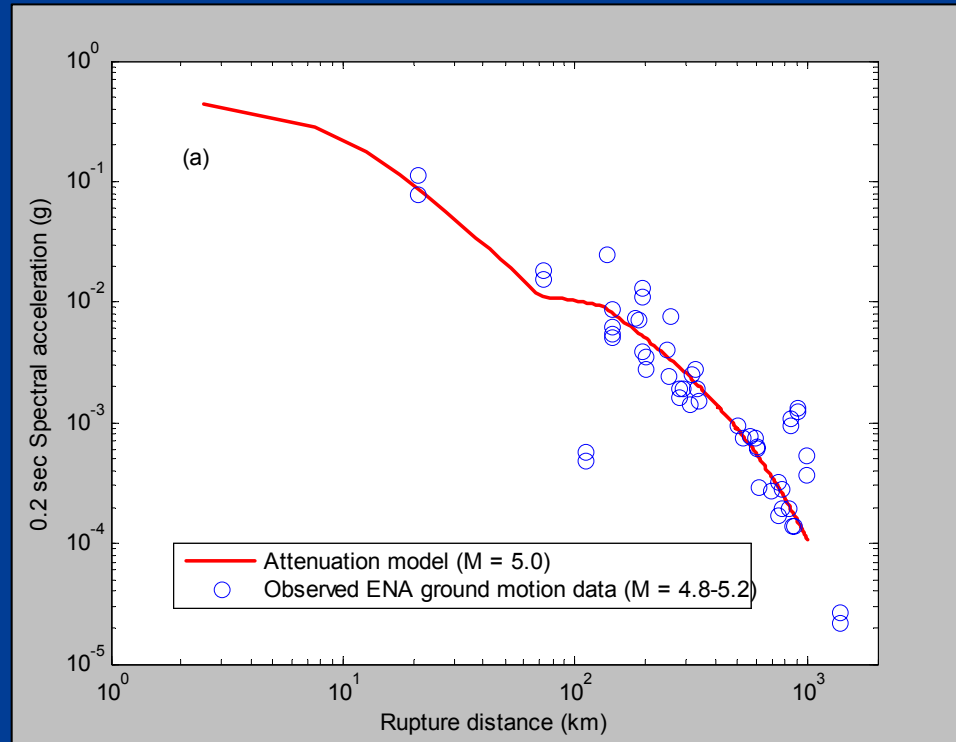




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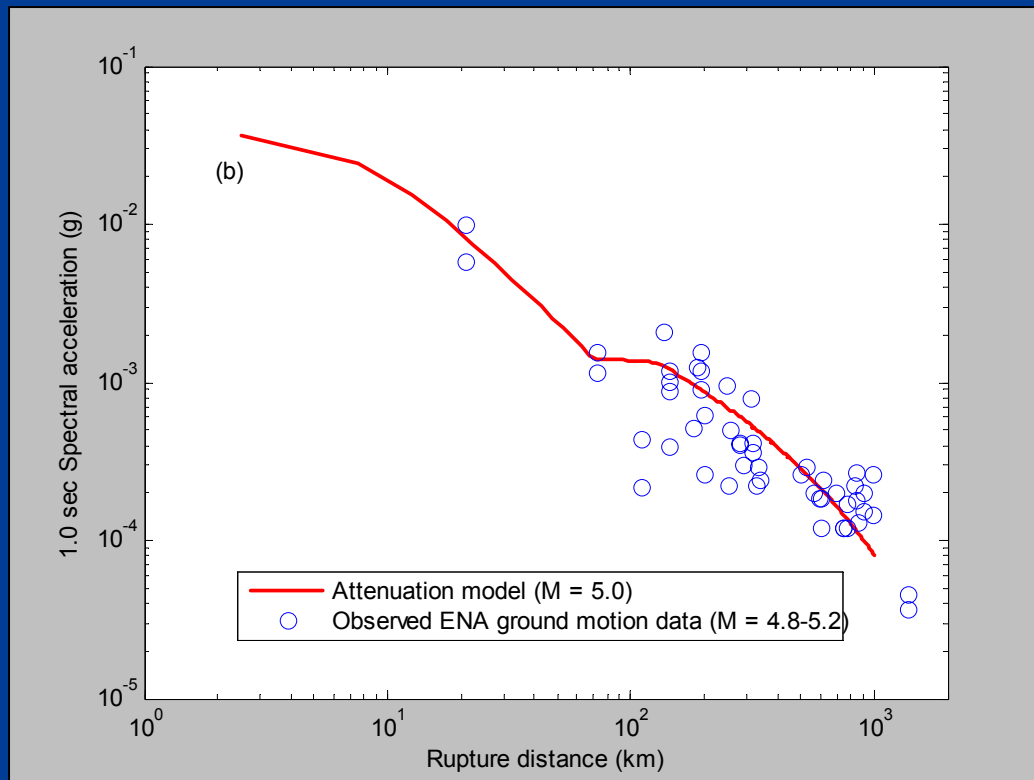


# Comparison of Results with Observed Ground Motion Data for ENA



Data from Kafka and Atkinson (2005)

# Comparison of Results with Observed Ground Motion Data for ENA



# Conclusions

- Consider both **double and single corner source spectra** for WNA and ENA.
- Consider the **HGA** to estimate the epistemic and aleatory uncertainties.
- Consider the effects of **near field saturation**, **focal depth**, and **stress drop** on ground motions.
- Consider the **effect of finite-faults** using the finite-fault stochastic models.
- Consider the effects of **rupture propagation** and **directivity** to define finite-fault source model for near-field ground motion characteristics in ENA.