

Development of Regional Hard Rock Attenuation Relations for CEUS, Mid-Continent and Gulf Coast Areas

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Pacific Engineering and Analysis

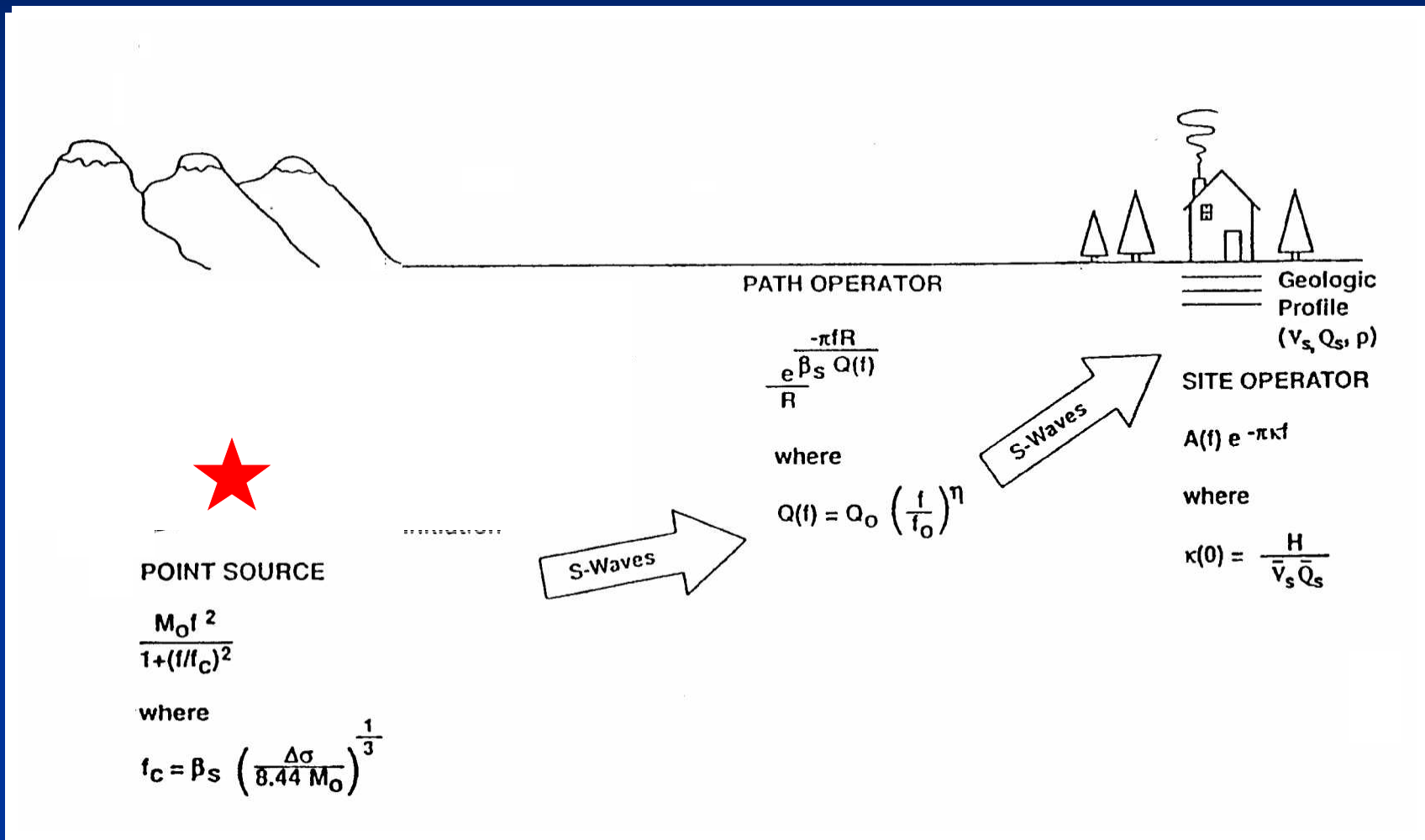
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Introduction

- Stochastic Point Source Model
- Model Validation
- Input Parameter Variability
- Update Summary

Stochastic Point Source Model



Model Validation

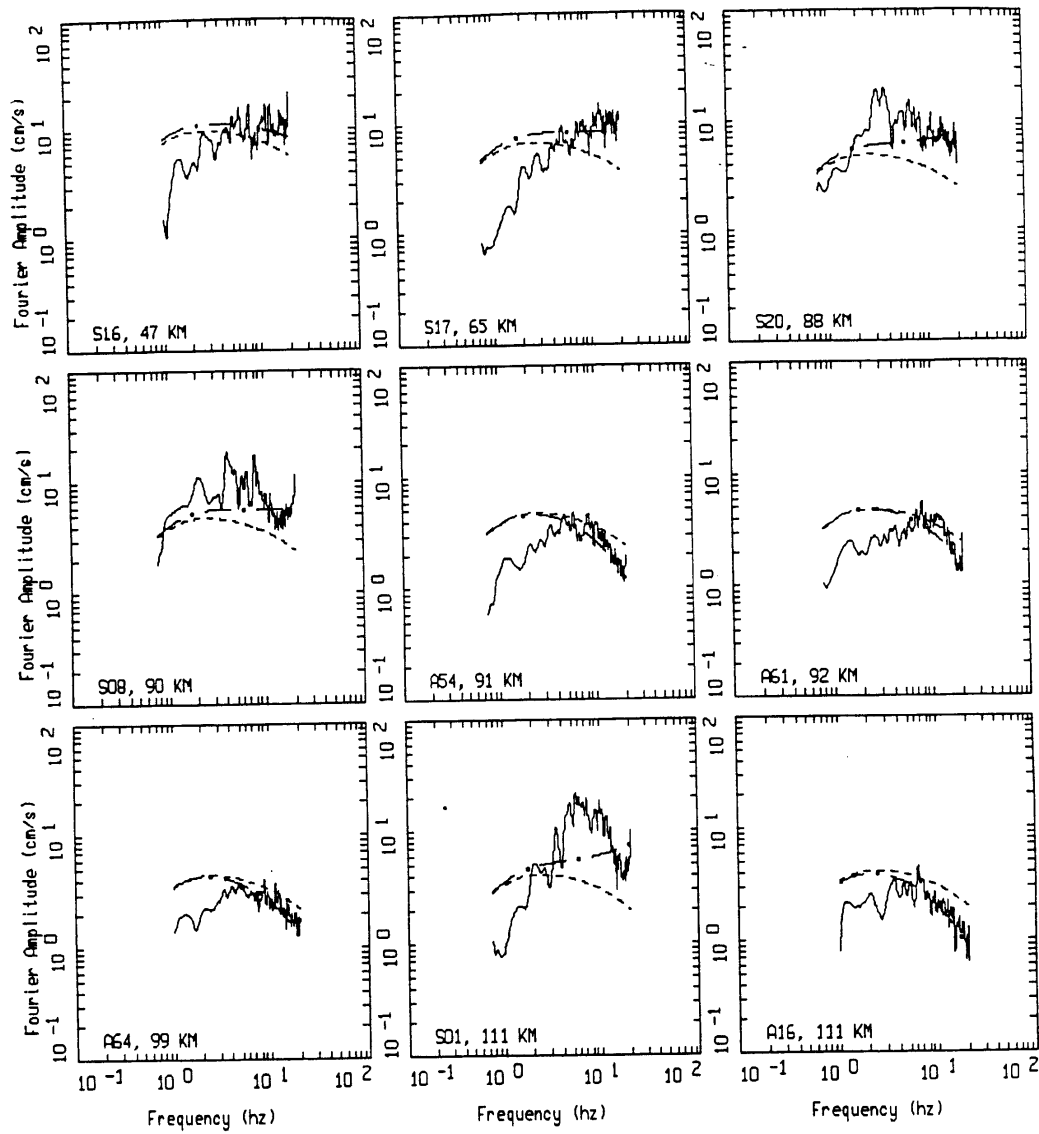
(Silva et al., 1997)

- 16 Earthquakes (M5.3 – M7.4)
- 503 Sites
 - 159 Rock
 - 344 Soil
- Distance Range: 1 – 460 km

Earthquake	M	Dist (km)	Rock Sites	Total Sites
1971 San Fernando	6.6	3 – 218	21	39
1978 Tabas	7.4	3 – 90	3	4
1979 Coyote Creek	5.7	3 – 30	3	10
1979 Imperial Valley	6.4	1 – 50	2	35
1979 Imperial Valley (AS)	5.3	12 – 52	0	16
1984 Morgan Hill	6.2	1 – 70	8	29
1985 Nahanni	6.8	6 – 16	3	3
1986 North Palm Springs	6.0	1 – 90	9	29
1987 Whittier	6.0	10 – 80	18	88
1987 Superstition Hills	6.4	1 – 28	1	12
1988 Saguenay	5.8	47 – 460	22	22
1989 Loma Prieta	6.9	5 – 90	33	53
1992 Little Skull Mtn.	5.7	15 – 98	8	8
1992 Landers	7.2	1 – 177	5	57
1992 Cape Mendocino	6.8	8 – 45	1	5
1994 Northridge	6.7	7 – 147	23	94

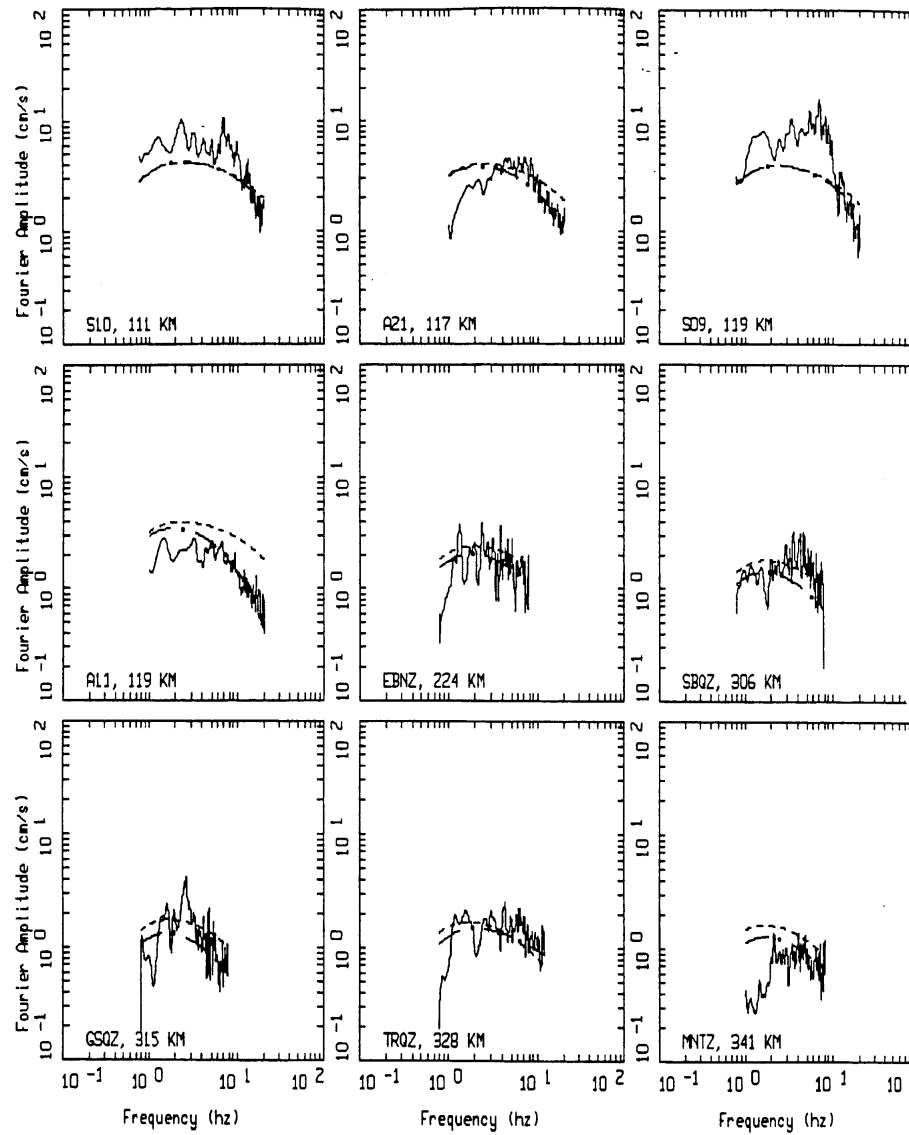
Saguenay EQ Inversion: Input Parameters

- 22 Rock Sites (Distances: 47 – 460 km)
- Crustal Model (Hartzell et al., 1994)
- Point Source Depth = 25.7 km
- Starting Stress Drop = 300 bars
- Starting Kappa = 0.008 sec



