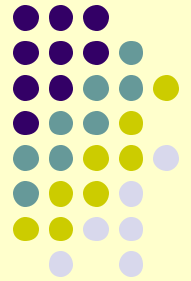




Ground Motions in the Central United States

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Dept. Earth Sciences
Carleton University

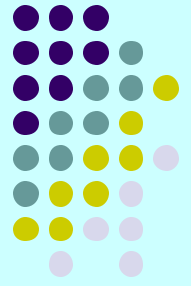




Ground motion relations

- Knowledge of ground motions is expressed as relations giving parameters such as peak ground acceleration (PGA) and response spectra as functions of magnitude and distance
- Ground motion relations are a key input to seismic hazard analysis
- Uncertainty in ground motion relations is typically the largest source of uncertainty in estimation of seismic hazard

What is known about ground motions in the CUS (Midcontinent)



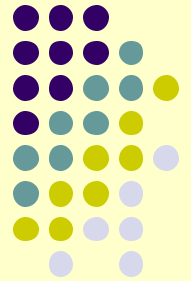
- Ground motion models (alternative relations)
- Ground motion data
- Issues in earthquake source
- Issues in earthquake path
- Overview of uncertainties in ground motion relations

CUS (Midcontinent) Ground Motion Relations: Models



- Studies (EPRI, 1993) have shown that attenuation should be similar throughout the Midcontinent region (Central U.S., eastern U.S., southeastern Canada) – therefore I address entire midcontinent as a whole
- There are insufficient ground-motion data in the magnitude-distance range of engineering interest to directly obtain ground-motion relations by regression analysis
- Thus CUS relations are developed from models, which may be validated with data to varying degrees

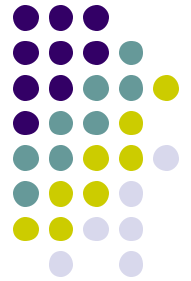
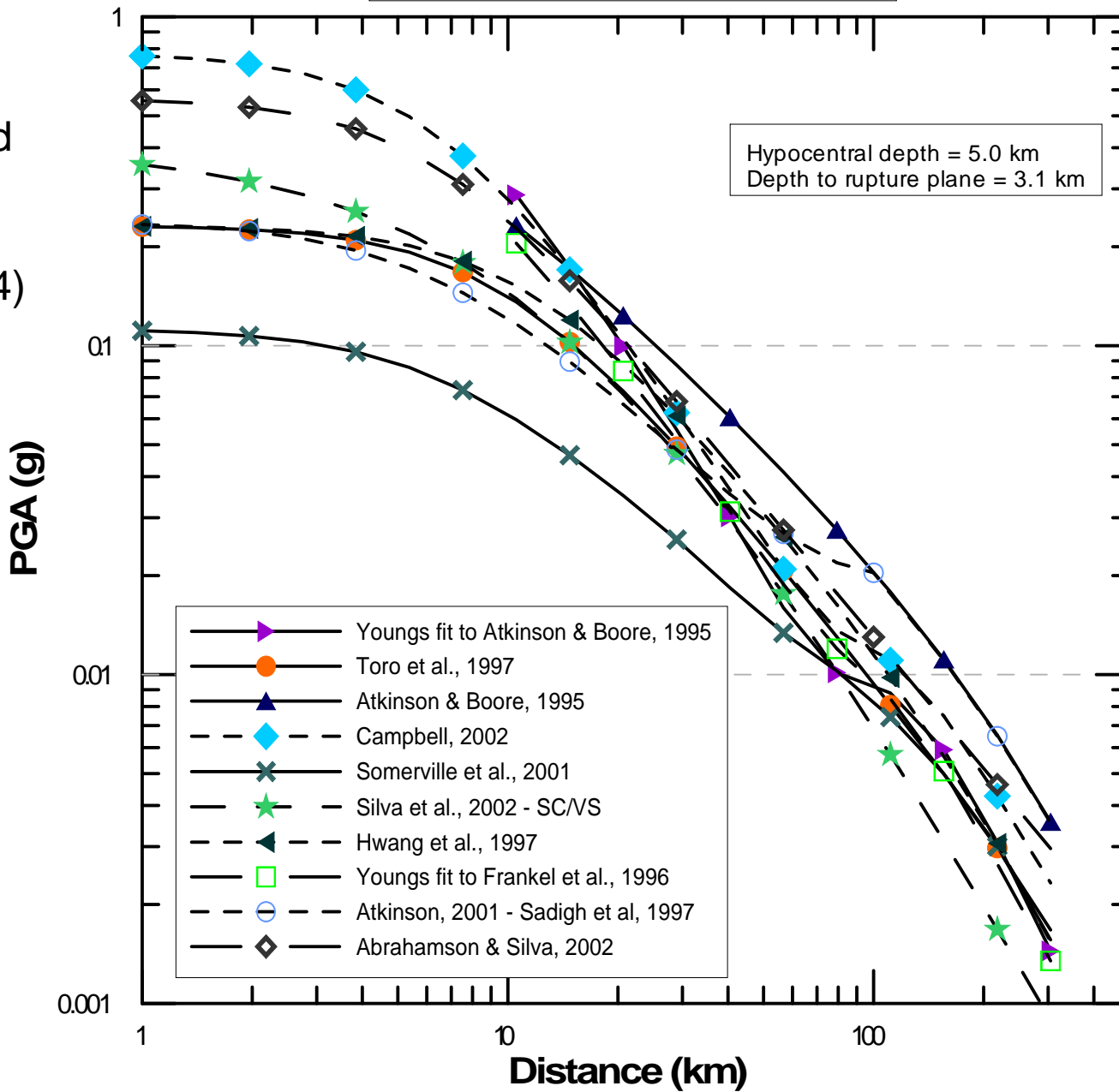
Types of models used in development of ENA ground motion relations



- Stochastic point source (single corner source)
eg. Toro et al., 1997; Frankel et al., 1996
- Stochastic point source (double corner source)
eg. Atkinson and Boore, 1995
- Hybrid empirical model (eg. Campbell, 2003)
- Finite-source/Green function numerical (eg. Somerville et al., 2001)
- Stochastic finite fault (eg. Atkinson and Boore, 2005)

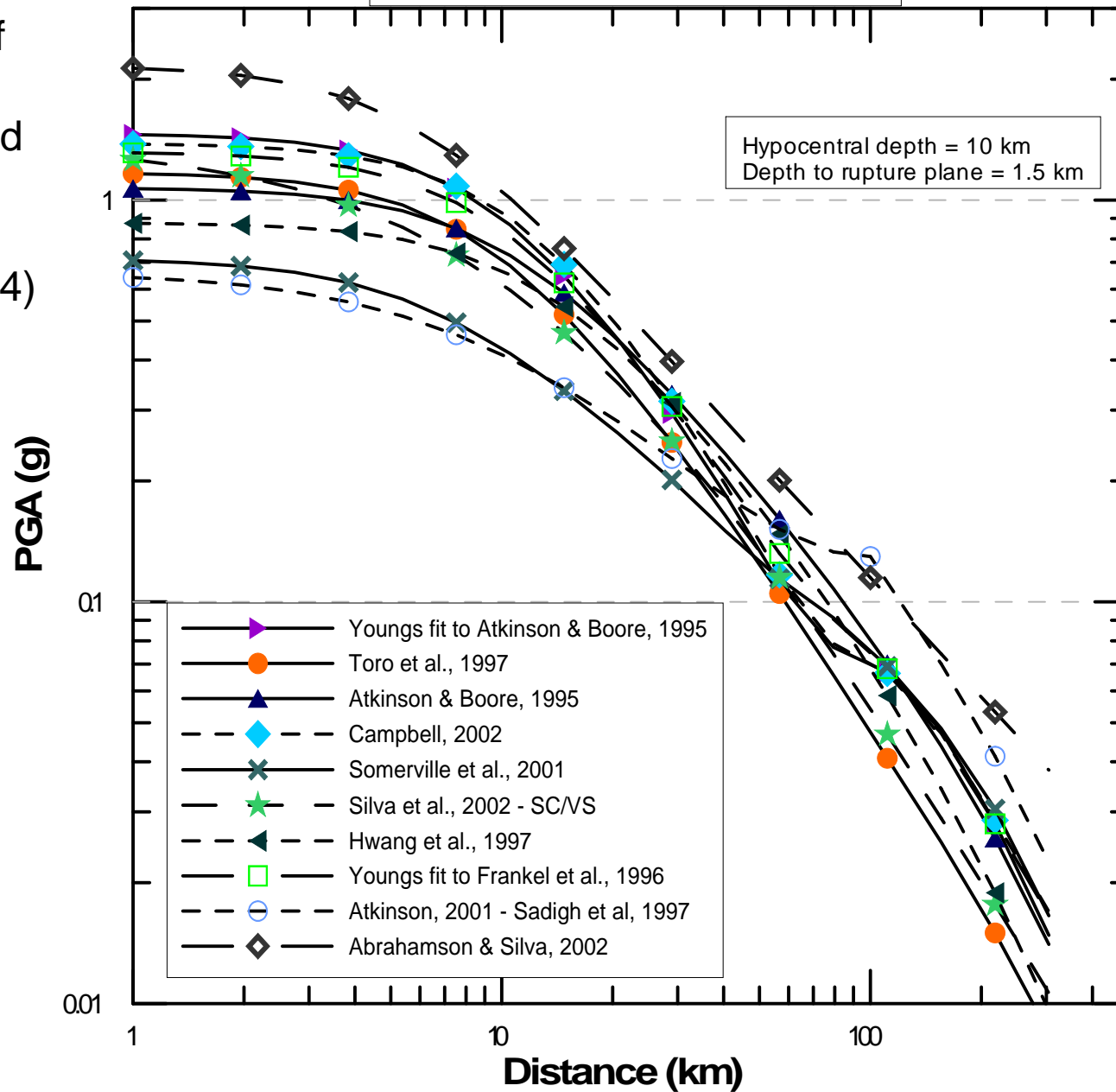
Peak Ground Acceleration M = 5.0

Example of
alternative
ENA ground
motion
relations
(EPRI, 2004)

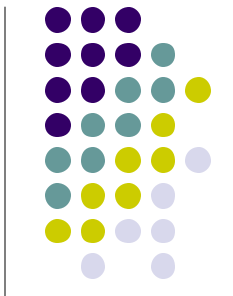


Peak Ground Acceleration M = 7.0

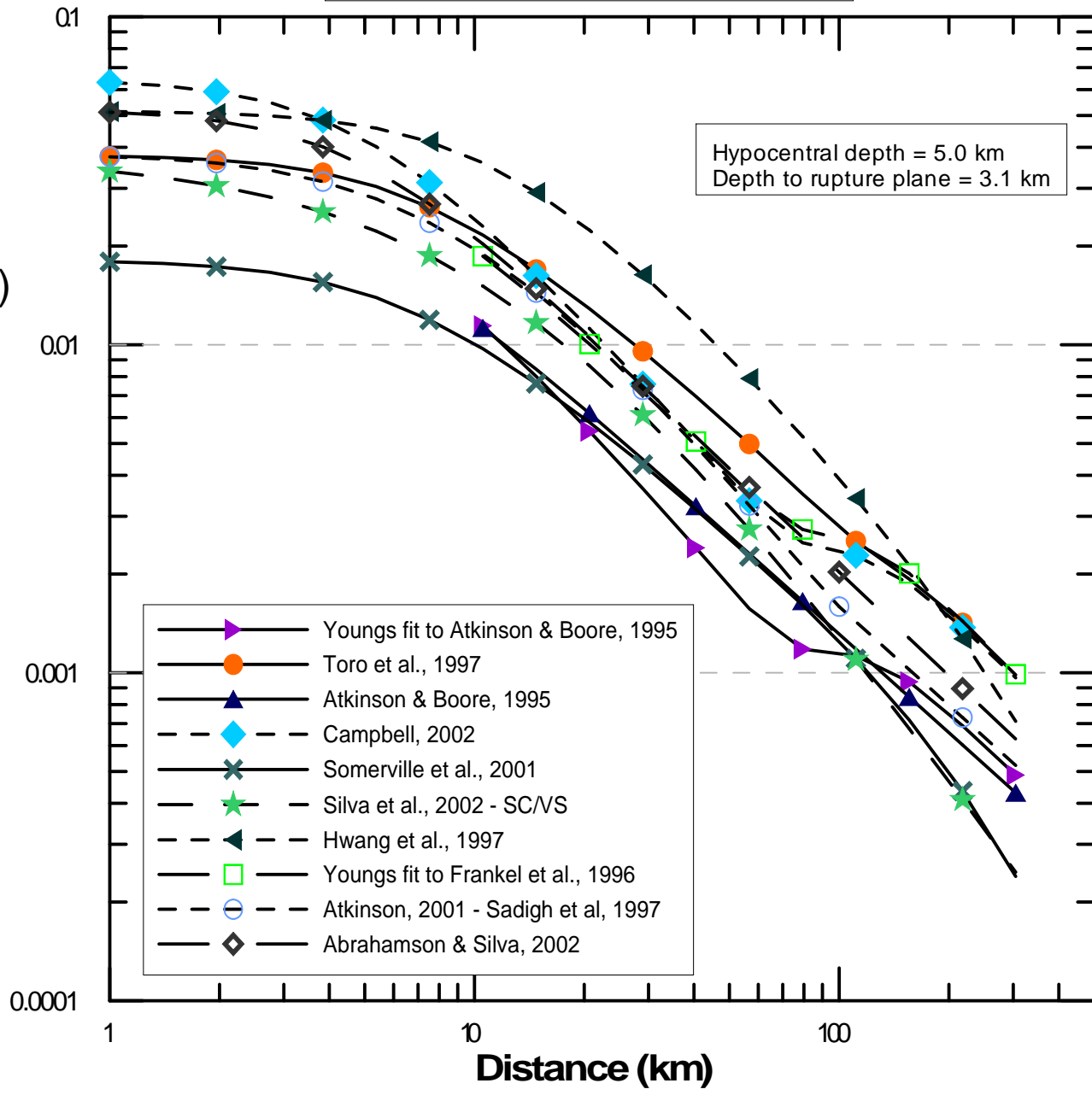
Example of
alternative
ENA ground
motion
relations
(EPRI, 2004)