SAGUENAY EARTHQUAKE, M=5.8, PAGE 1 OF 3.

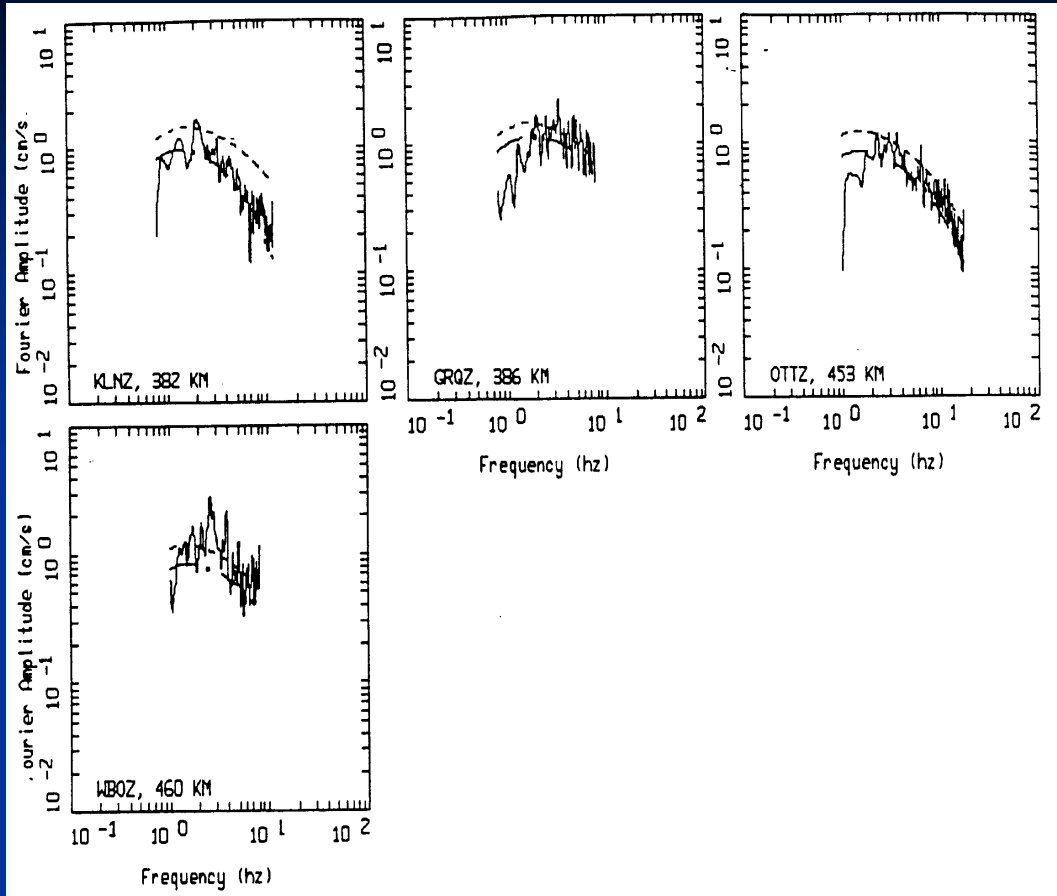
——— DATA
 - - - - - INITIAL MODEL
 - . - . - FINAL MODEL



SAGUENAY EARTHQUAKE, M=5.8, PAGE 2 OF 3.

LEGEND

- DATA
- - - INITIAL MODEL
- · - FINAL MODEL

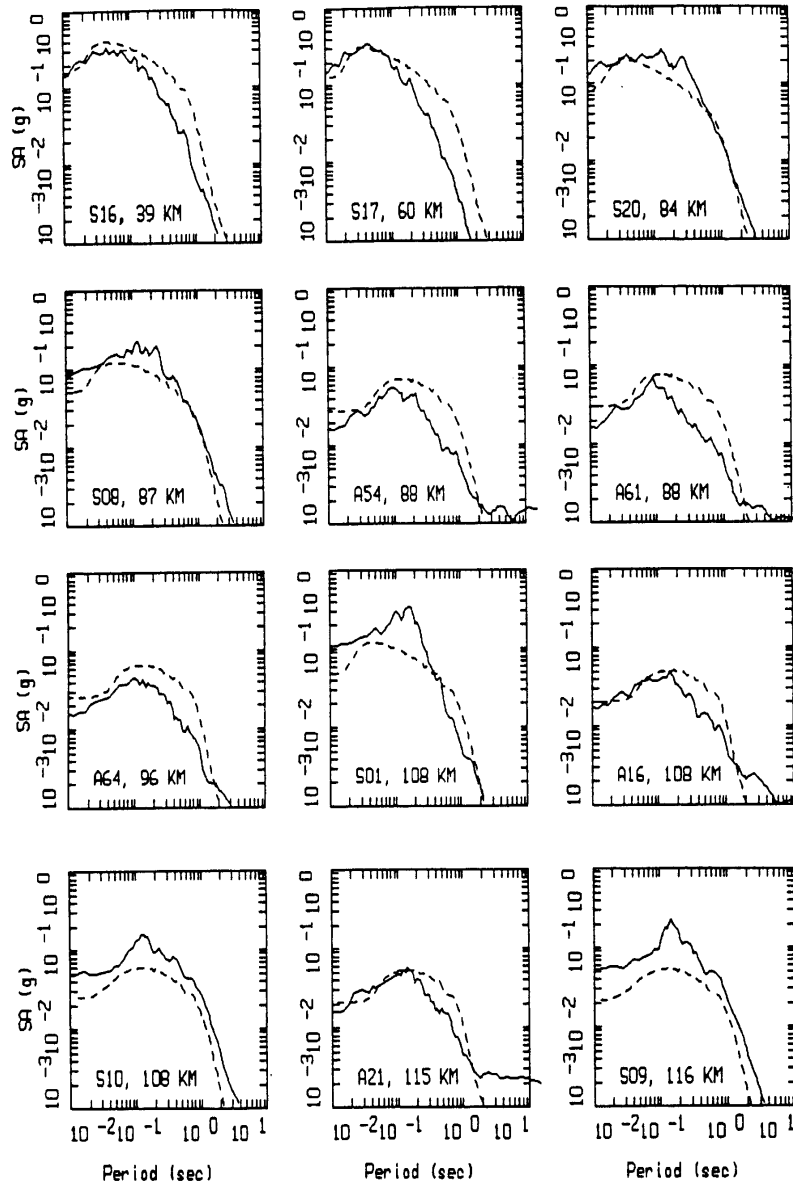


SAGUENAY EARTHQUAKE, M=5.8, PAGE 3 OF 3.

——— DATA
 - - - - INITIAL MODEL
 - . - . FINAL MODEL

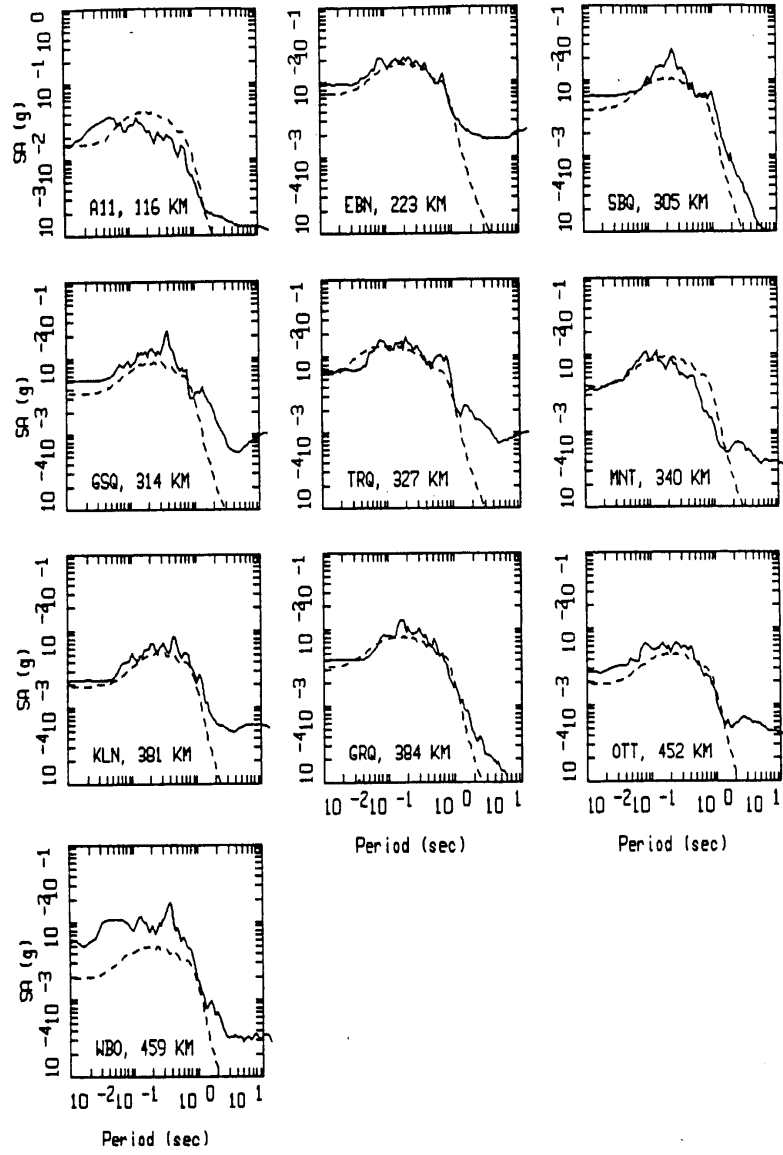
Saguenay EQ Inversion: Results

- Stress Drop = 572.2 ± 25.4 bars
- Kappa Average = 0.023 sec
- $Q(f) = 351f^{0.84}$



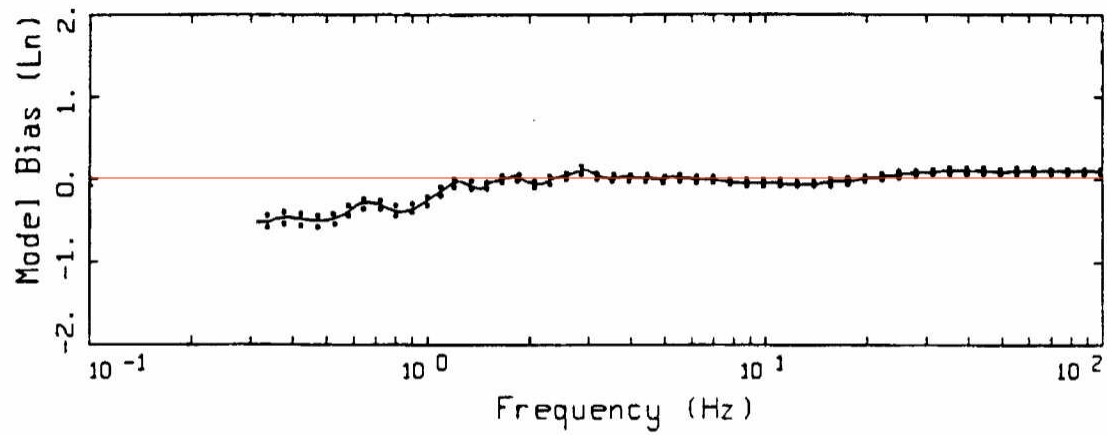
SAGUENAY, POINT SOURCE MODELING, PAGE 1 OF 2.
 LINEAR.

LEGEND
 — DATA
 - - - MODEL

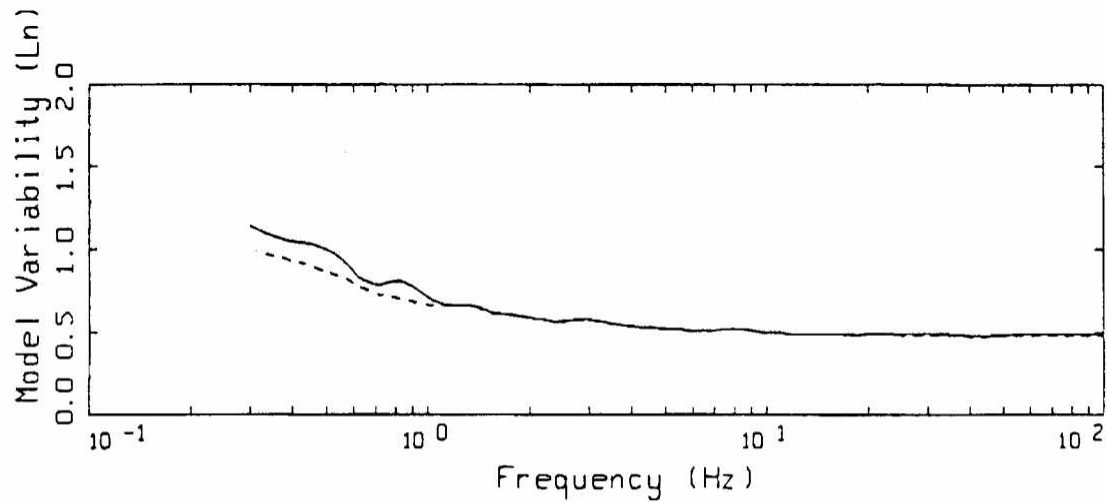


SAGUENAY, POINT SOURCE MODELING, PAGE 2 OF 2.
 LINEAR.

— DATA
 - - - MODEL



LEGEND
 ——— MODELING BIAS
 90% CONFIDENCE INTERVAL OF MODELING BIAS
 90% CONFIDENCE INTERVAL OF MODELING BIAS



LEGEND
 ——— MEAN=0.0
 - - - - BIAS CORRECTED

16 EARTHQUAKES POINT-SOURCE
 NONLINEAR. ALL 503 SITES

Additional Earthquakes for Model Validation/Variability Update

Earthquake	Mag	Earthquake	Mag
1994 Northridge AS1	6.05	1999 Chi-Chi AS2	6.20
1994 Northridge AS2	5.20	1999 Chi-Chi AS3	6.20
1994 Northridge AS3	5.93	1999 Chi-Chi AS4	6.20
1994 Northridge AS4	5.13	1999 Chi-Chi AS5	6.30
1994 Northridge AS5	5.28	1999 Koaceli (Turkey)	7.51
1995 Kobe (Japan)	6.90	1999 Duzce (Turkey)	7.14
1999 Hector Mine	7.13	2000 Tottori (Japan)	7.3
1999 Chi-Chi MS	7.62	2002 Denali	7.9
1999 Chi-Chi AS1	5.90	2003 Bam (Iran)	6.6
		2004 Niigata (Japan)	6.8

Model Parameters

- Point Source Stress Drop ($\Delta\sigma$)
- Crustal Model
- Point Source Depth
- Q-model: $Q(f) = Q_0 f^\eta$
- Geometrical Attenuation
- Kappa (Site term)

Point Source Stress Drop ($\Delta\sigma$)

- Magnitude dependent Stress Drop:
 - $M_{\leq 5.5} = 160$ bars
 - $M_{6.5} = 120$ bars
 - $M_{7.5} = 90$ bars
 - $M_{8.5} = 70$ bars
- Constant Stress Drop: 120 bars
- High, Medium, Low Stress Drop Models
- Variability: $\sigma_{ln} = 0.5$

Point Source Stress Drop ($\Delta\sigma$)

Earthquakes	Stress Drop (Bars)	σ_{In}
All	46.9	0.47
Shallow Slip	30.6	0.37
Deep Slip	56.6	0.38

Crustal Models

■ EPRI (1993) Mid-Continent Crustal Model

Thickness (km)	Vs (km/sec)	Density (cgs)
1.30	2.83	2.52
11.00	3.52	2.71
28.00	3.75	2.78
Half-Space	4.62	3.35

■ EPRI (1993) Gulf Coast Crustal Model

Thickness (km)	Vs (km/sec)	Density (cgs)
7.00	2.31	2.37
8.00	3.05	2.58
15.00	3.76	2.78
Half-Space	4.74	3.40

Source Depth

- Magnitude Dependent Truncated Depth Distribution

Magnitude	Lower Bound (km)	Mean Depth (km)	Upper Bound (km)
4.5	2	6	15
5.5	2	6	15
6.5	4	8	20
7.5	5	10	20
8.5	5	10	20

$$\sigma_{ln} = 0.6$$

Q-Model

- Mid-Continent (Silva et al. 1997):

$$Q(f) = 351f^{0.84}$$

- Gulf Coast (EPRI 1993):

$$Q(f) = 300 f^{0.30}$$

- $\sigma_{\ln Q_0} = 0.4$

Geometrical Attenuation and Kappa

- Magnitude Dependent Far Field Attenuation:

$$R^{-(a+b(M-6.5))} \quad \text{where } a=1.0296, b=-0.0422$$

$$R^{-(a+b(M-6.5))/2} \quad \text{for } R > 80 \text{ km}$$

- Kappa = 0.006 sec (EPRI, 1993)

DataSet

- 5 magnitudes: 4.5, 5.5, 6.5, 7.5, 8.5
- 9 Distances: 1, 5, 10, 20, 50, 75, 100, 200, 400
- 300 Realizations for each magnitude and distance pair
- Randomly Vary source depth, Stress Drop, Q_0 , and top 100 feet of profile
- Total of 13,500 response spectra

Alternative Source Models

- Single Corner Model
 - Constant Stress Drop (120 bars)
 - Variable Stress Drop (Magnitude Dependent)
- Double Corner Model
(Atkinson and Boore, 1995)

Saturation of Ground Motions

- Reduction in the scaling of ground motions as a function of magnitude
- Fictitious Depth term:
$$H = H'^* \exp(-1.250 + 0.227M)$$
for $M > 6.5$
- Applied to Double Corner and Single Corner with Constant Stress Drop Models

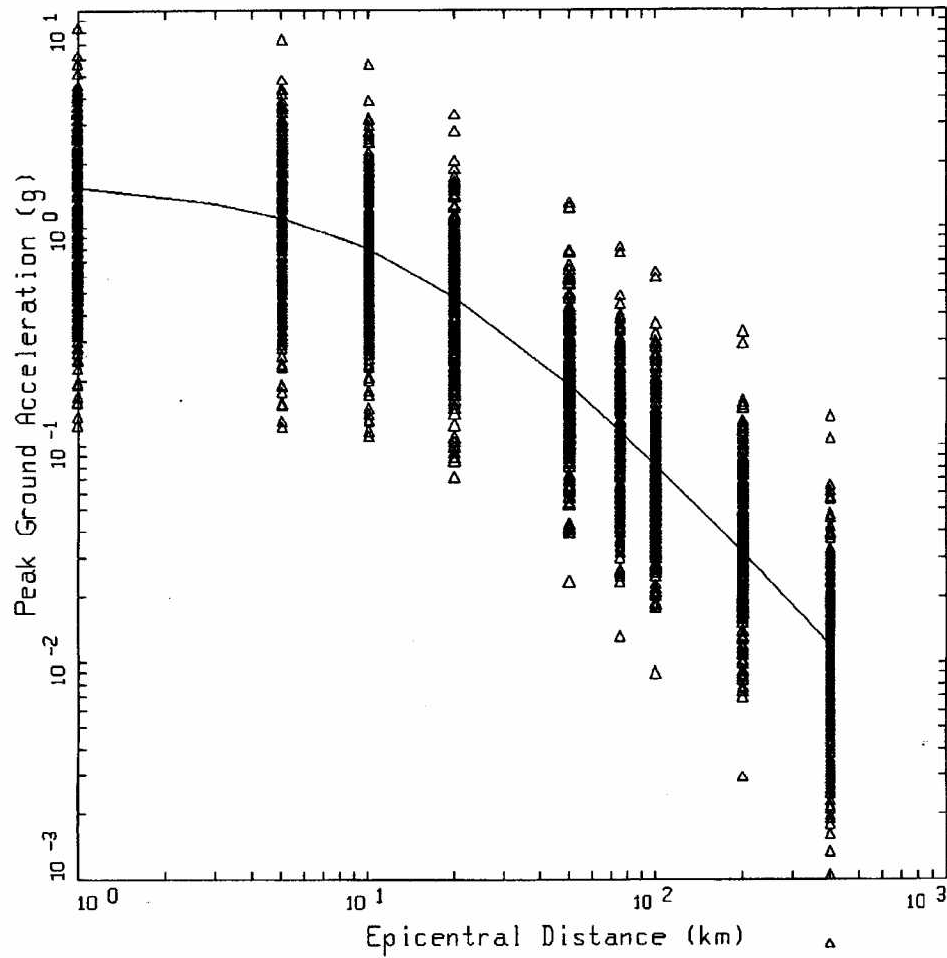
Summary of Ground Motion Models

- Single Corner Constant Stress Drop
(Low, Medium, High)
- Single Corner Constant Stress Drop with Saturation (Low, Medium, High)
- Single Corner Variable Stress Drop
(Low, Medium, High)
- Double Corner
- Double Corner with Saturation