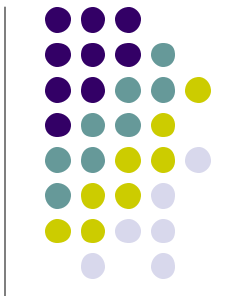
Spectral Acceleration 1 Hz M = 5.0



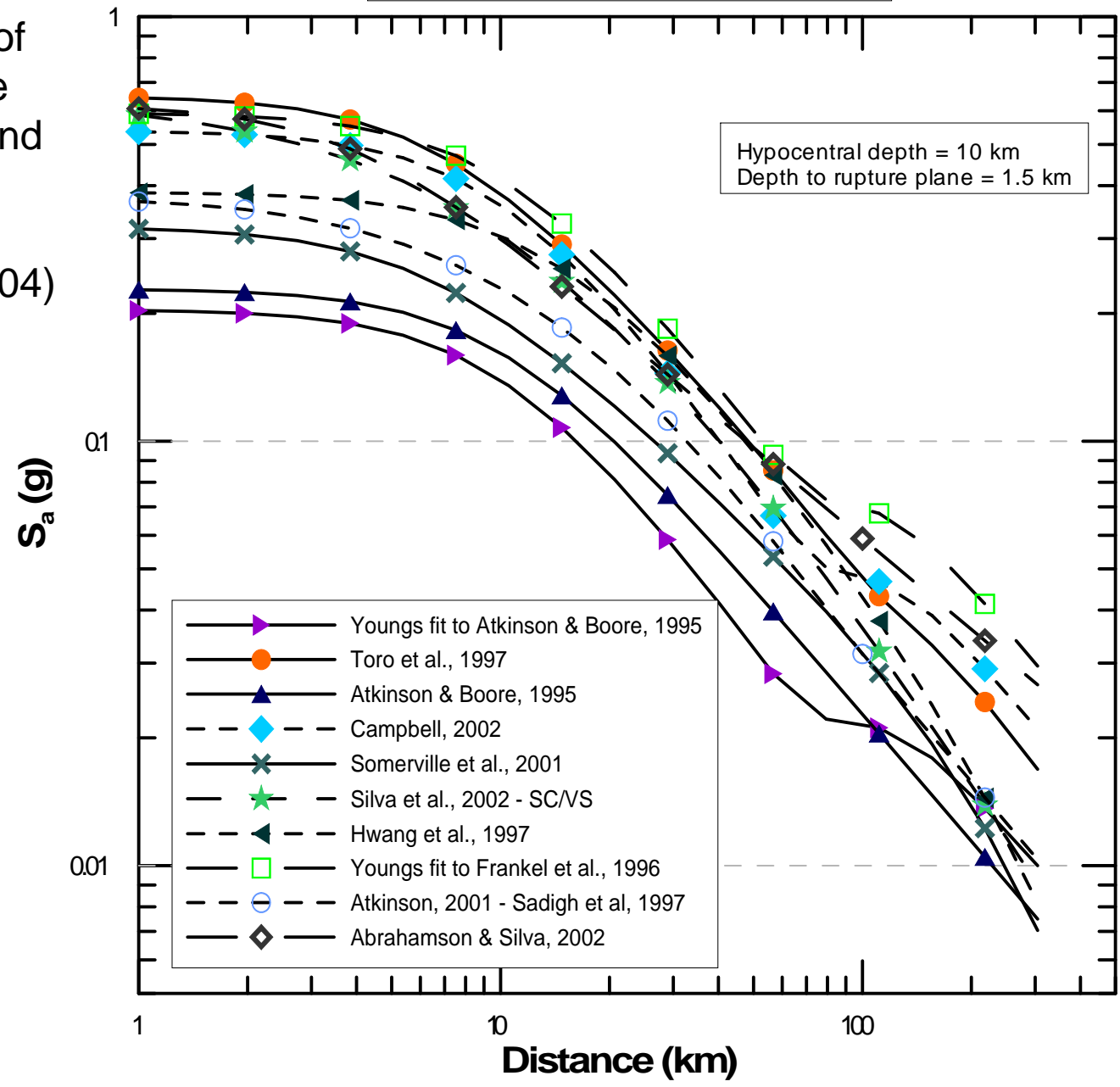
Example of
alternative
ENA ground
motion
relations
(EPRI, 2004)



Spectral Acceleration 1 Hz M = 7.0

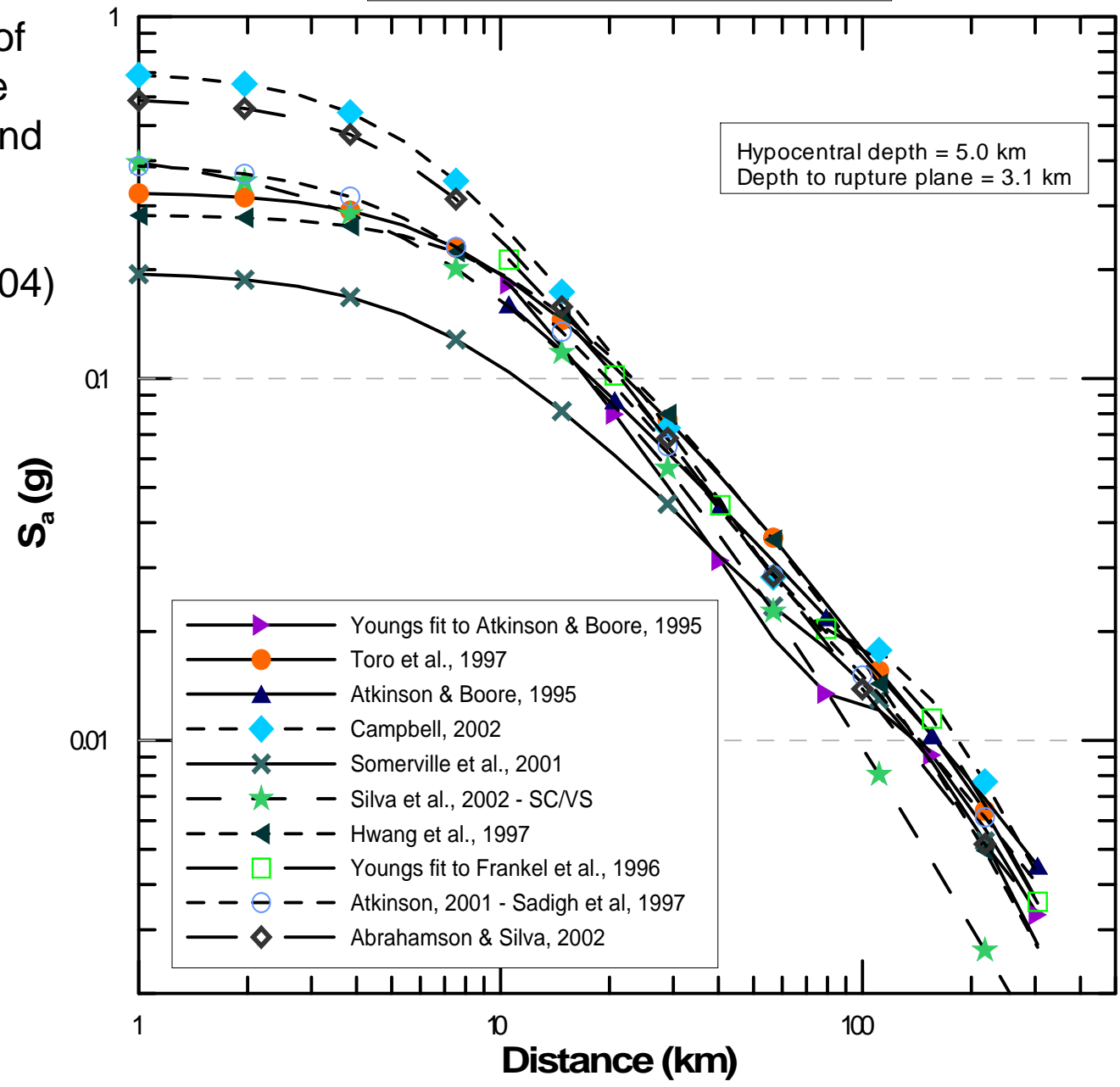


Example of
alternative
ENA ground
motion
relations
(EPRI, 2004)



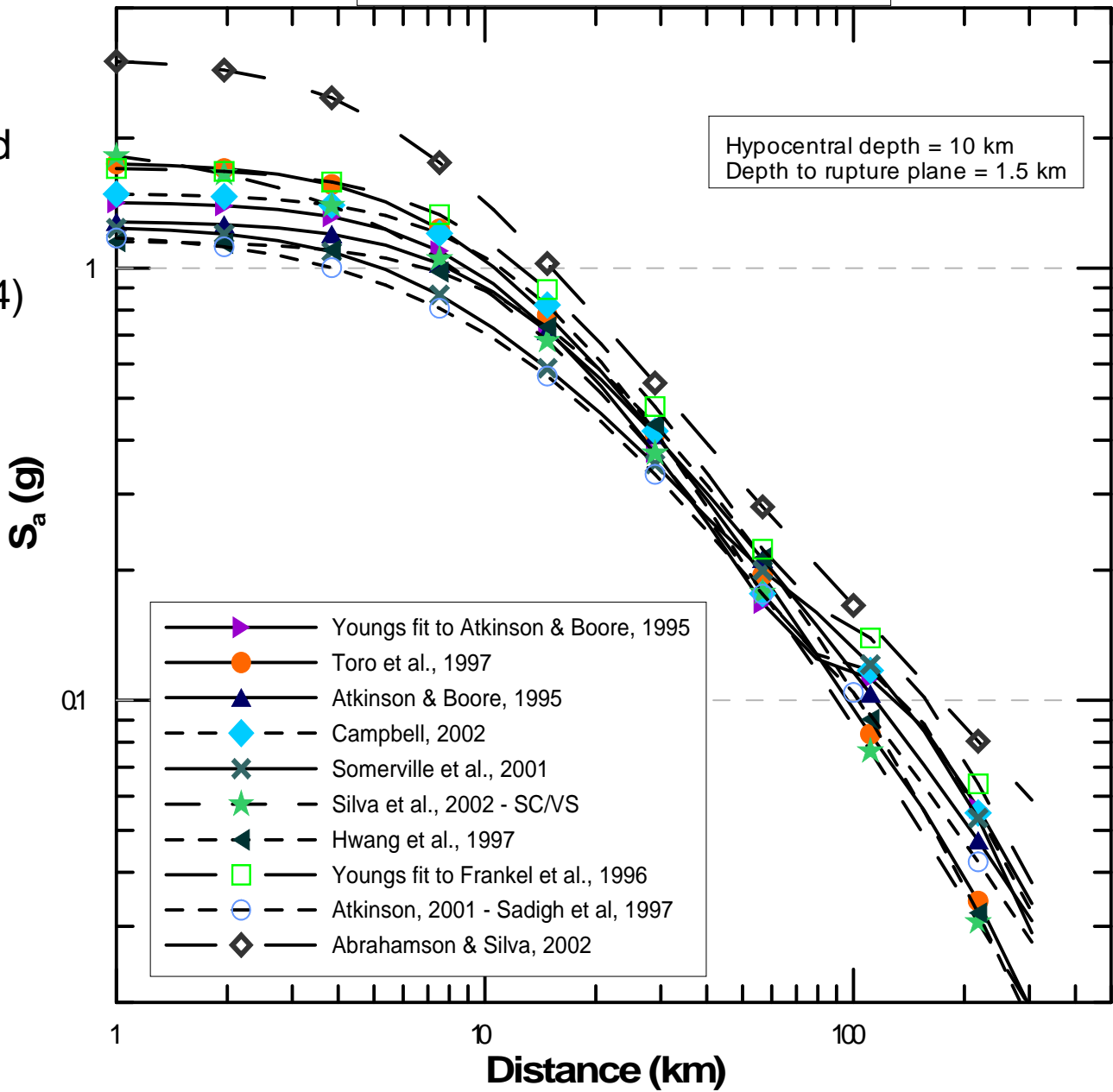
Spectral Acceleration 5 Hz M = 5.0

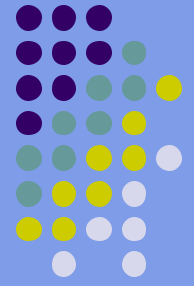
Example of alternative ENA ground motion relations (EPRI, 2004)



Spectral Acceleration 5 Hz M = 7.0

Example of alternative ENA ground motion relations (EPRI, 2004)

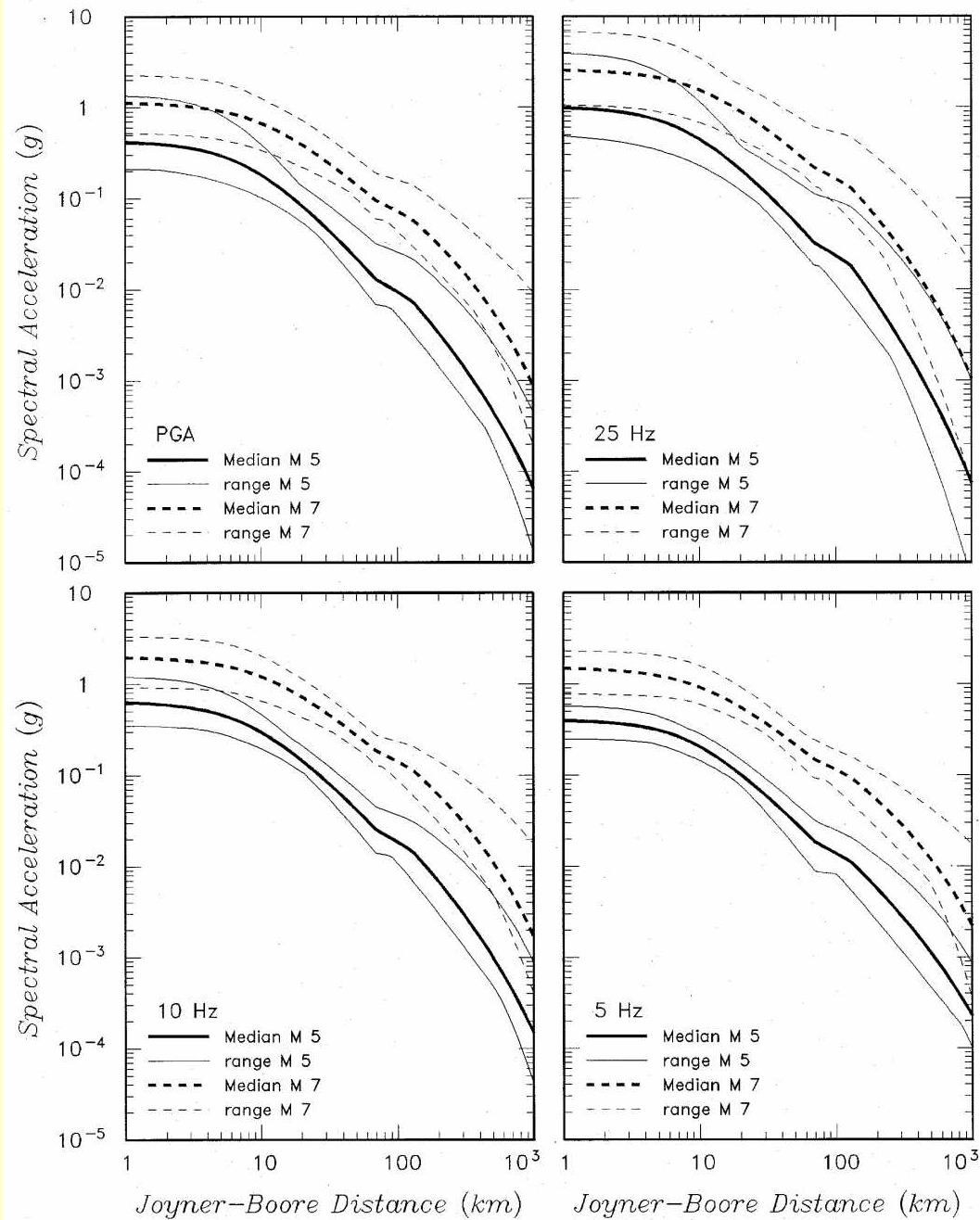
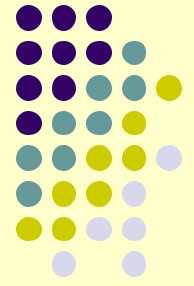




Overview of relations

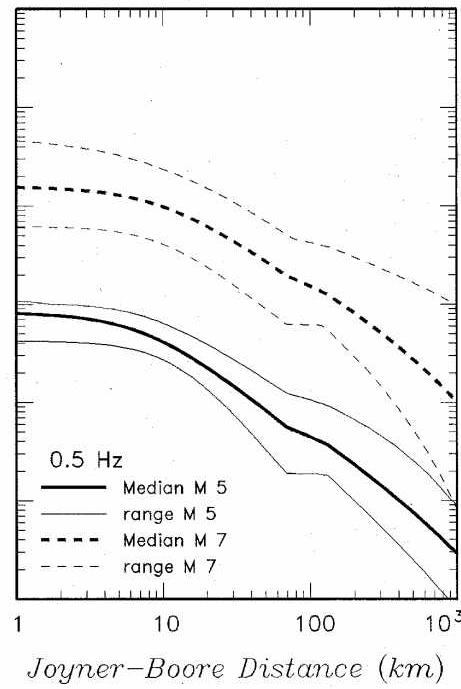
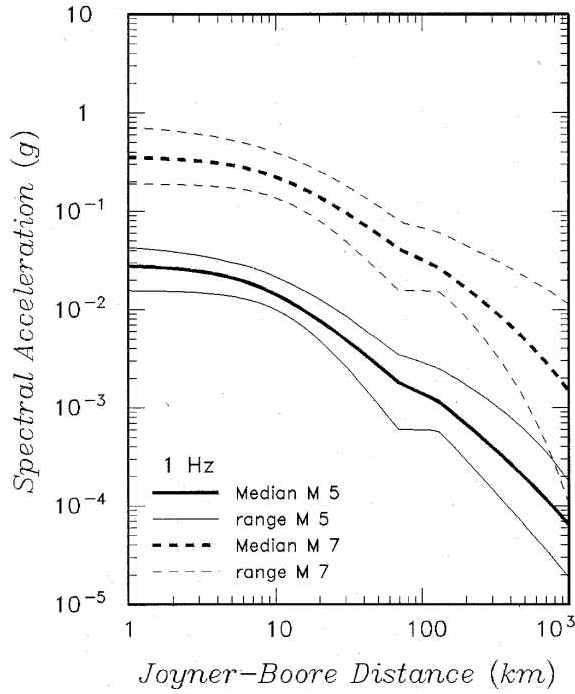
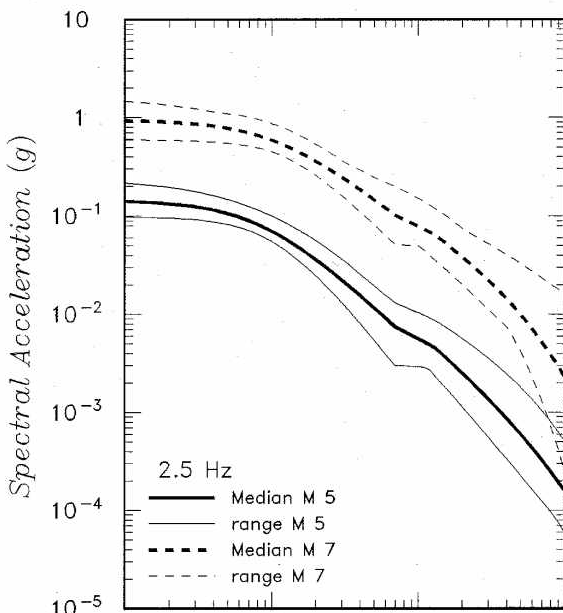
- EPRI (2004) provided overall synthesis and evaluation of the four main types of ground motion relations (to 2003)
- Results given as family of alternative relations expressing overall epistemic uncertainty (ie. uncertainty in modeling)
- Model for aleatory uncertainty (random variability) also provided

Note that in hazard analysis both epistemic and aleatory uncertainty in ground motion relations are important input parameters.



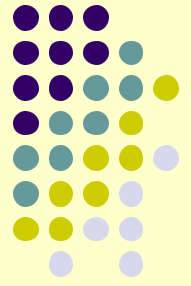
General Mid Continent

Range of models for M5 and M7 (EPRI, 2004)

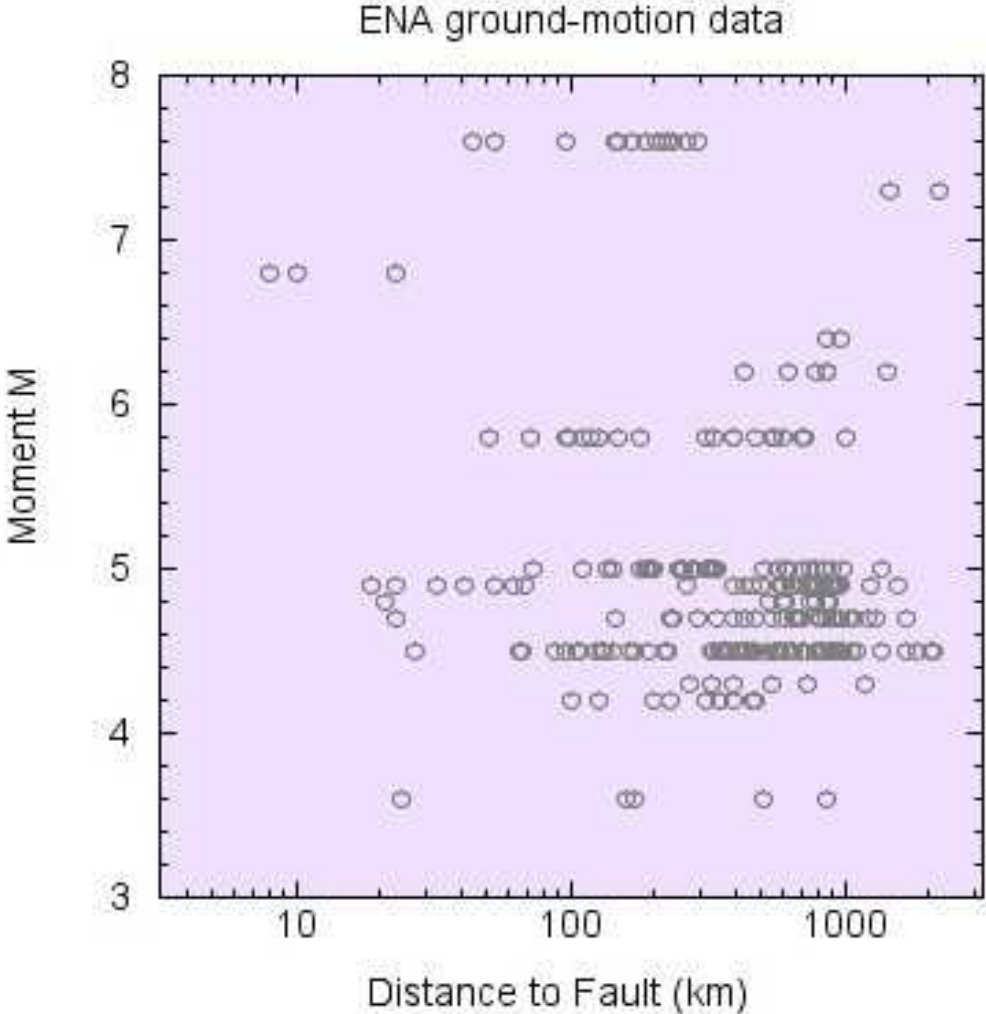


General Mid Continent

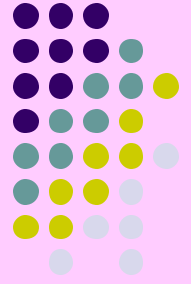
Range of models for M5 and M7 (EPRI, 2004)



Ground Motion Data (ENA)



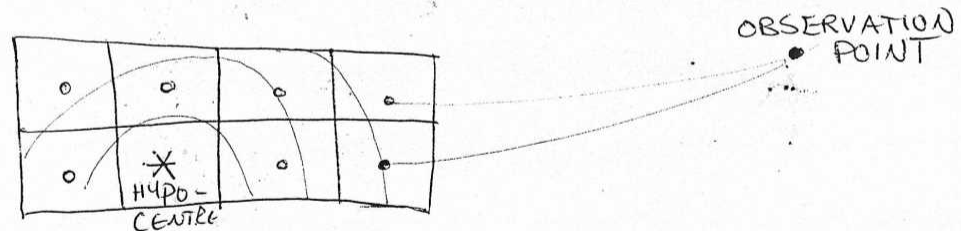
Atkinson and Boore 2005 relations



- Based on stochastic finite-fault model (of Motazedian and Atkinson, 2005)
- Key source parameter is stress drop – determined from compilation of instrumental and historical data
- Attenuation model based on empirical trilinear model of Atkinson, 2004 for ENA

STOCHASTIC FINITE-FAULT MODEL
(Beresnev and Atkinson, 1997, 1998)

TREAT FINITE FAULT PLANE AS AN ARRAY OF
SUBFAULTS



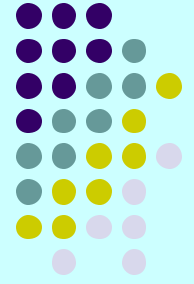
MODEL EACH SUBFAULT AS A STOCHASTIC
POINT SOURCE, WITH A BRUNE (ω^2) SOURCE
SPECTRUM

RUPTURE STARTS AT A SPECIFIED SUBFAULT
(HYPOCENTRE), AND PROPAGATES IN ALL
DIRECTIONS WITH SPECIFIED RUPTURE
PROPAGATION VELOCITY (SAY 0.8 TIMES SHEAR
WAVE VELOCITY).

SUBFAULT RADIATION IS 'TRIGGERED' WHEN
RUPTURE REACHES THE CENTRE OF THE
SUBFAULT

CONTRIBUTIONS TO RADIATION AT
OBSERVATION POINT ARE SUMMED OVER ALL
SUBFAULTS.