Total CEUS Models = 22

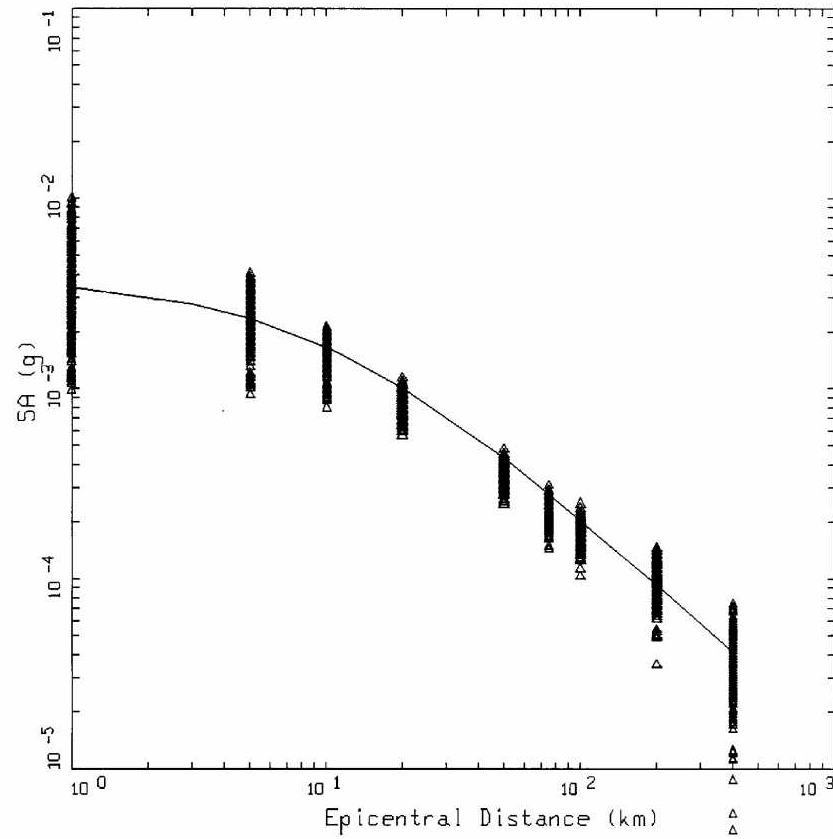
Attenuation Model

$$\begin{aligned} \ln(S_a) = & C_1 + C_2 * M + \\ & (C_6 + C_7 * M) * \ln(R + \exp(C_4)) \\ & + C_{10} * (M - 6)^2 \end{aligned}$$



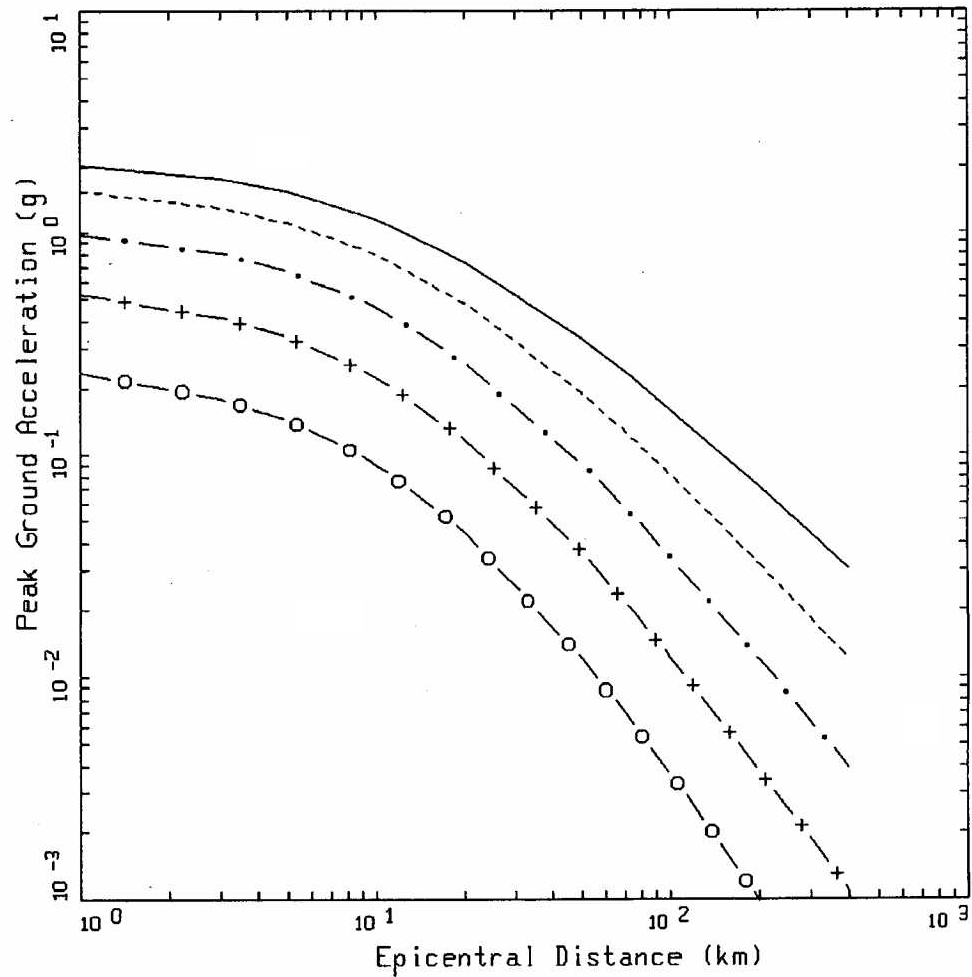
1 CORNER VARIABLE STRESS DROP
 M=7.5, CEUS HARD ROCK, PGA

Δ Δ LEGEND
 — DATA: PGA
 M=7.5, SIGMA=0.6912



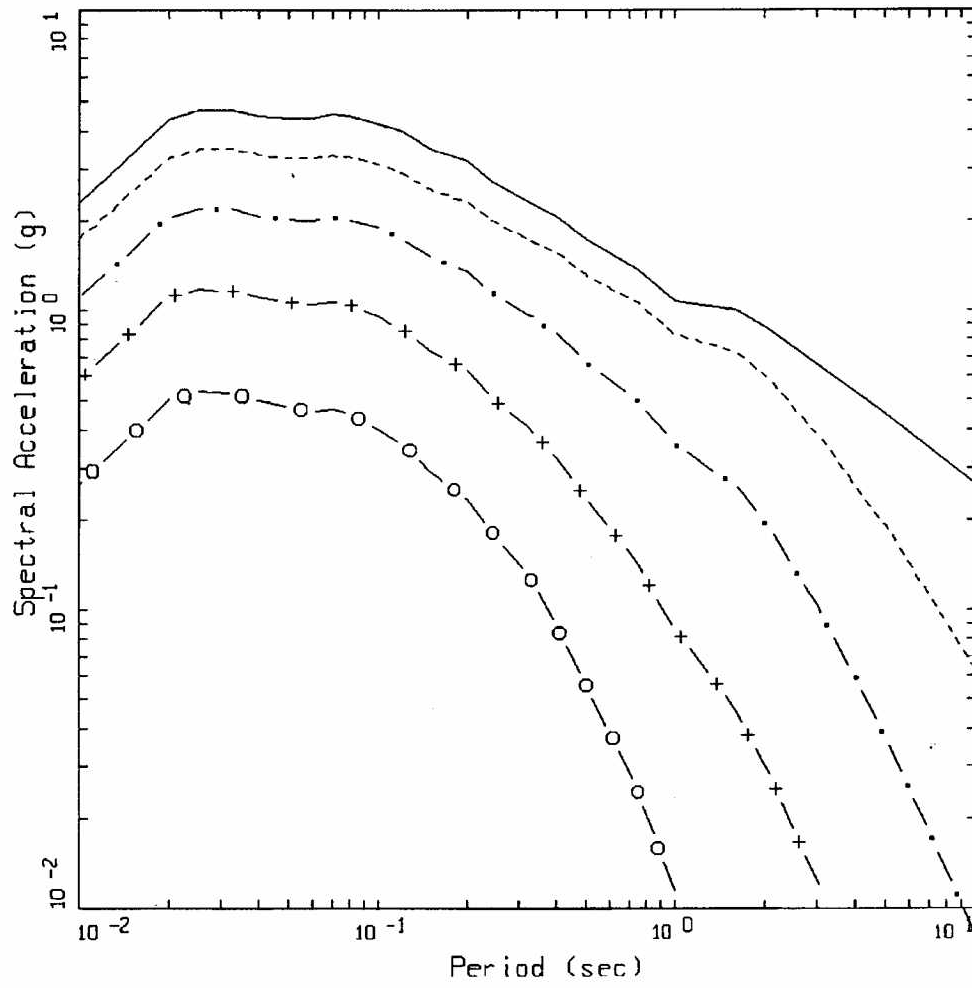
1 CORNER VARIABLE STRESS DROP
 M=5.5, CEUS HARD ROCK, 0.2HZ