**Stochastic finite
fault model (Silva;
Beresnev and
Atkinson;
Motazedian and
Atkinson, 2005)**



Parameters needed to apply stochastic finite-fault model

- All parameters needed for stochastic point source model
- Geometry of source (can assume fault plane based on empirical relations such as Wells and Coppersmith on fault length and width vs. M)
- Direction of rupture propagation (assumed random)
- Slip distribution on fault (assumed random)

Some features of Motazedian and Atkinson (2005) stochastic finite fault model:

- simulations independent of subfault size (conservation of radiated energy)
- model applicable over wide range of magnitudes (can simulate M 4 to 8 with single consistent model)
- incorporation of “self-healing” behavior

Figure 3.a 100 % Pulsing area

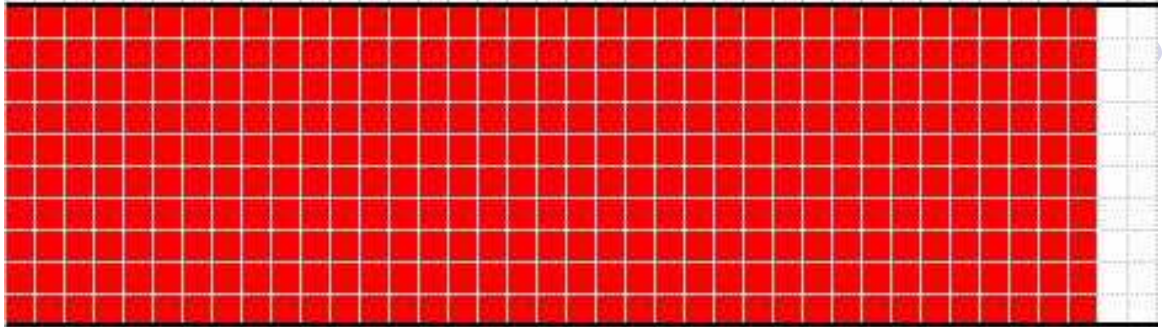


Figure 3.b 25% Pulsing area

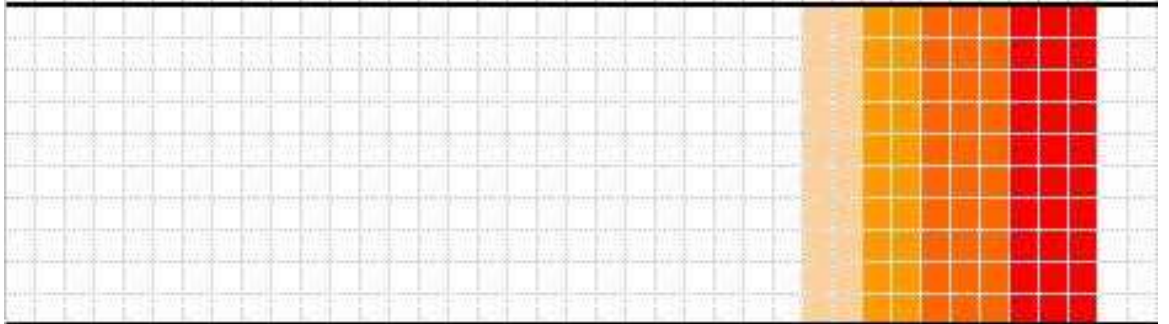


Figure 3. a-b. In the healing-front model (3. a) when a subfault ruptures, the total ruptured area contributes to the frequency content of the radiated wave from the rupturing subfault. In the self-healing model, a wave front has a tail which includes the pulsing subfaults and those subfaults that are still sliding. In the self-healing model (3. b), the passive area (white cells) should not have any effect on the frequency content of the distant subfault.

**Self-healing
model: in the
lower panel, only
part of the fault is
slipping at any
one time**



The low-frequency spectral shape (and sag at intermediate frequencies) is controlled by the %pulsing area

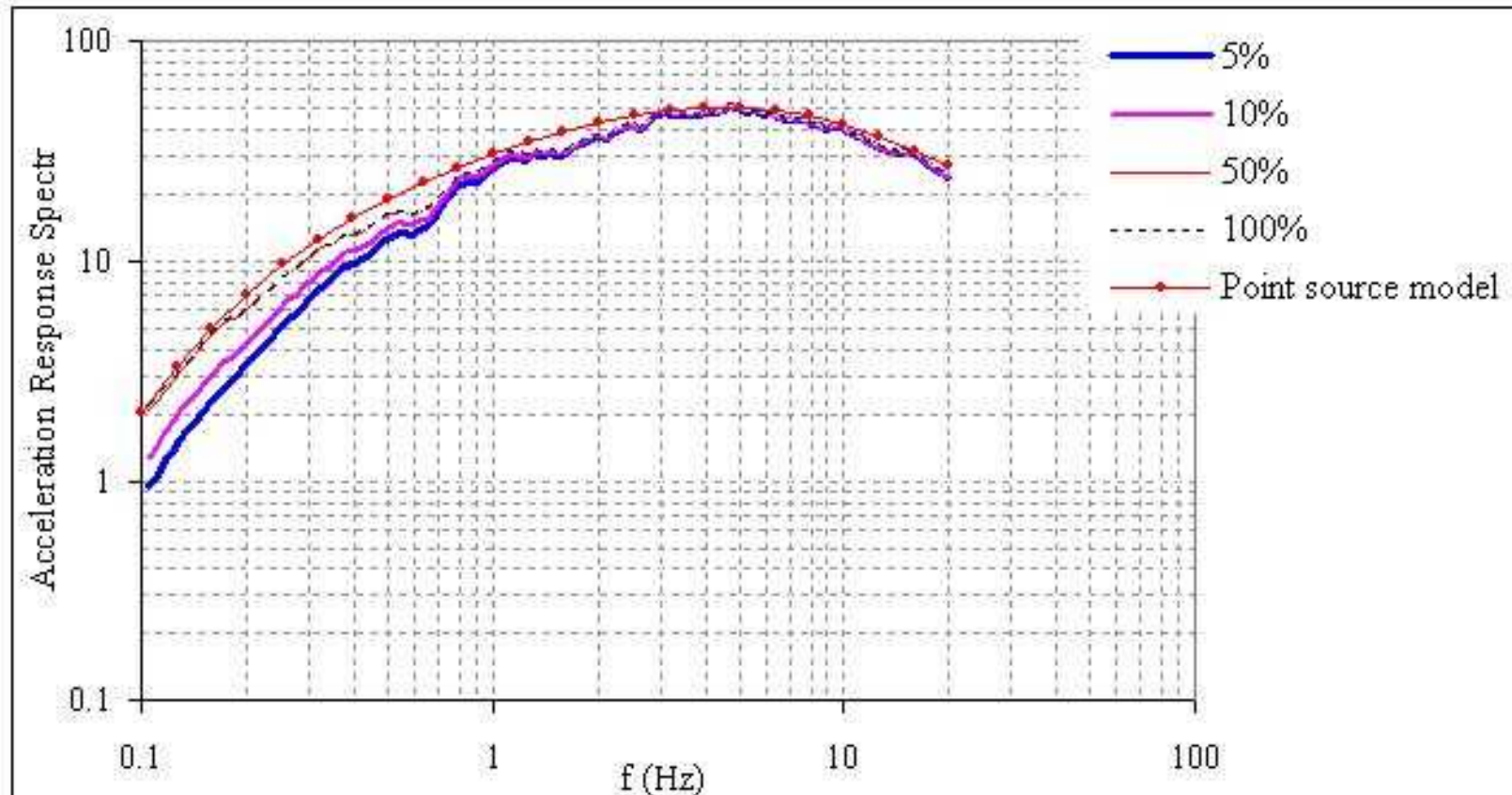


Fig 5. 5% damped pseudo-acceleration for event of M7.0 at R=100 km for different pulsing area percentages, using dynamic corner frequency and corresponding point-source model. In EXSIM, variation of pulsing area can be used to adjust the relative amplitudes of low-frequency motion in finite fault modeling. A narrow pulsing area results in lower amplitudes at longer periods.

Finite-fault model reproduces 2-corner shape of source spectrum that is observed empirically (thus providing an explanation as to why we obtain a 2-corner shape)

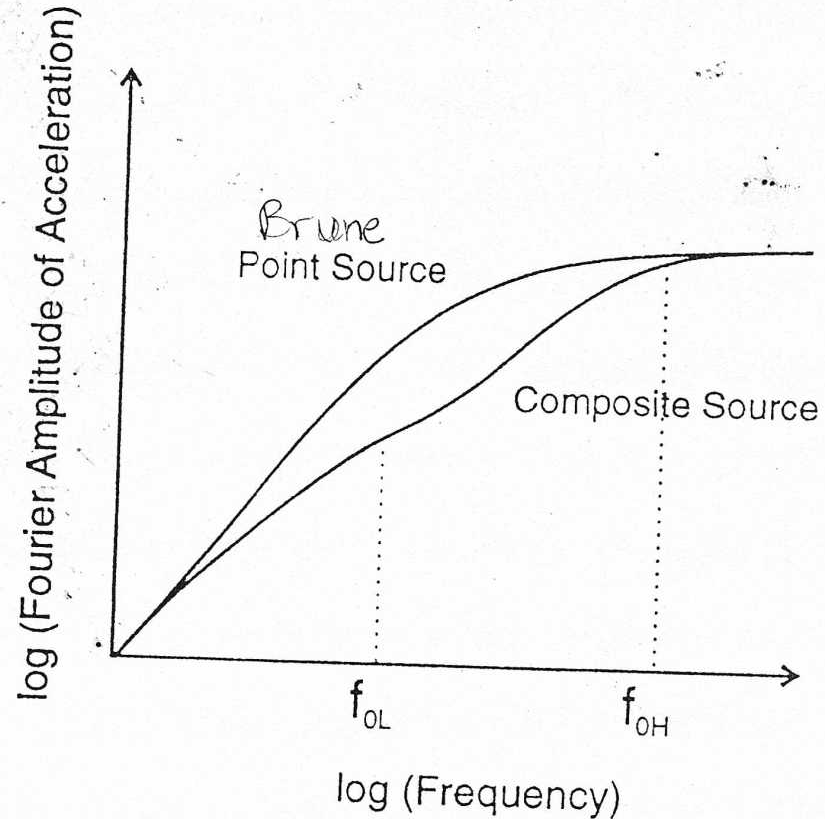


Figure 3. Comparison of the spectrum resulting from the summation of subevent point sources over a finite fault plane (lower line), with a single ω^2 spectrum, having the same moment magnitude and high-frequency spectral level (upper line). f_{OH} is the subfault corner frequency. f_{OL} is the second (low-frequency) corner produced by the summation procedure, under the conservation-of-moment constraint.

High-frequency spectral level depends on stress drop (as in point-source model)

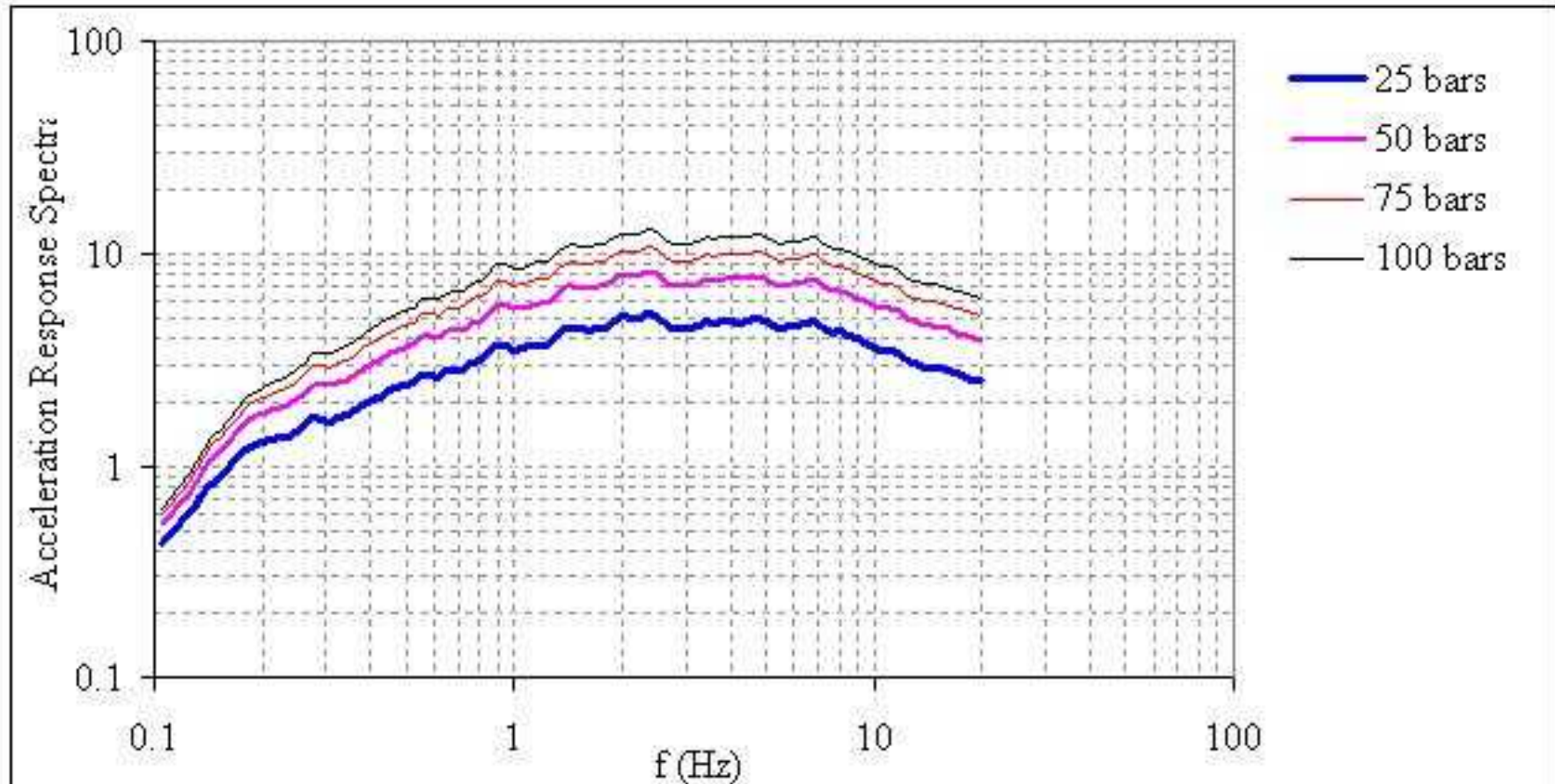


Fig 6. 5% damped pseudo-acceleration for event of M7.0 at R=333 km (25% pulsing area) for different stress parameter, using dynamic corner frequency. In EXSIM, variation of stress parameter can be used to adjust the relative amplitudes of high-frequency motion. By increasing the stress parameter, the amplitude of high frequencies increases.

Example
Finite-fault
stochastic
simulation
record

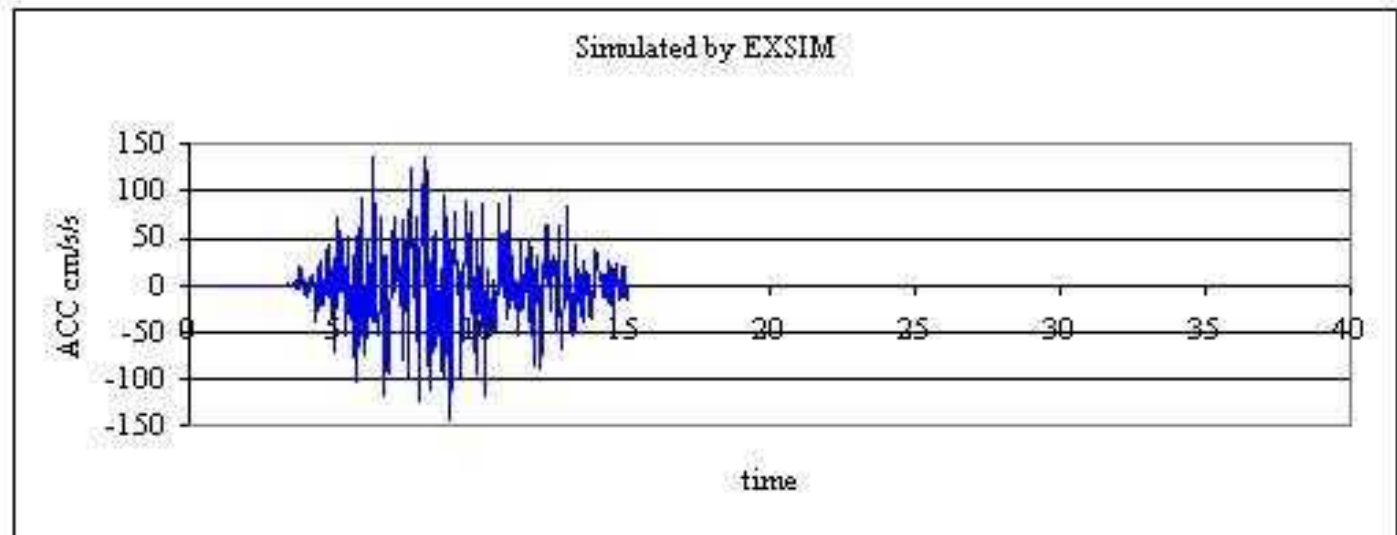
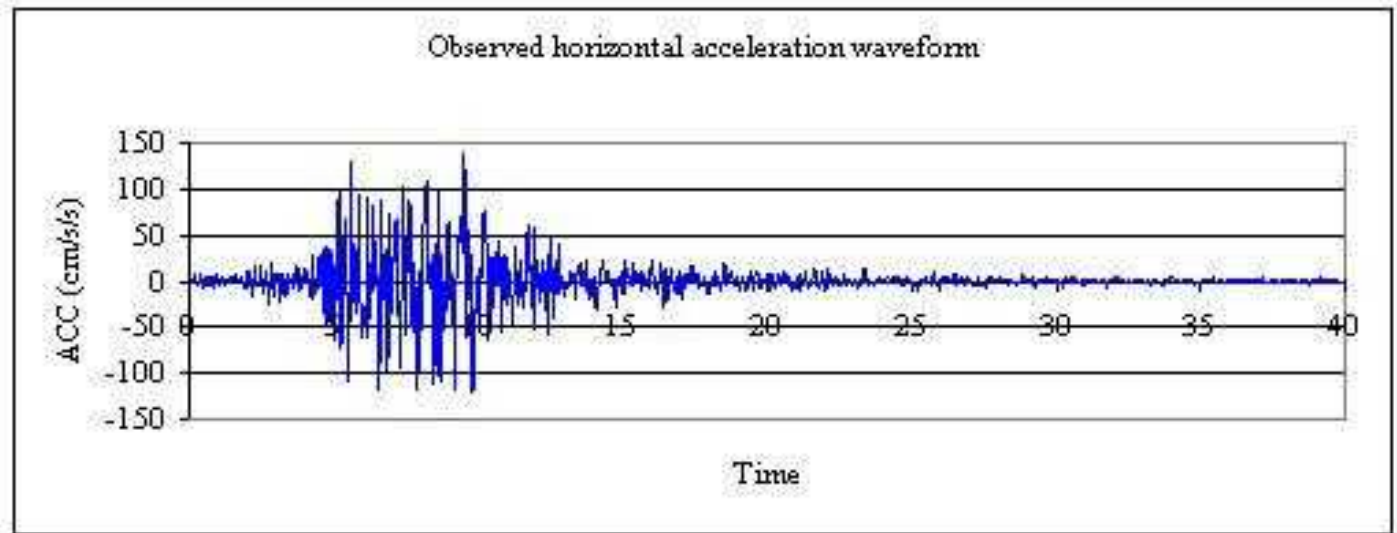


Figure 7. Simulated and observed horizontal acceleration waveform for M6.7, 1994 Northridge earthquake (Vasquez Rocks Park station).

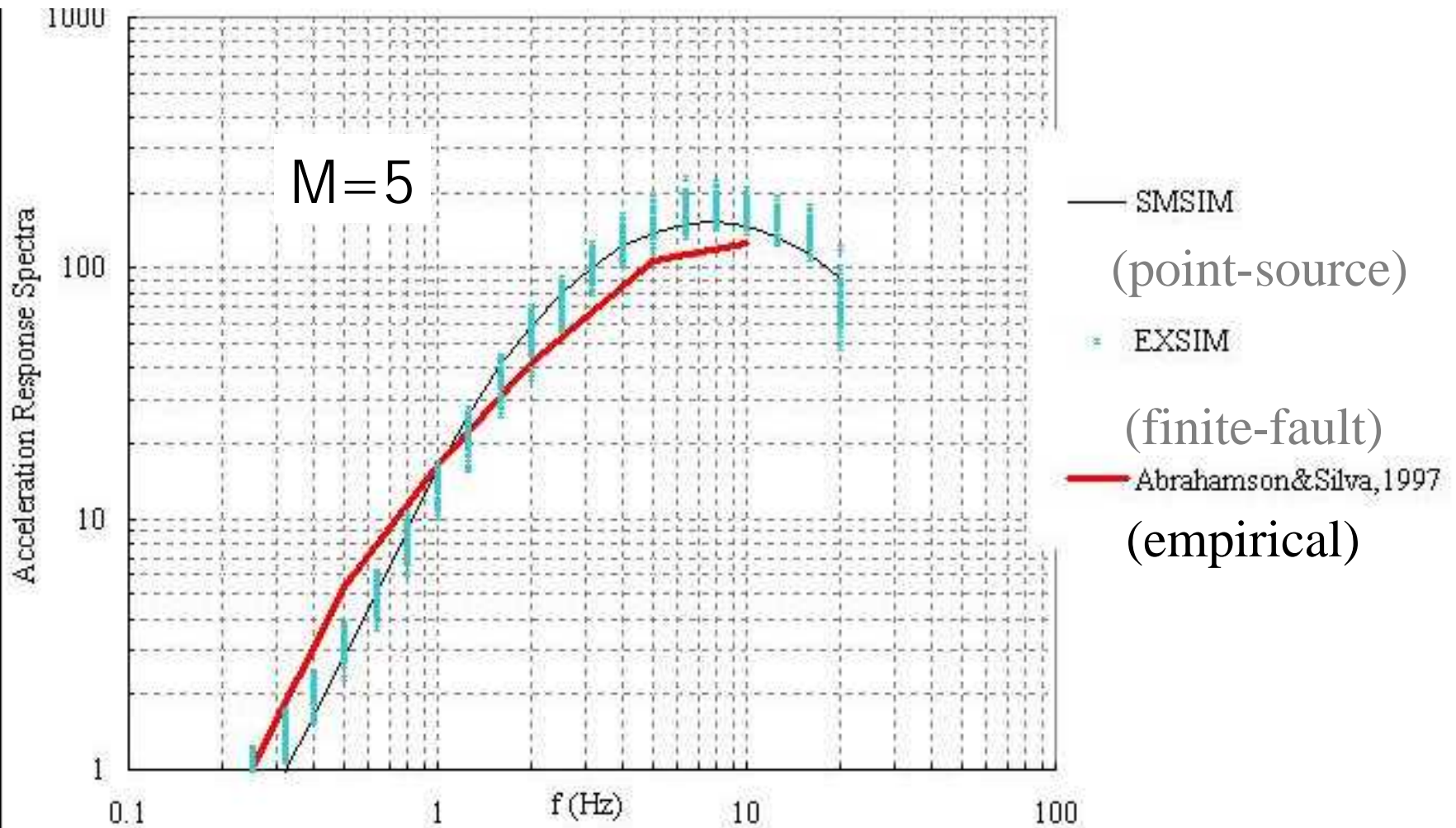


Fig 11. Comparison between response spectra from M5.0 point source modeling, SMSIM, Boore, 1995 ($R=15$, stress drop=120 bars), Abrahamson and Silva ground motion relations for California, 1997 ($R=15$), and EXSIM(a profile of observation points around the fault plane with $R=15$ km and azimuth coverage from 0 to 180 degrees, stress drop=120 bars, and 50% pulsing area).

Comparison of finite fault, point source and empirical models for M5 in California

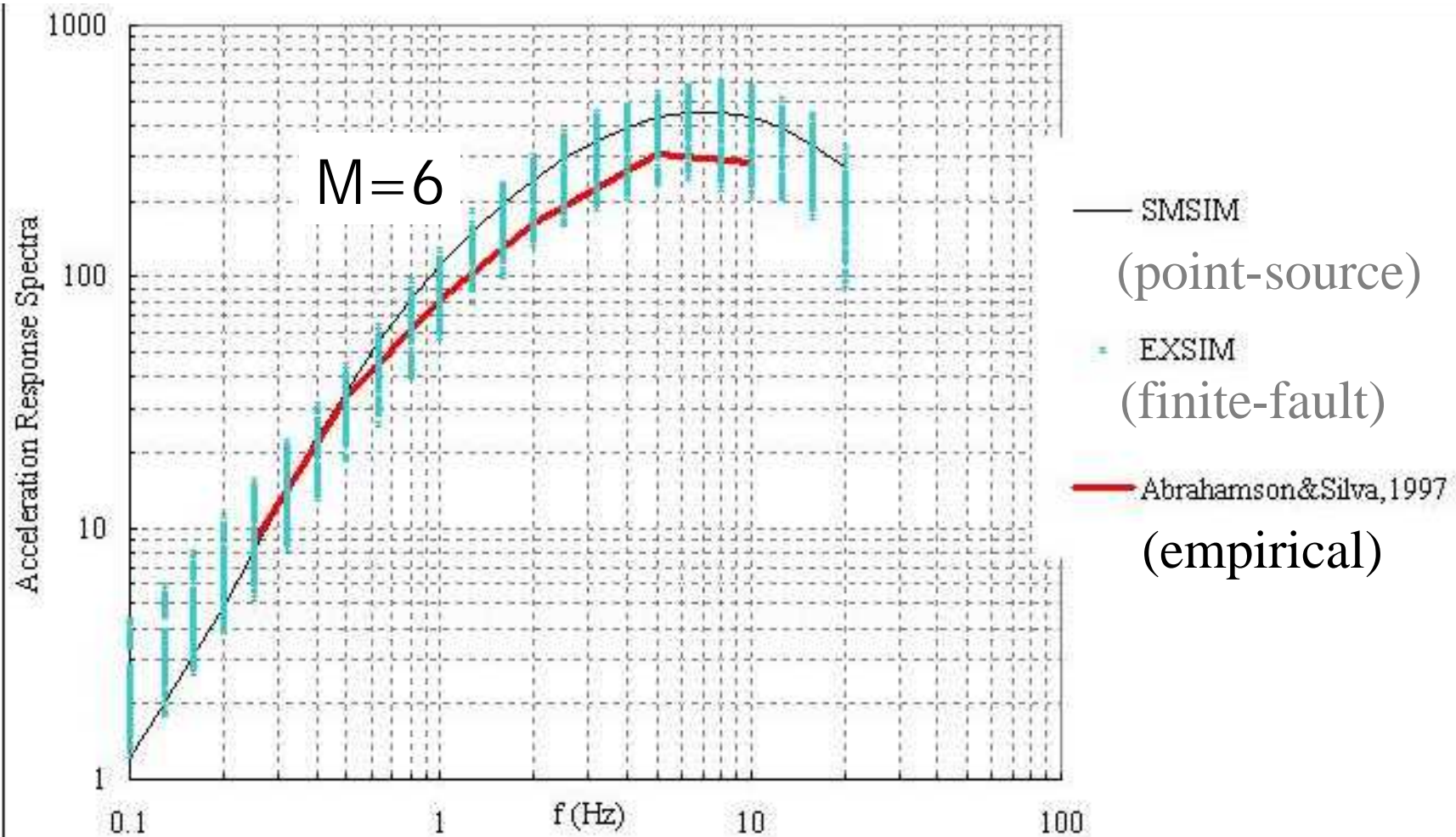


Fig 12. Comparison between response spectra from **M6.0** point source modeling, SMSIM, Boore, 1995 ($R=15$, stress drop=120 bars), Abrahamson and Silva ground motion relations for California, 1997 ($R=15$), and EXSIM(a profile of observation points around the fault plane with $R=15$ km and azimuth coverage from 0 to 180 degrees, stress drop=120 bars, and 50% pulsing area).