Δ Δ
 ———
 LEGEND
 DATA: 0.20 HZ
 M=5.5, SIGMA=0.3660



1 CORNER VARIABLE STRESS DROP
HARD ROCK, PGA

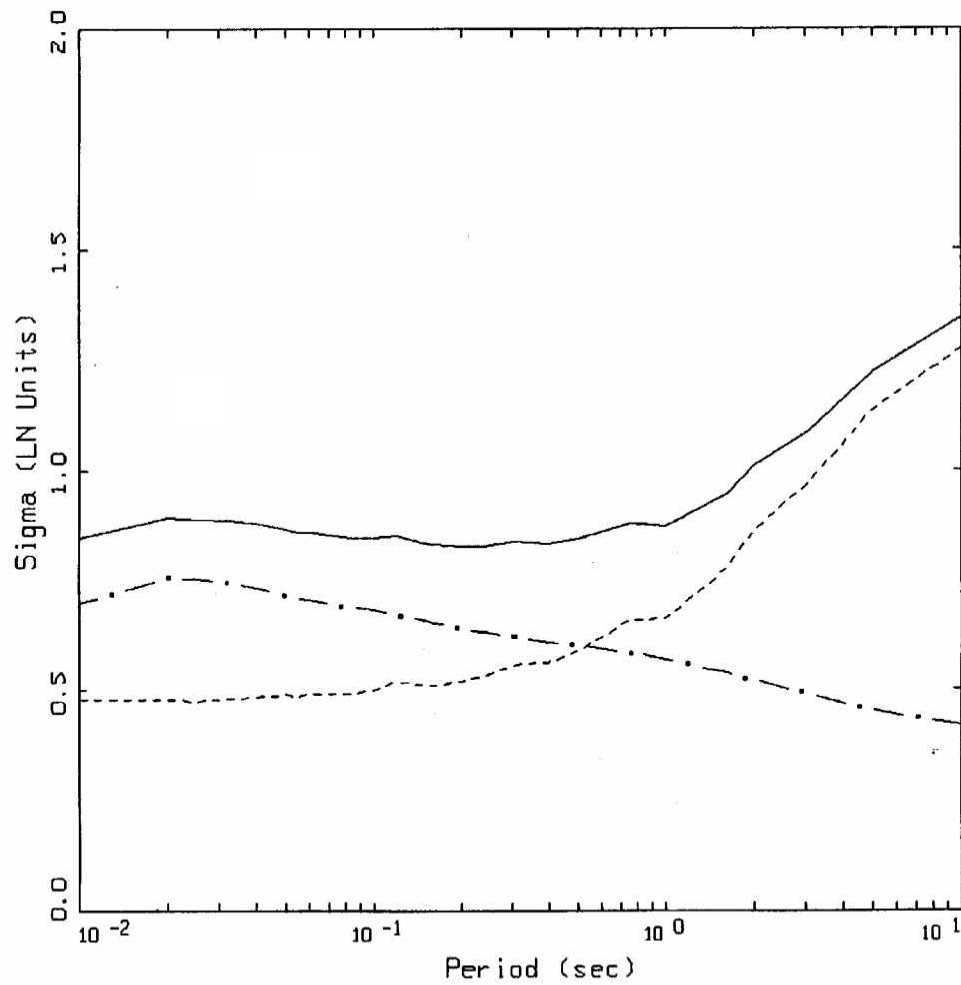
LEGEND	
—	M=8.5, SIGMA=0.6912
- - -	M=7.5, SIGMA=0.6912
- · -	M=6.5, SIGMA=0.6912
- + -	M=5.5, SIGMA=0.6912
- o -	M=4.5, SIGMA=0.6912



1 CORNER VARIABLE STRESS DROP
 DISTANCE=1 KM, HARD ROCK, SA

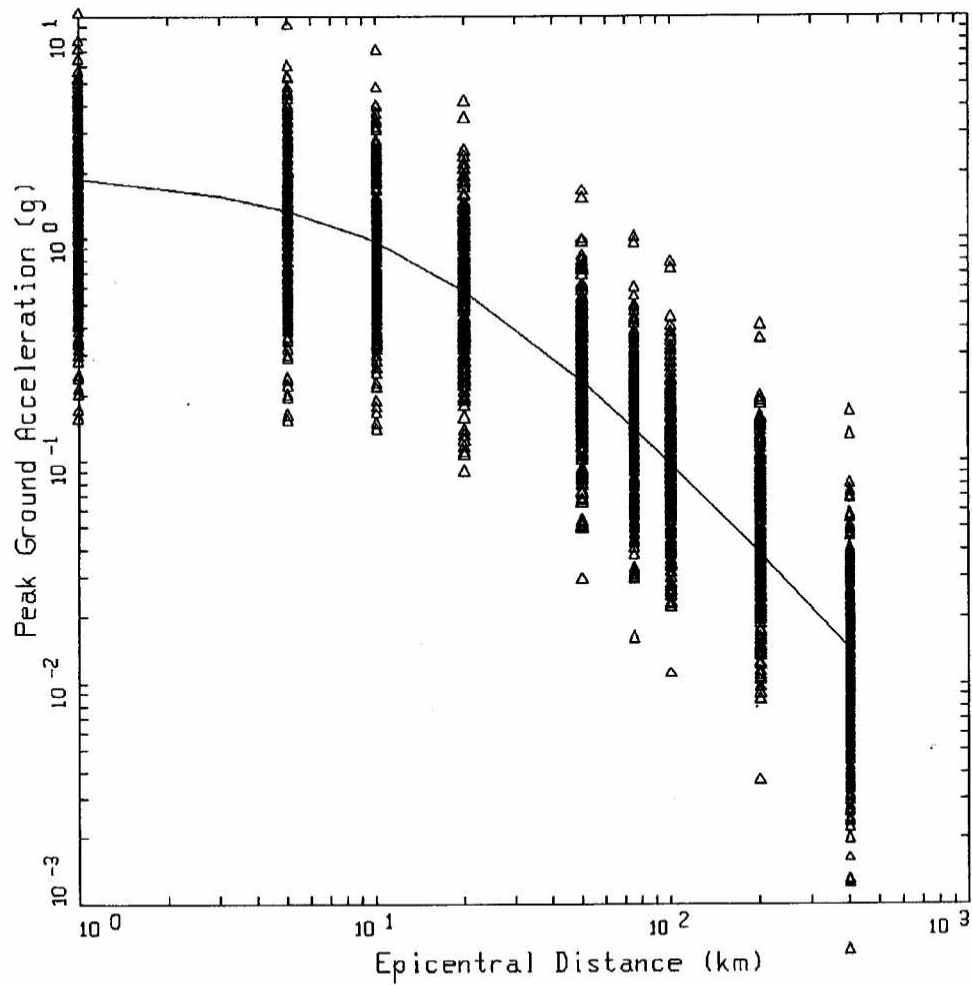
LEGEND

- M=8.5
- - - M=7.5
- · - M=6.5
- + - M=5.5
- o - M=4.5



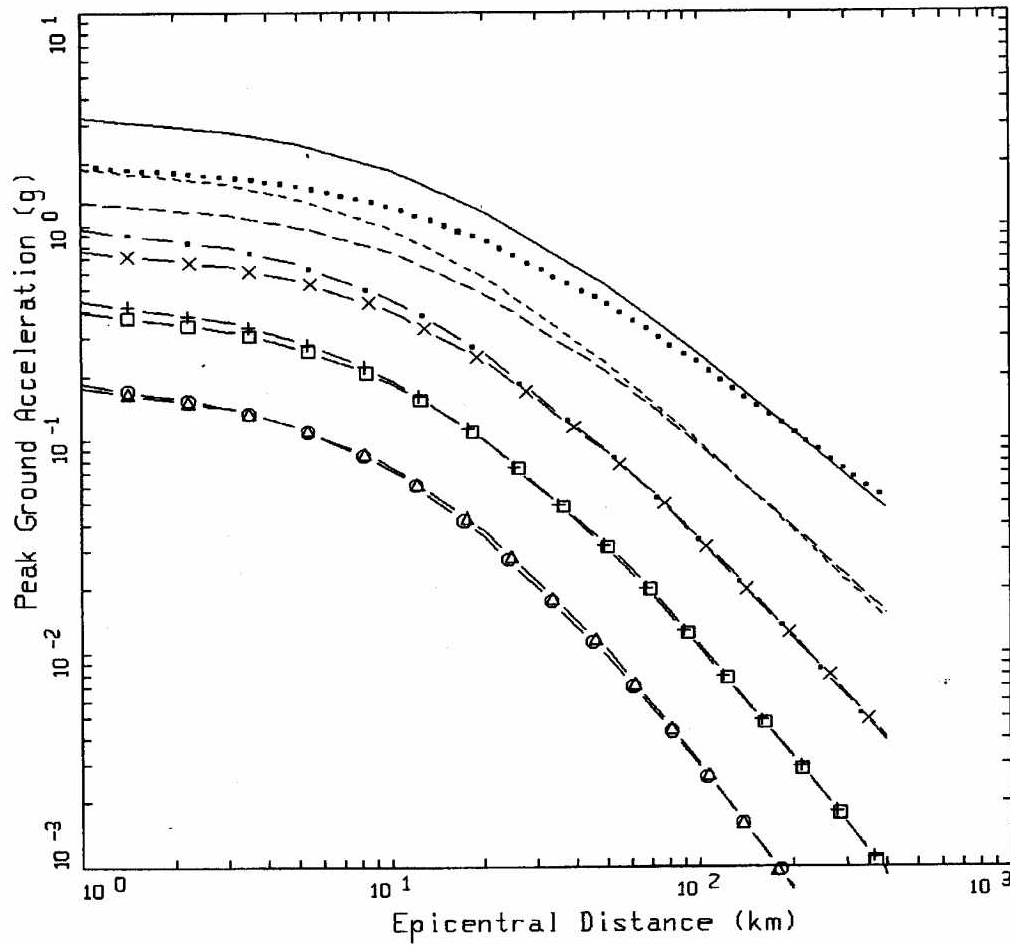
1 CORNER VARIABLE STRESS DROP
HARD ROCK, SIGMA

LEGEND
 ——— TOTAL SIGMA
 - · - PARAMETRIC SIGMA
 - - - MODELING SIGMA (BIAS CORRECTED)



1 CORNER CONSTANT STRESS DROP
 M=7.5, CEUS HARD ROCK, PGA

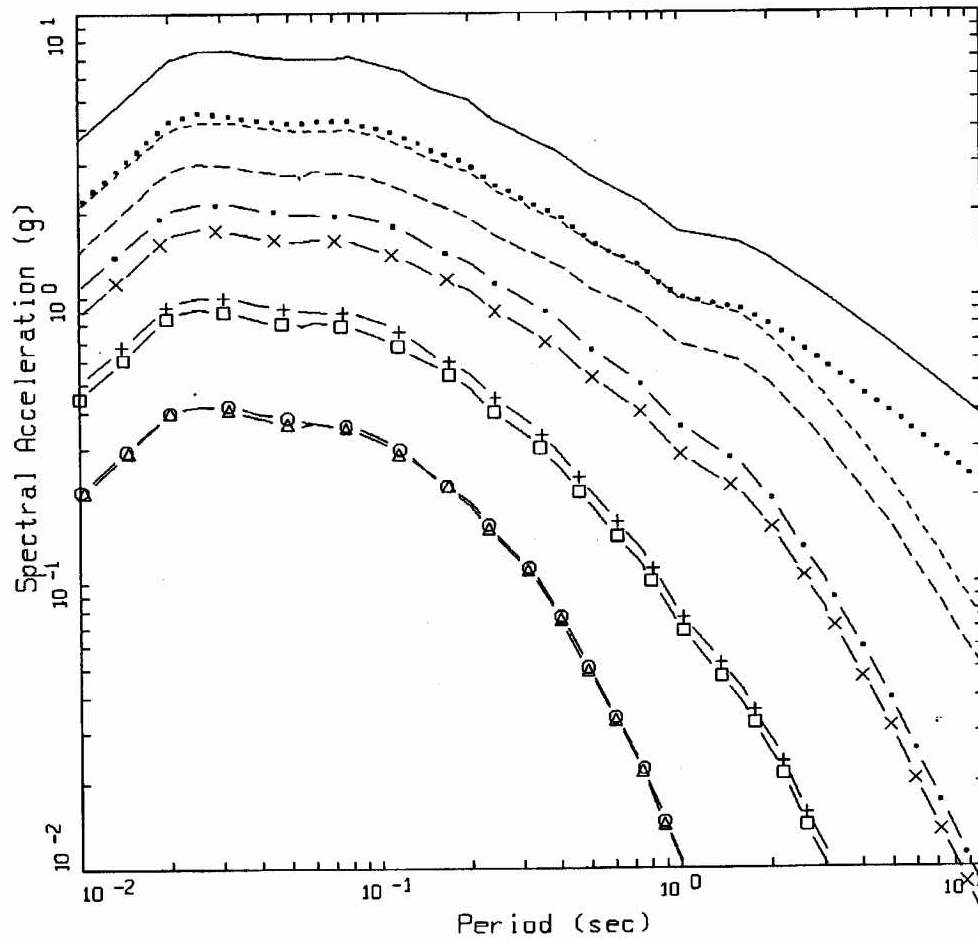
Δ Δ LEGEND
 — DATA: PGA
 M=7.5, SIGMA=0.6886