Comparison of finite fault, point source and empirical models for M6 in California

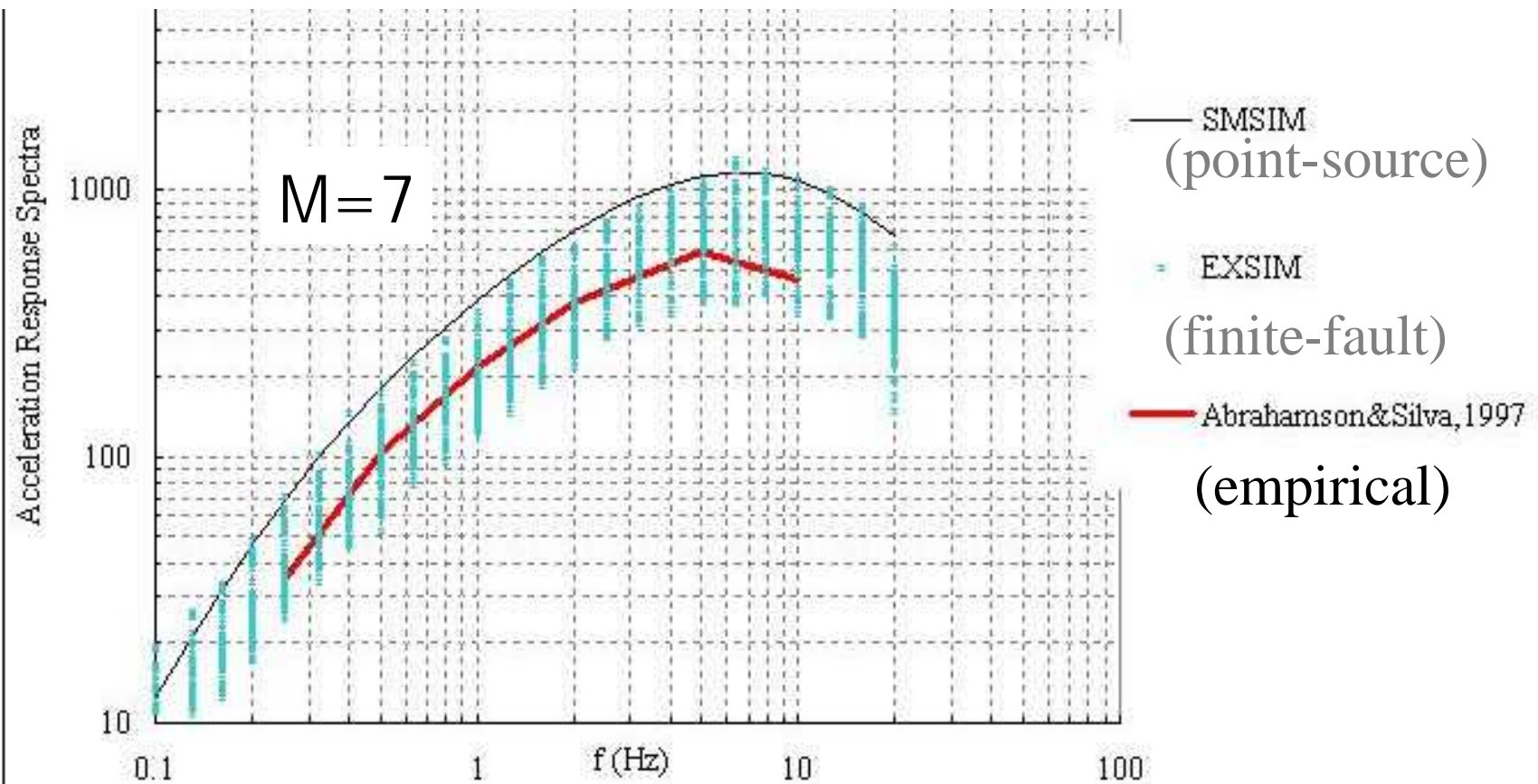


Fig 13. Comparison between response spectra from $M7.0$ point source modeling, SMSIM, Boore, 1995 ($R=15$, stress drop=120 bars), Abrahamson and Silva ground motion relations for California, 1997 ($R=15$), and EXSIM (a profile of observation points around the fault plane with $R=15$ km and azimuth coverage from 0 to 180 degrees, stress drop=120 bars, and 50% pulsing area). Finite-fault effects in ground motions become important for larger earthquakes. Point source models of earthquake ground motion are inappropriate for earthquakes that rupture an extended fault plane.

Comparison of finite fault, point source and empirical models for M7 in California

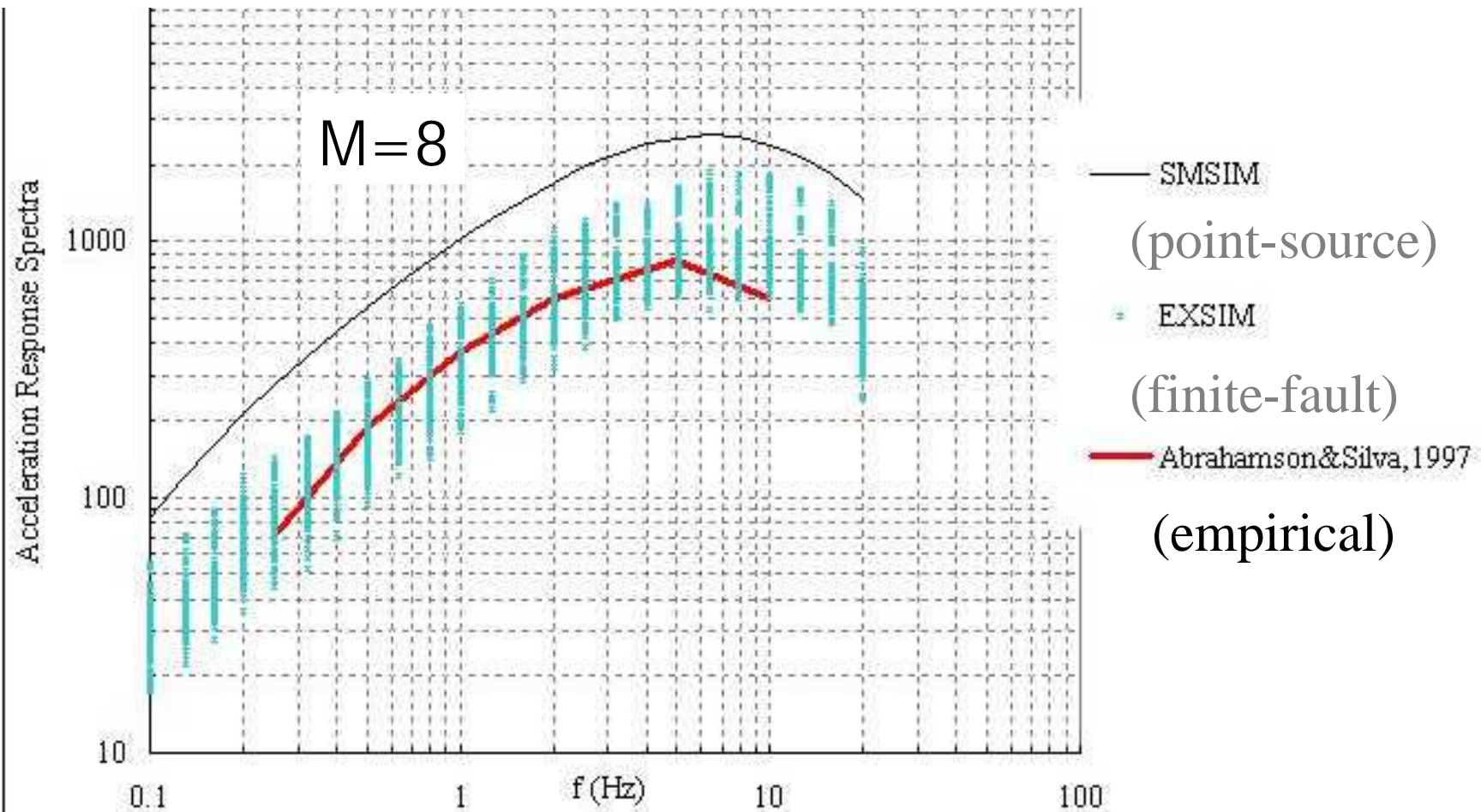


Fig 14. Comparison between response spectra from **M8.0** point source modeling, SMSIM, Boore, 1995 ($R=15$, stress drop=120 bars), Abrahamson and Silva ground motion relations for California, 1997 ($R=15$), and EXSIM(a profile of observation points around the fault plane with $R=15$ km and azimuth coverage from 0 to 180 degrees, stress drop=120 bars, and 50% pulsing area). Finite-fault effects in ground motions become important for larger earthquakes. Point source models of earthquake ground motion are inappropriate for earthquakes that rupture an extended fault plane.

Comparison of finite fault, point source and empirical models for M8 in California

ENA Model Parameters and their aleatory variability (AB05)



Parameter	Distribution type	Median	Standard Deviation	Minimum	Maximum
Fault Dip	Normal	50.	20.	10.	90.
Log stress	Normal	2.14	0.31		
Pulsing%	Random			10.	90.
Kappa	Random			0.002	0.01
b1 (R<70)	Random	-1.3		-1.5	-1.1
b2 (70-140)	Random	+0.2		-0.5	+0.9
Depth	Normal	13.	10.	2.	30.
Fault length factor	Random			0.2	0.8
Fault width factor	Random			0.4	1.0