1 CORNER CONSTANT STRESS DROP
HARD ROCK, PGA

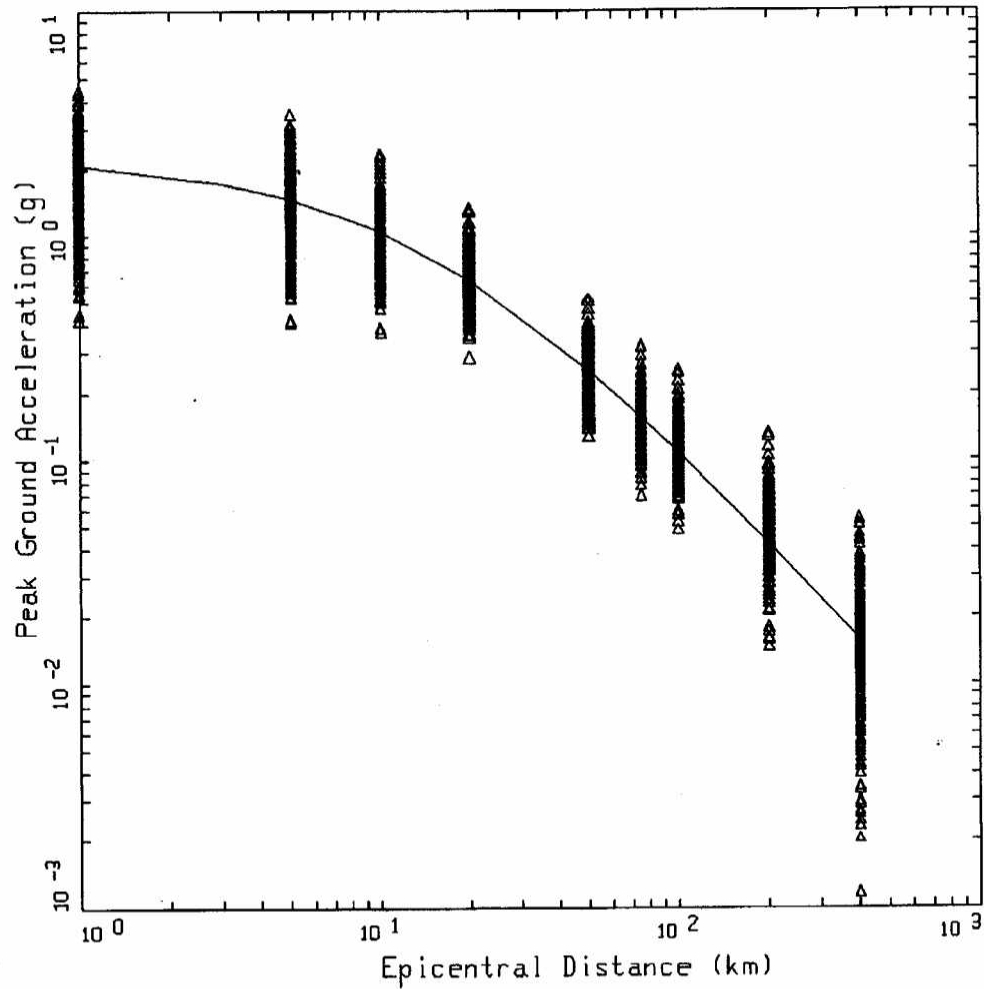
LEGEND

—	M=8.5, SIGMA=0.6886
- - -	M=7.5, SIGMA=0.6886
- · -	M=6.5, SIGMA=0.6886
- + -	M=5.5, SIGMA=0.6886
- O -	M=4.5, SIGMA=0.6886
· · · ·	M=8.5 WITH SATURATION, SIGMA=0.6998
- - -	M=7.5 WITH SATURATION, SIGMA=0.6998
- X -	M=6.5 WITH SATURATION, SIGMA=0.6998
- □ -	M=5.5 WITH SATURATION, SIGMA=0.6998
- Δ -	M=4.5 WITH SATURATION, SIGMA=0.6998



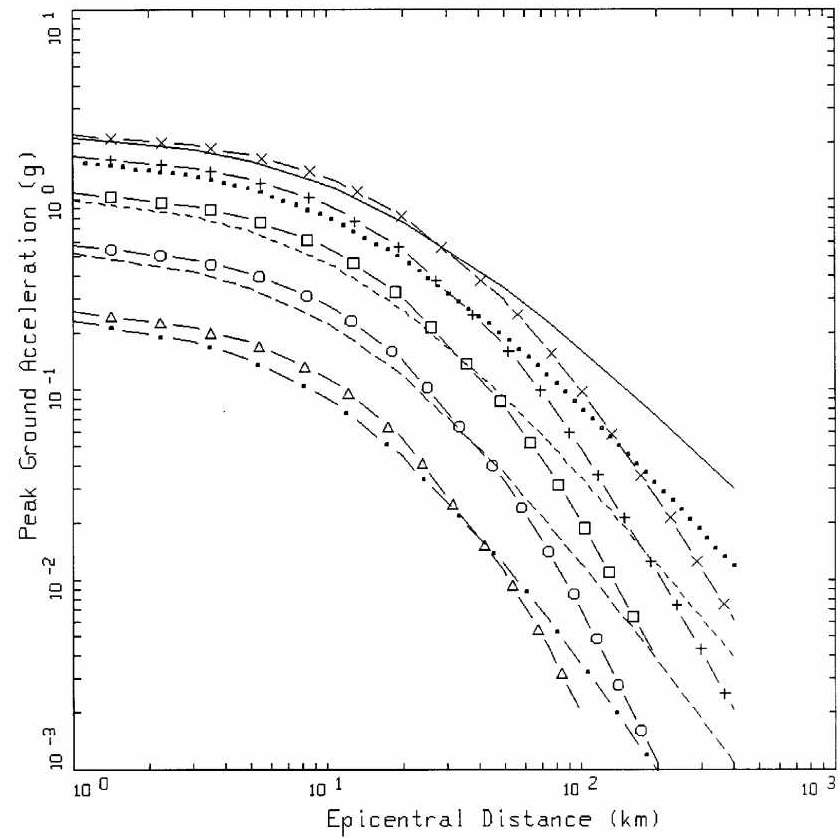
1 CORNER CONSTANT STRESS DROP
 DISTANCE=1 KM, HARD ROCK, SA

LEGEND	
—	M=8.5
- - -	M=7.5
- · -	M=6.5
- + -	M=5.5
- ○ -	M=4.5
· · ·	M=8.5 WITH SATURATION
- - -	M=7.5 WITH SATURATION
- x -	M=6.5 WITH SATURATION
- □ -	M=5.5 WITH SATURATION
- △ -	M=4.5 WITH SATURATION



2 CORNER
 M=7.5, CEUS HARD ROCK, PGA

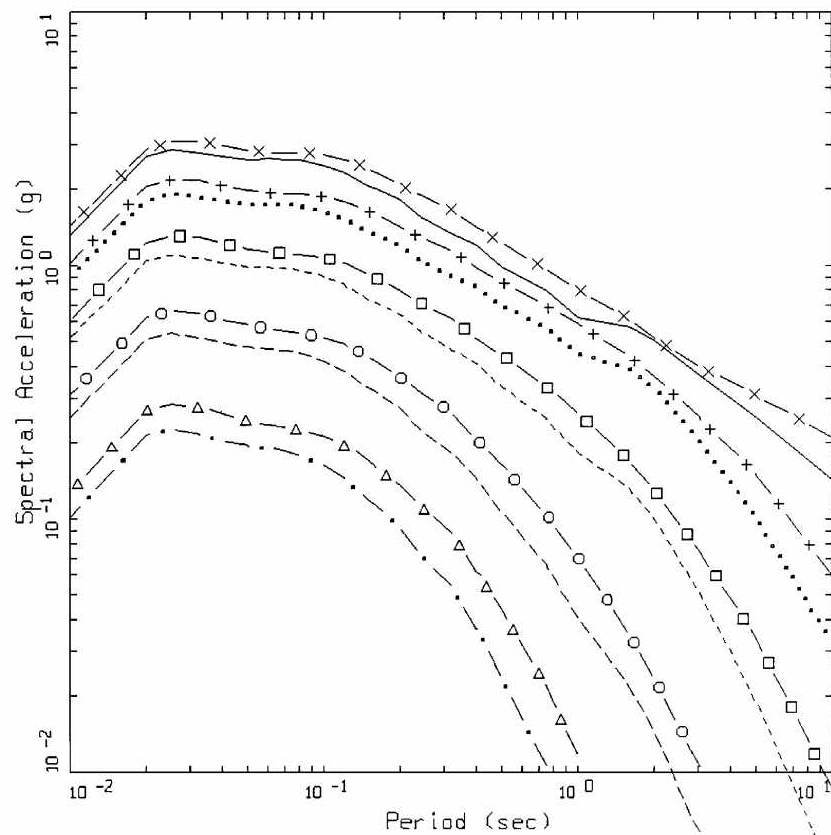
Δ Δ
 ———
 LEGEND
 DATA: PGA
 M=7.5, SIGMA=0.6912



1 CORNER VAR. STRESS DROP (M)
MIDCONTINENT AND GULF, PGA

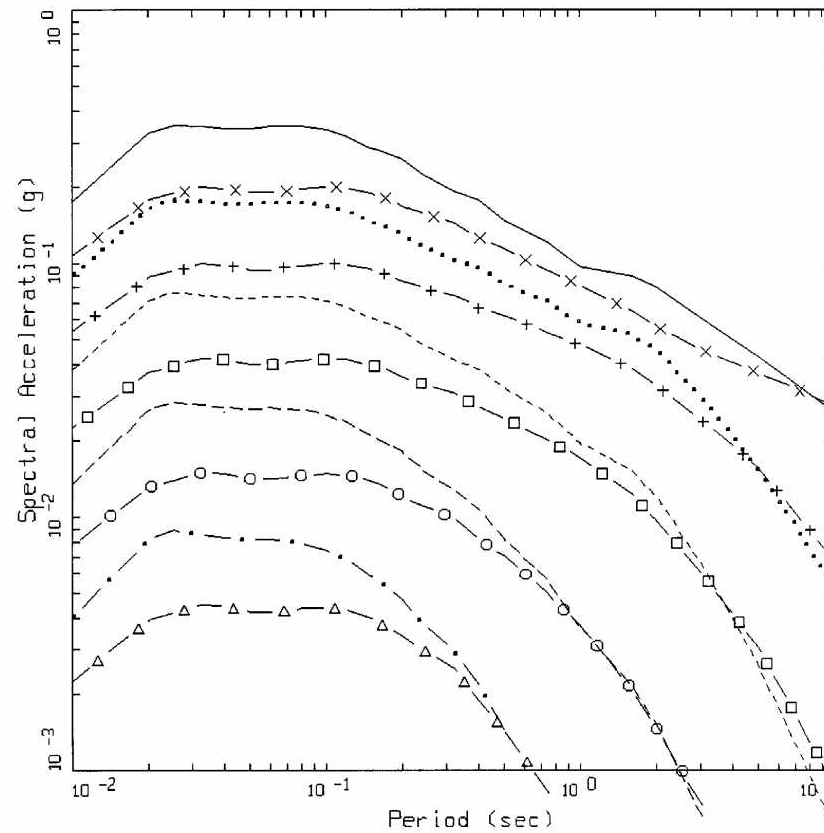
LEGEND

- MIDCONTINENT: M=8.5, SIGMA=0.5592
- MIDCONTINENT: M=7.5, SIGMA=0.5592
- MIDCONTINENT: M=6.5, SIGMA=0.5592
- MIDCONTINENT: M=5.5, SIGMA=0.5592
- · - MIDCONTINENT: M=4.5, SIGMA=0.5592
- x - GULF COAST: M=8.5, SIGMA=0.7666
- + - GULF COAST: M=7.5, SIGMA=0.7666
- □ - GULF COAST: M=6.5, SIGMA=0.7666
- ○ - GULF COAST: M=5.5, SIGMA=0.7666
- △ - GULF COAST: M=4.5, SIGMA=0.7666