Database of Vertical component Fourier Amplitudes

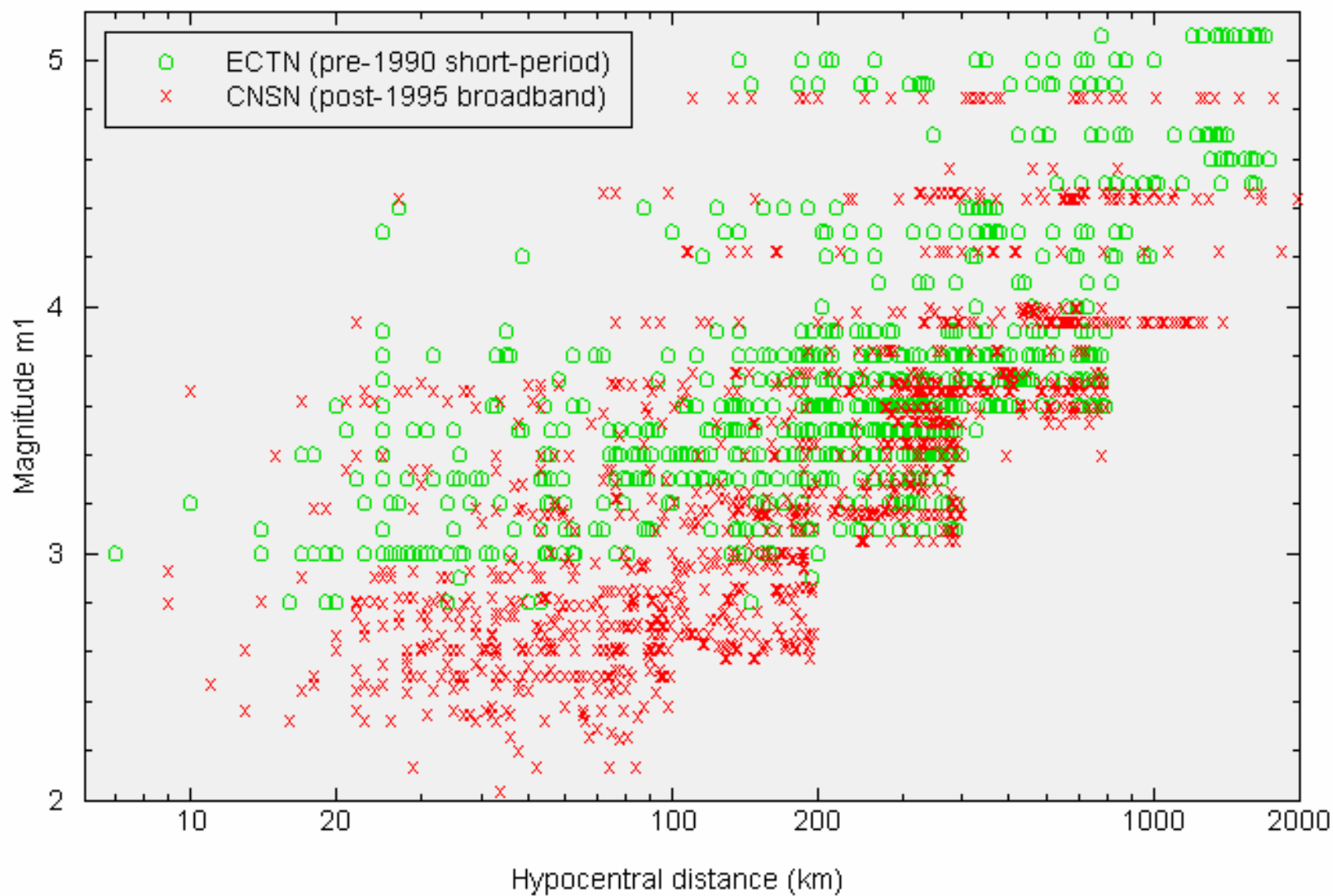
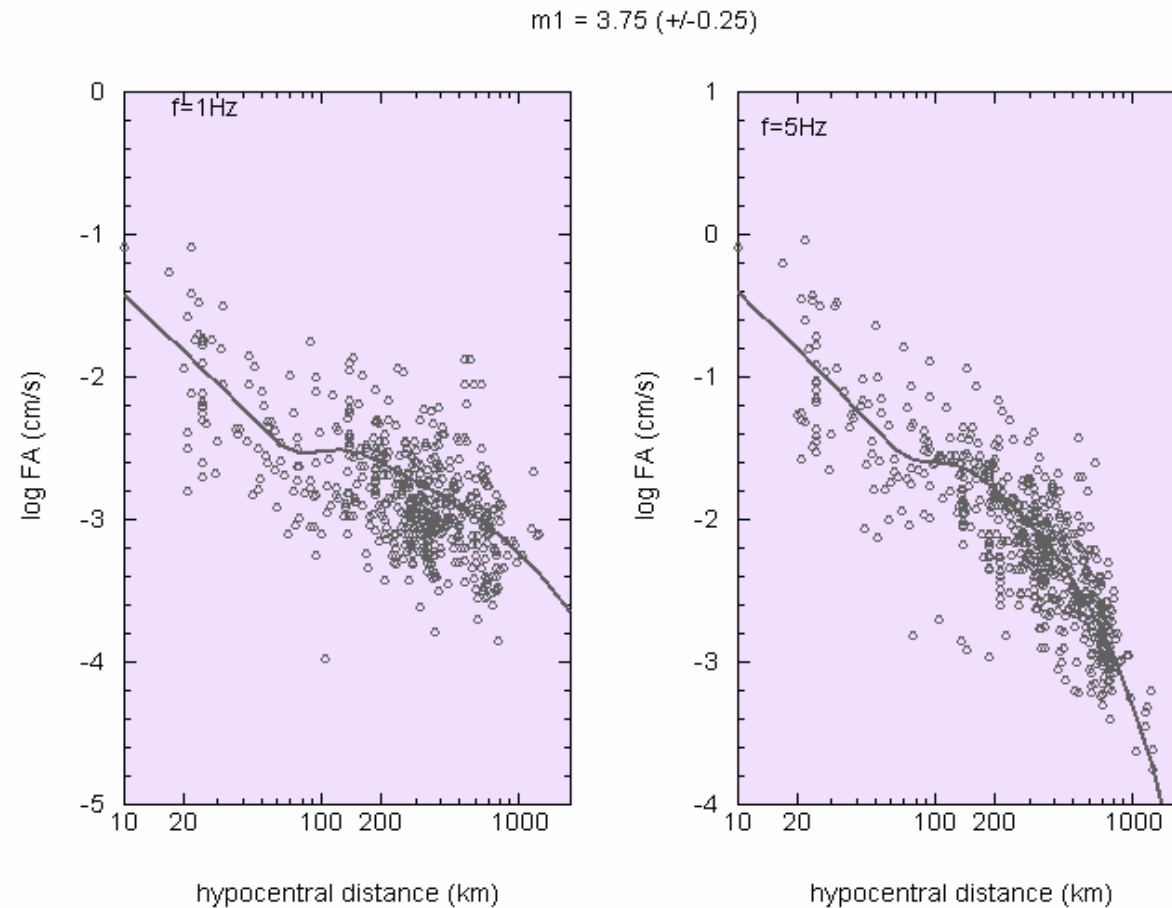
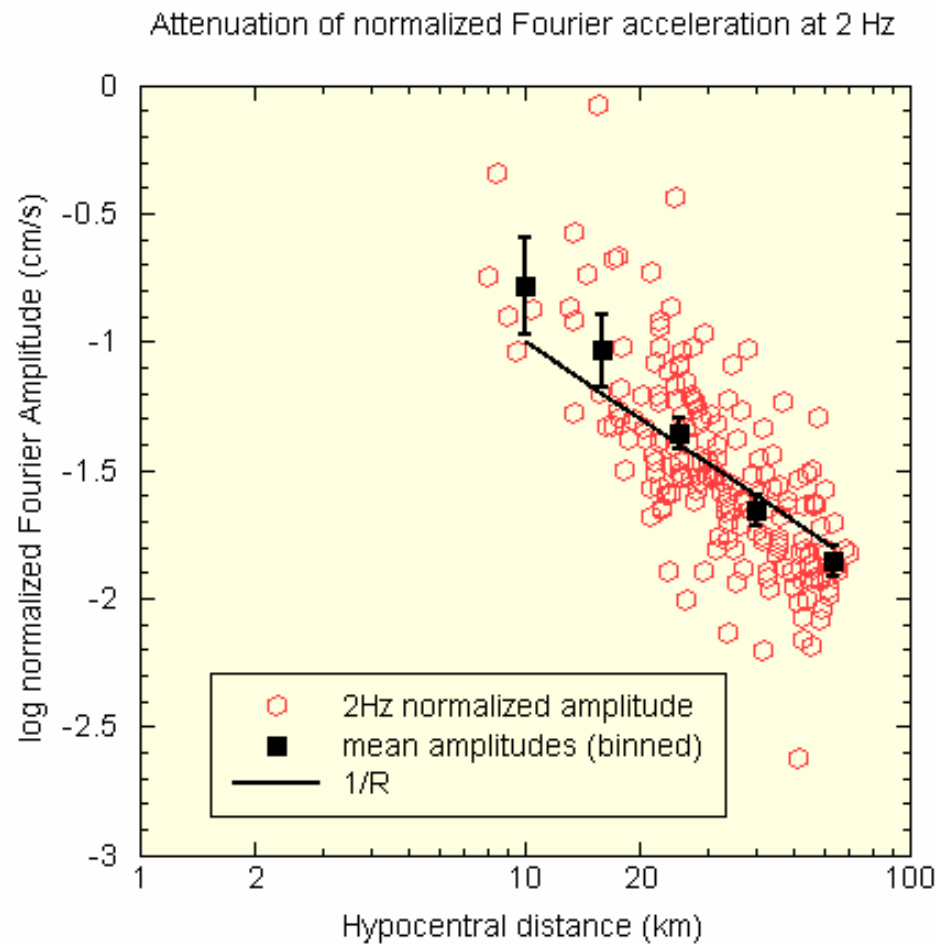




Illustration of typical decay of spectral amplitudes for $m_1=3.75$. Line is trilinear shape fitted to the data. Transition distances are $r_{01}=70$ km, $r_{02} = 140$ km. Slopes of geometric attenuation: $-1.3, +0.2, -0.5$



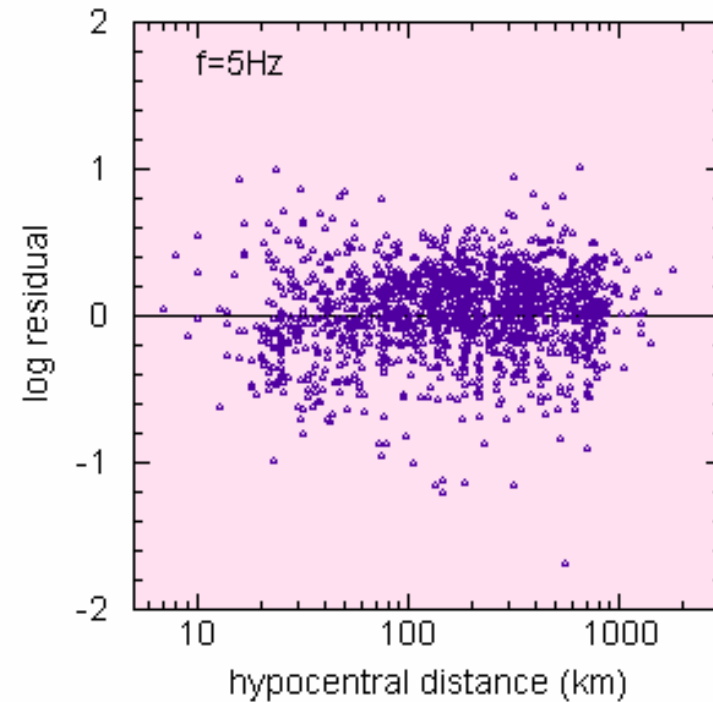
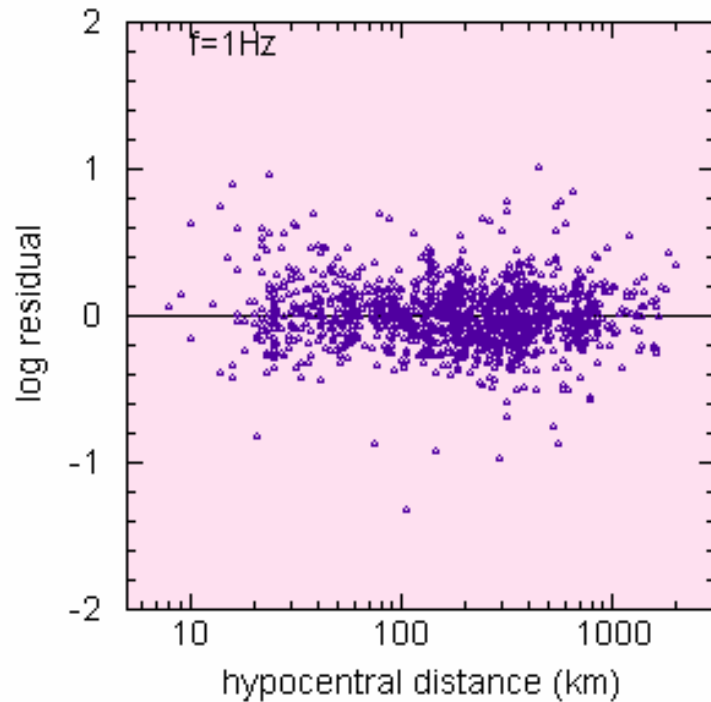
Amplitudes decay faster than $1/R$ at $R < 70$ km. This has important implications for ENA ground motion relations.



Residuals versus distance (1 and 5 Hz) for regression model (attenuation transitions r01, r02, geometric spreading slopes -1.3, +0.2, -0.5)



Regression Residuals (transitions 70, 140 km: $b_1=1.3$, $b_2=-0.2$)

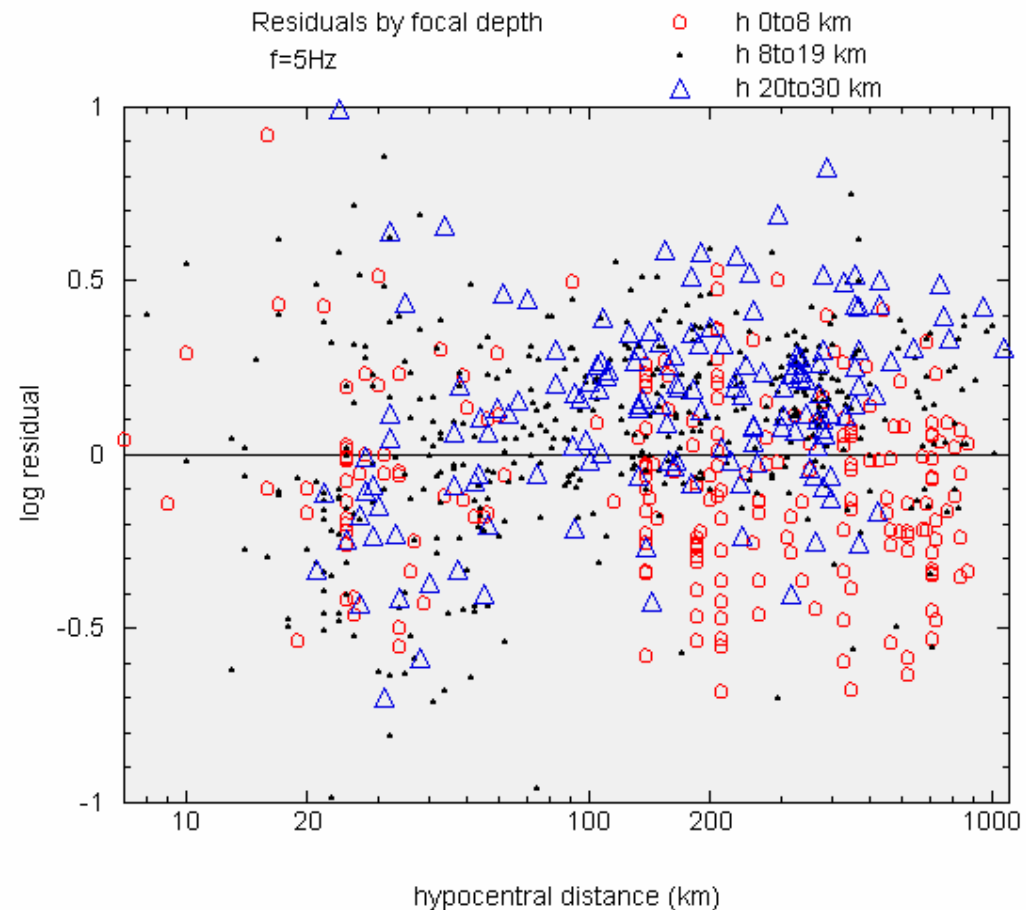




Regression residuals show distance trends when broken down by focal depth: deeper events attenuate more slowly than shallow events, especially at high frequencies