1 CORNER VAR. STRESS DROP (M)
 DISTANCE=10KM, MIDCONT. & GULF, SA

LEGEND	
—	MIDCONTINENT: M=8.5
.....	MIDCONTINENT: M=7.5
- - - -	MIDCONTINENT: M=6.5
- - - -	MIDCONTINENT: M=5.5
- . -	MIDCONTINENT: M=4.5
- x -	GULF COAST: M=8.5
- + -	GULF COAST: M=7.5
- □ -	GULF COAST: M=6.5
- ○ -	GULF COAST: M=5.5
- △ -	GULF COAST: M=4.5

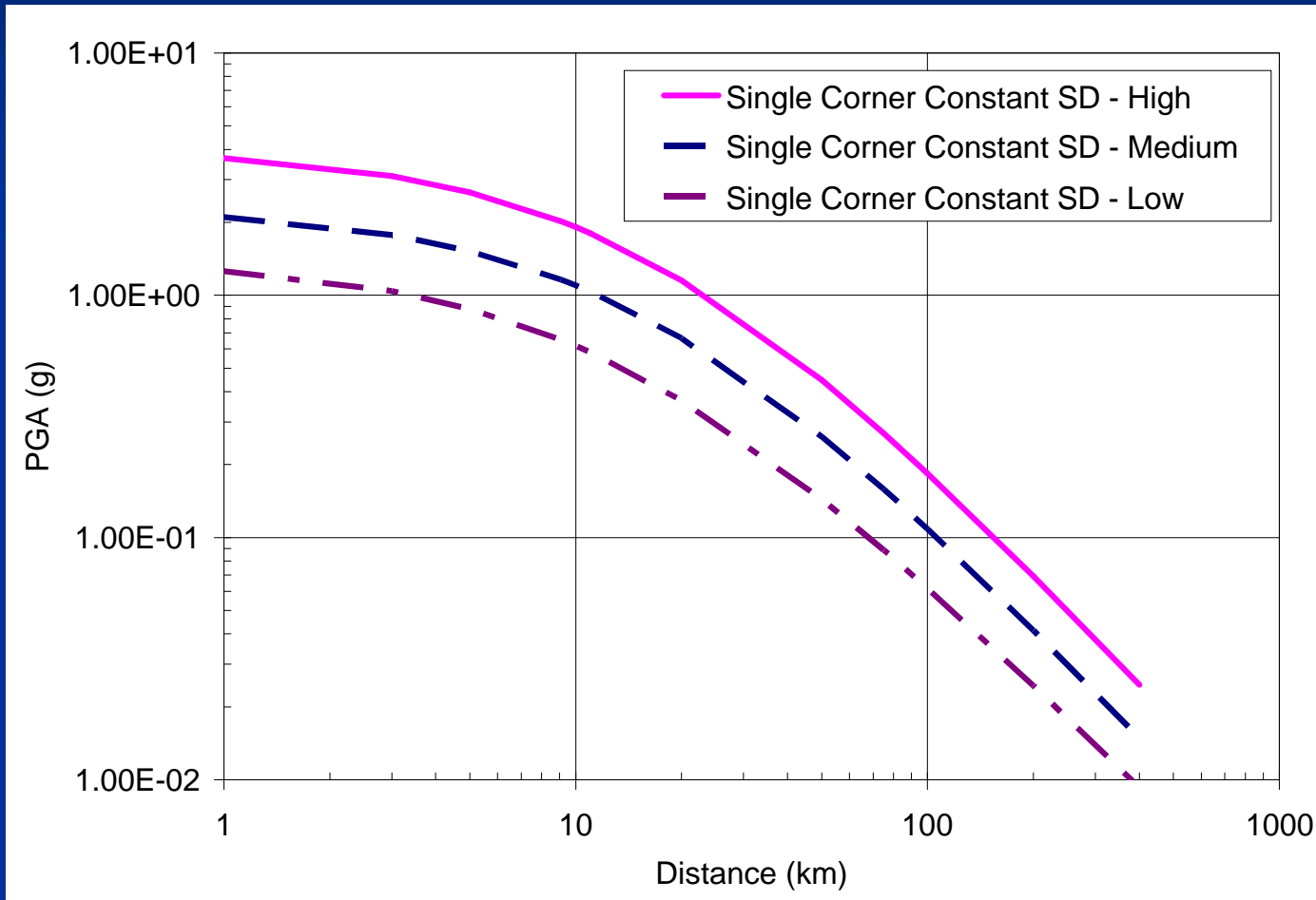


1 CORNER VAR. STRESS DROP (M)
 DISTANCE = 100KM, MIDCON. & GULF, SA

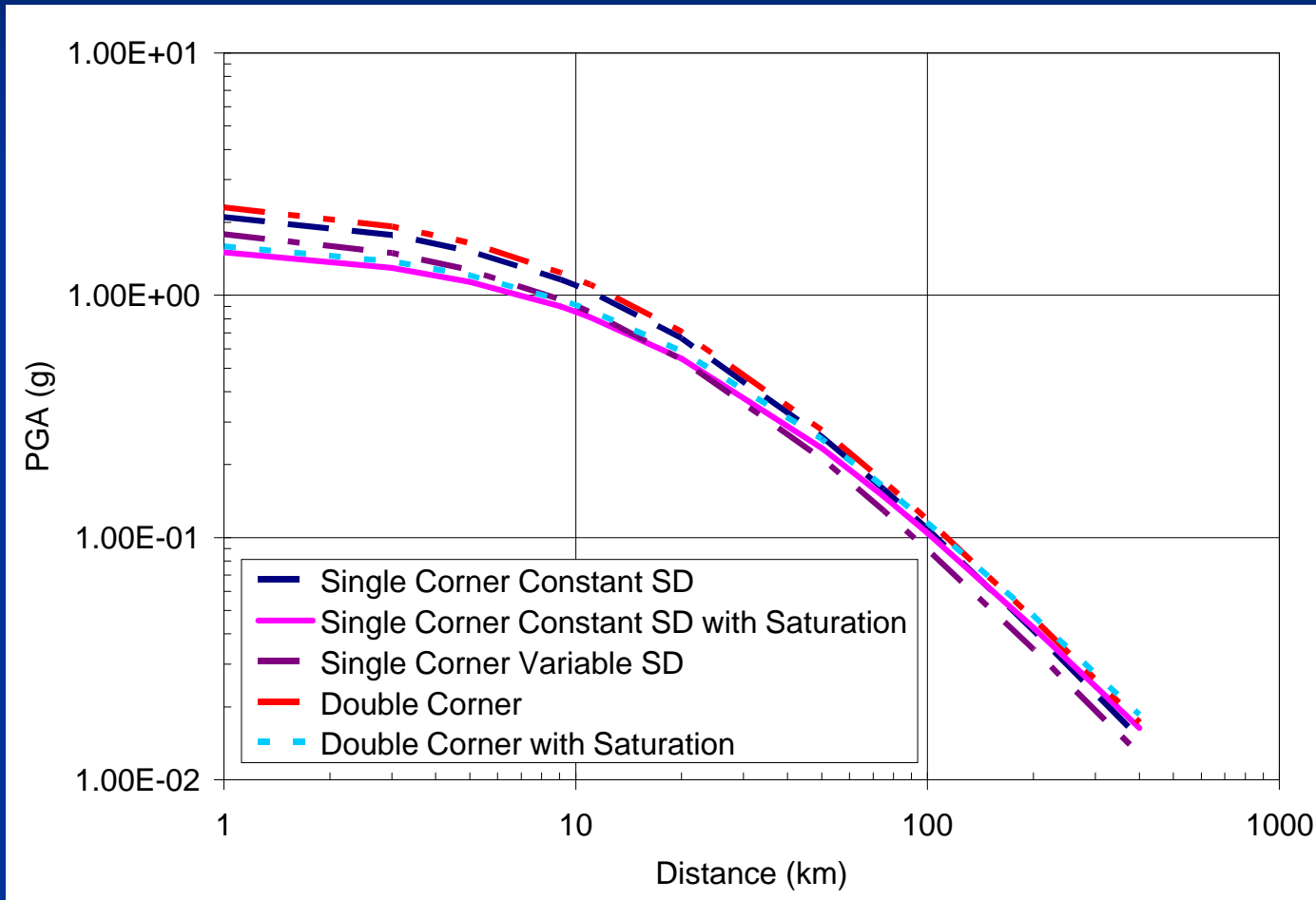
LEGEND

- MIDCONTINENT: M=8.5
- MIDCONTINENT: M=7.5
- MIDCONTINENT: M=6.5
- MIDCONTINENT: M=5.5
- · - MIDCONTINENT: M=4.5
- × - GULF COAST: M=8.5
- + - GULF COAST: M=7.5
- □ - GULF COAST: M=6.5
- ○ - GULF COAST: M=5.5
- △ - GULF COAST: M=4.5

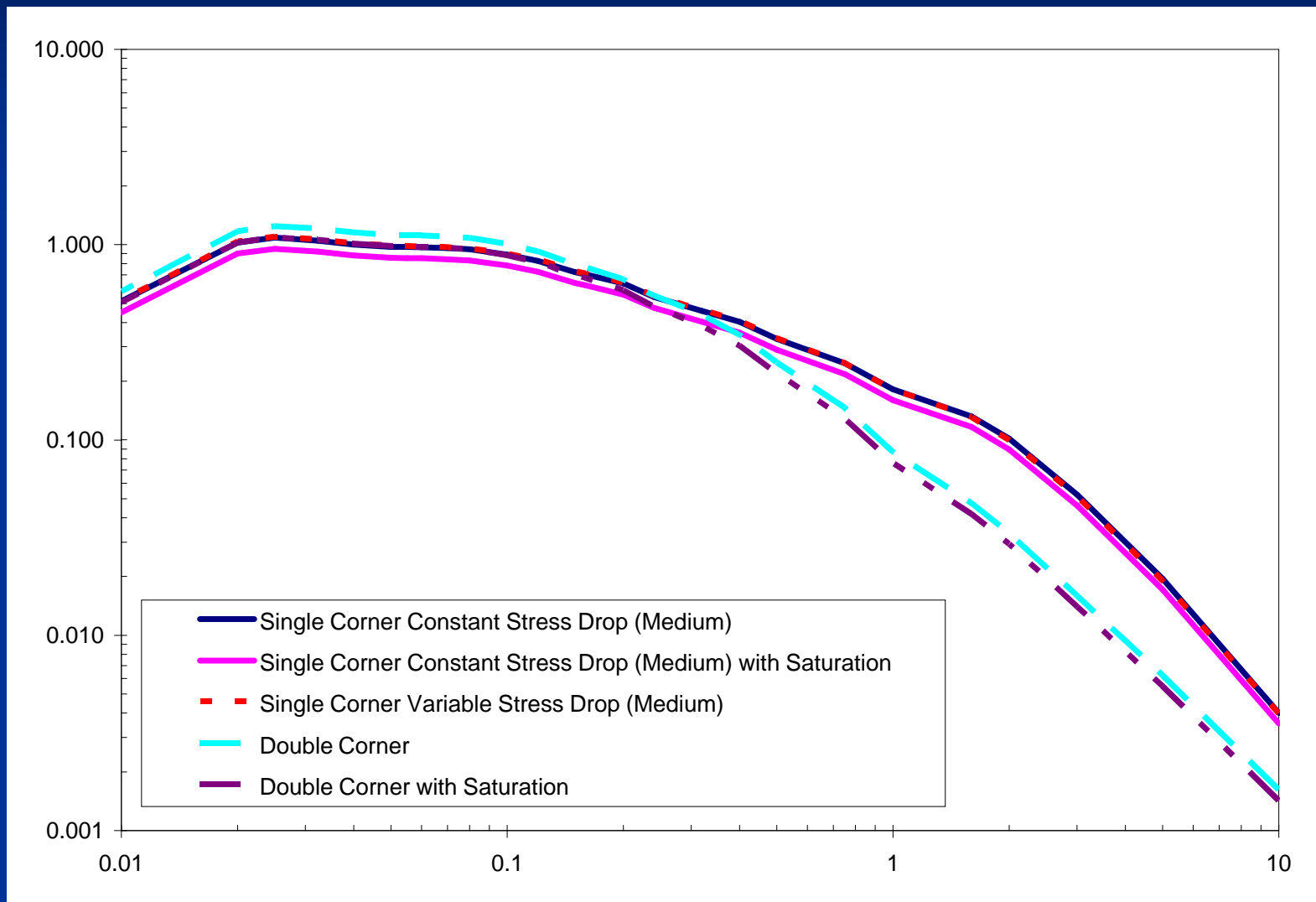
PGA - M7.5



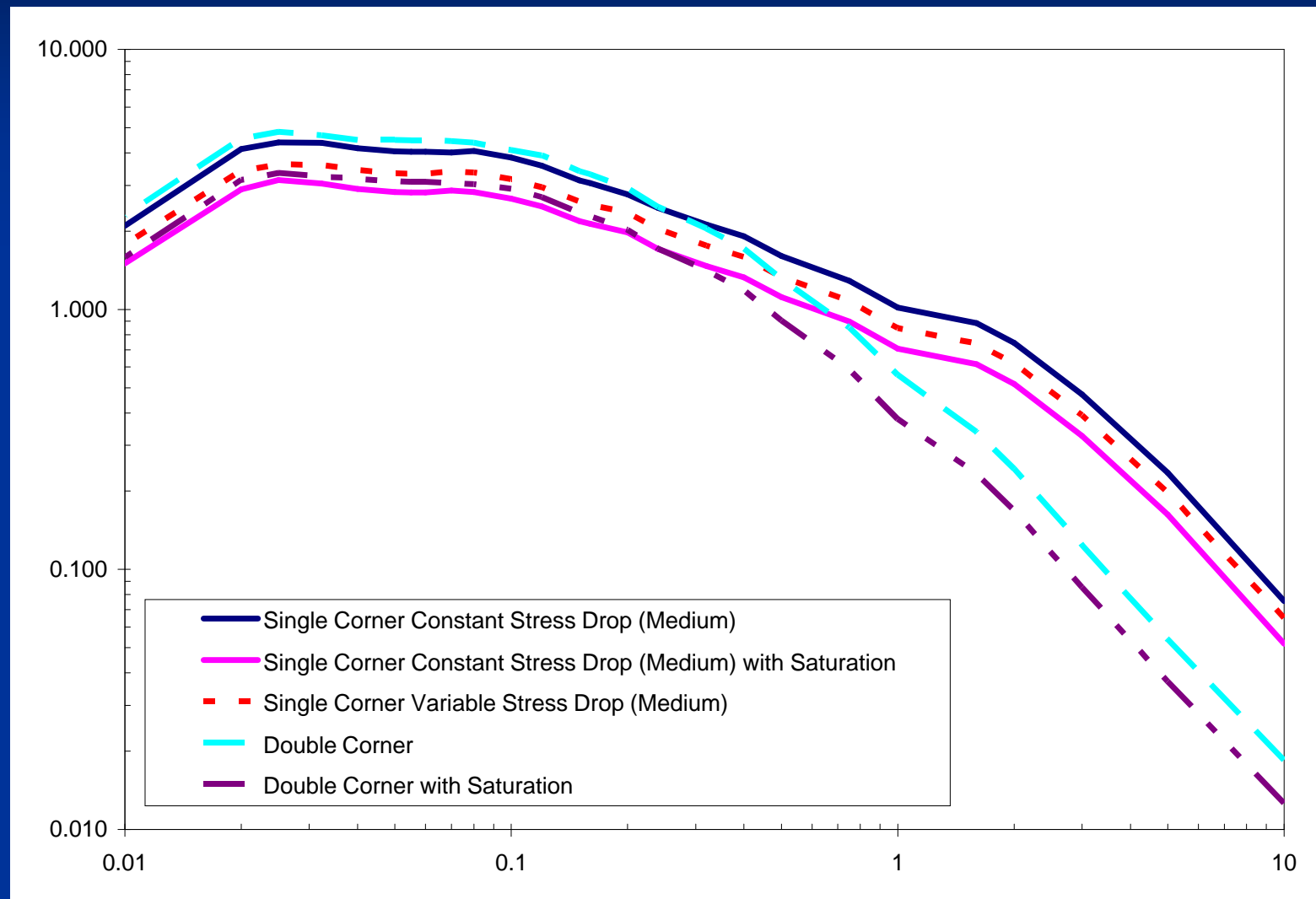
PGA – M7.5



M6.5, Distance = 10 km

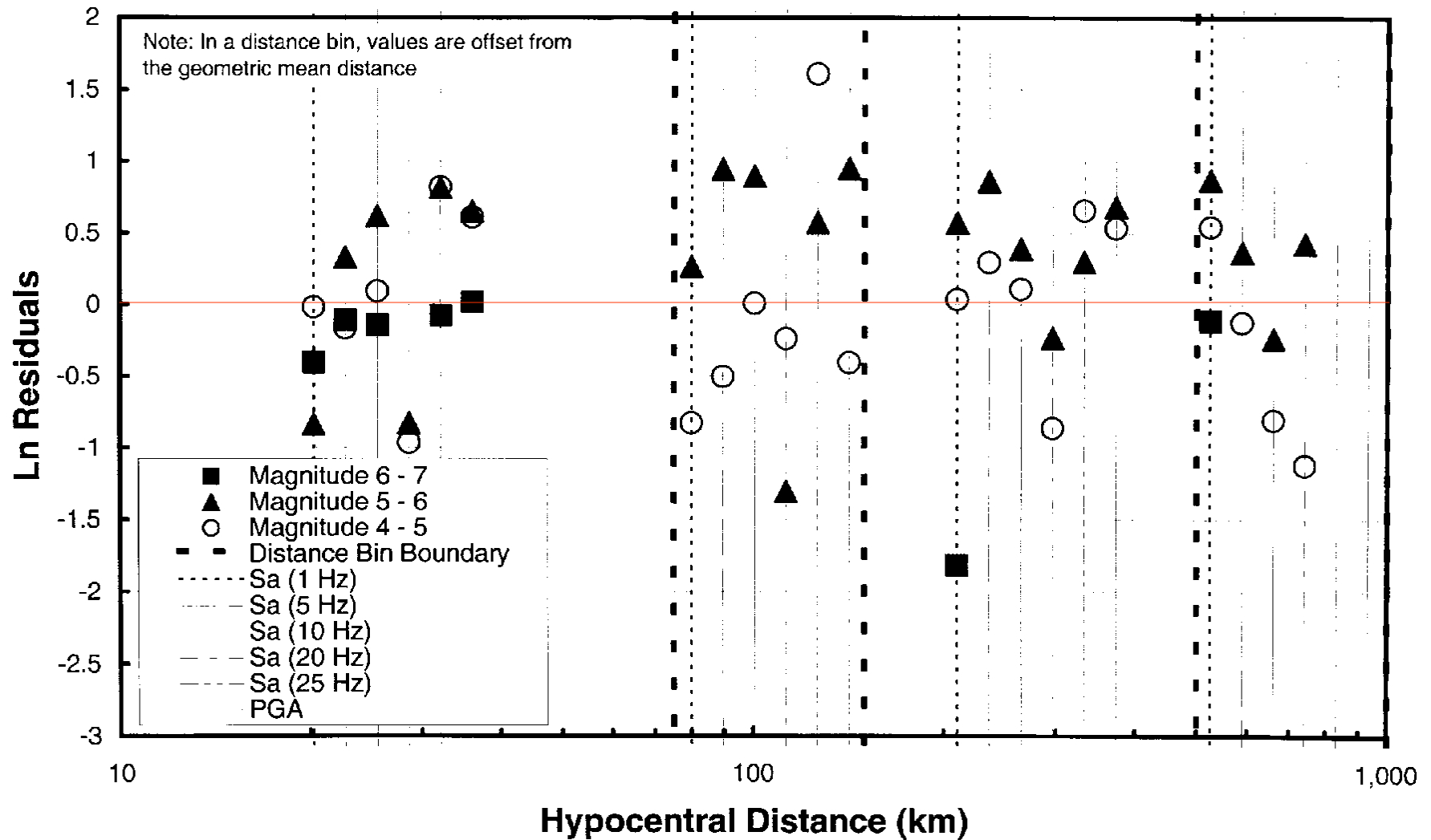


M7.5, Distance = 1 km



CEUS Residuals: Single Corner Variable Stress Drop

Silva et al. (2002) scvsvd Summary of Model/Residual Statistics



Ground Motion Model Updates

- Modeling Validation/Variability
- Point Source Stress Drop
- Geometrical Attenuation (NGA Empirical models)
- Saturation (NGA Empirical models)

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