A correction factor to the attenuation based on focal depth was developed to account for the depth-dependence of attenuation:

$$\text{Log Correction Factor} = d1 (h-10) \log R + d2$$

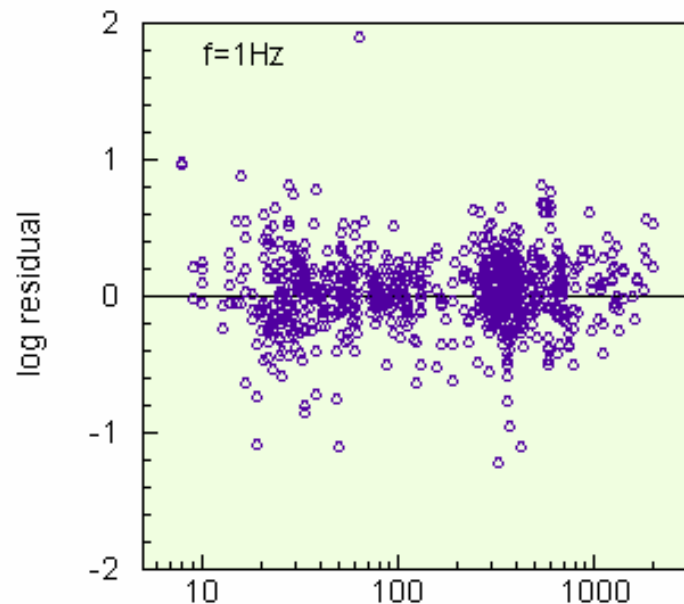




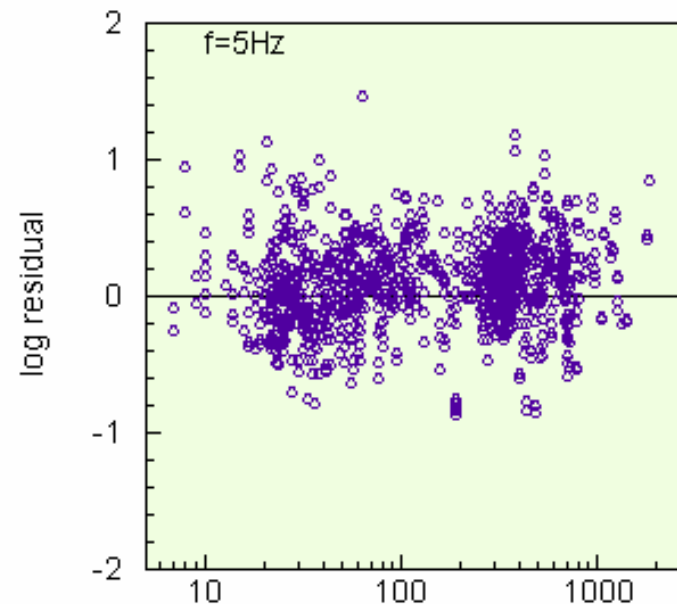
Evaluate whether the horizontal component attenuates differently than the vertical: apply the regression equation developed for the vertical component to the horizontal component data, and examine residuals (log observed – log predicted) versus distance.

Mean residual = H/V.

Horizontal-Component Residuals (transitions 70, 140km: $b_1=1.3$, $b_2=-0.2$)

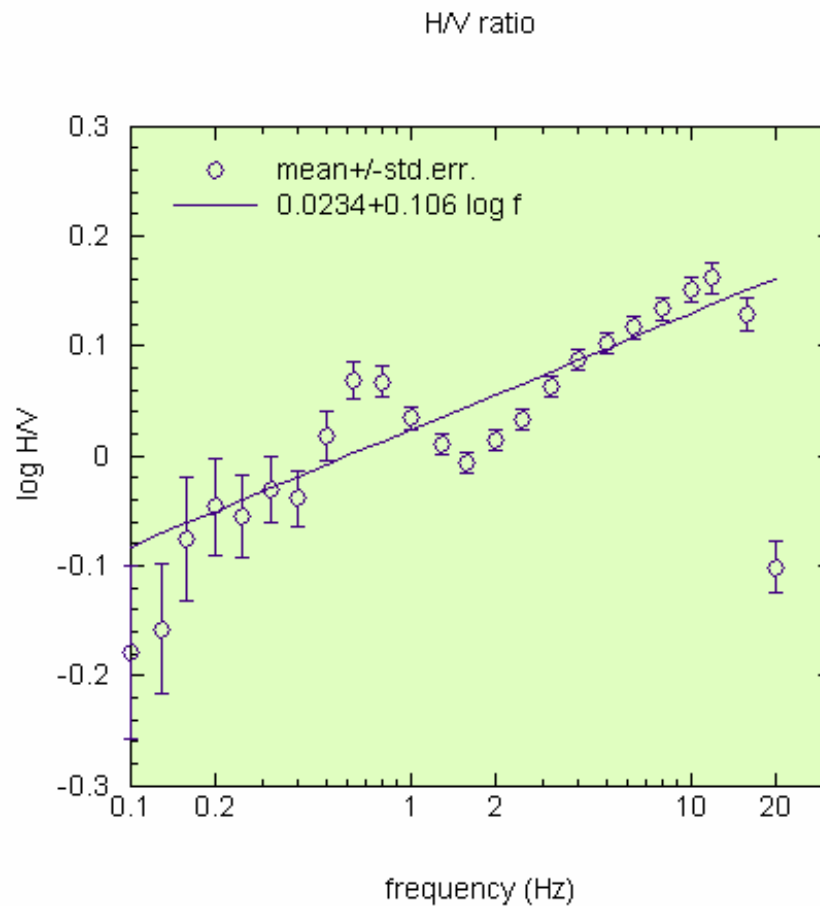
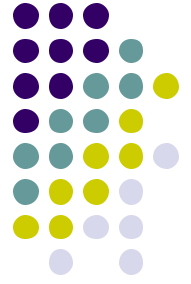


hypocentral distance (km)



hypocentral distance (km)

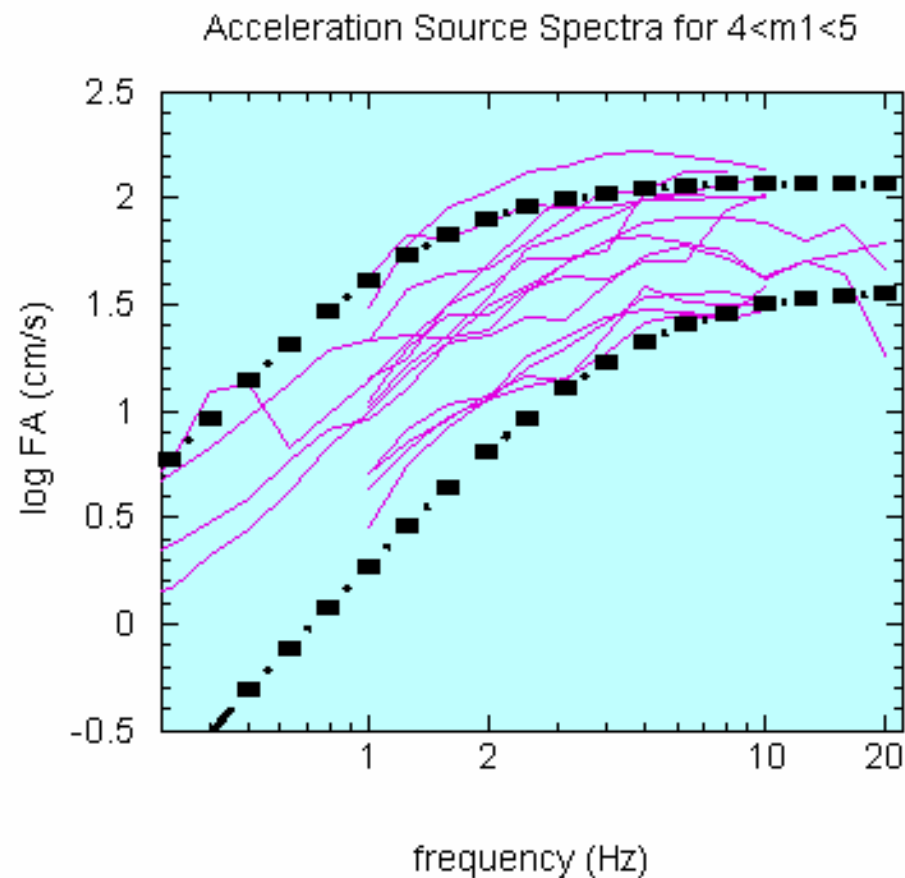
**Mean H/V ratio for ENA rock sites:
increases with frequency from values near unity at 1 Hz to a
factor of about 1.5 at high frequencies. This H/V is
assumed to represent crustal to near-surface amplification
effects for rock sites.**





Attenuation results can be used to correct observations back to the source, to obtain apparent source spectra for individual earthquakes. Events of $m_1 > 4$ follow Brune model with stress drop ~ 100 bars.

Thick black lines show Brune model spectra for 100 bars, for $M=4, 5$. Thin lines show source spectra for events of $4 < m_1 < 5$

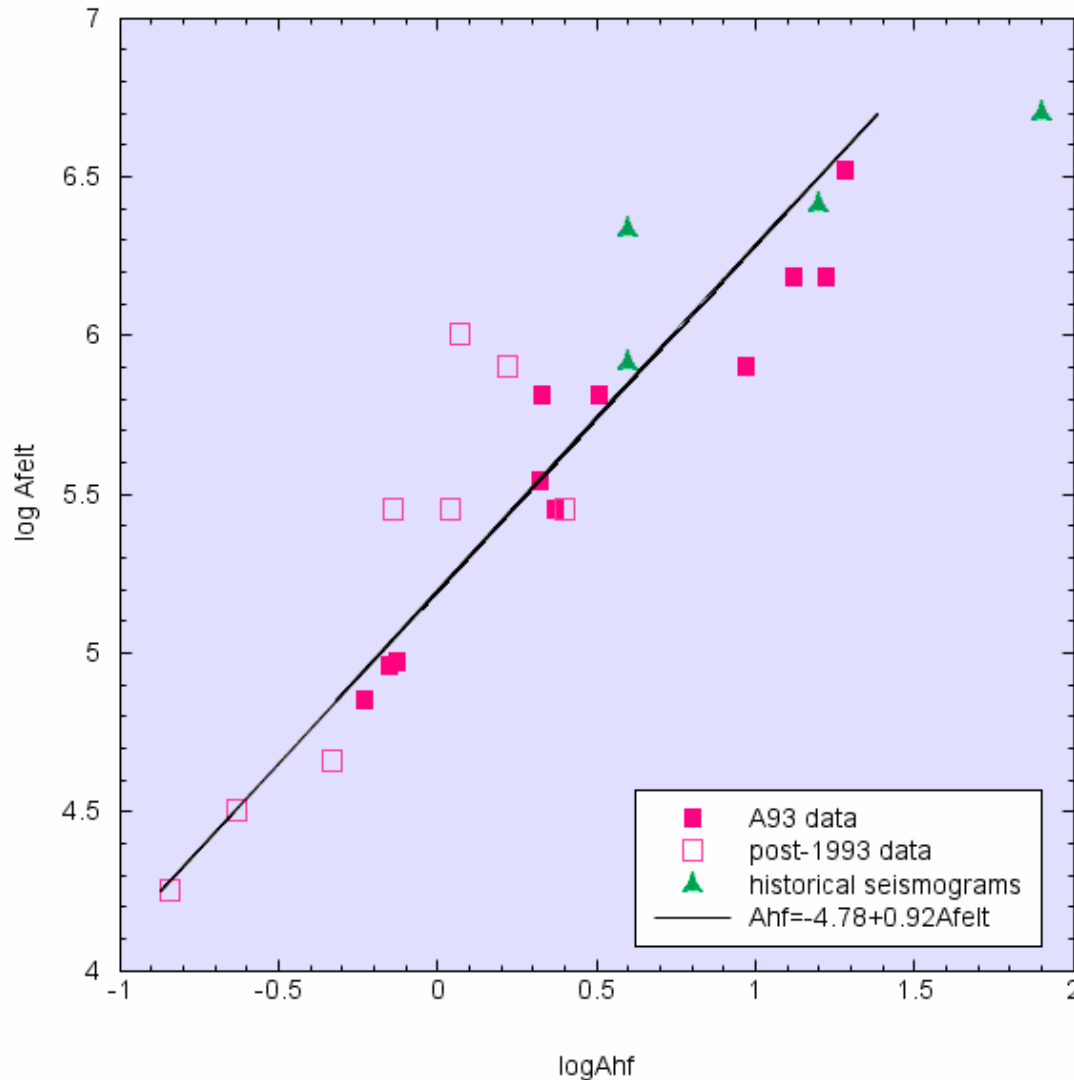


Data on high-frequency levels can be augmented by historical data based on felt areas.



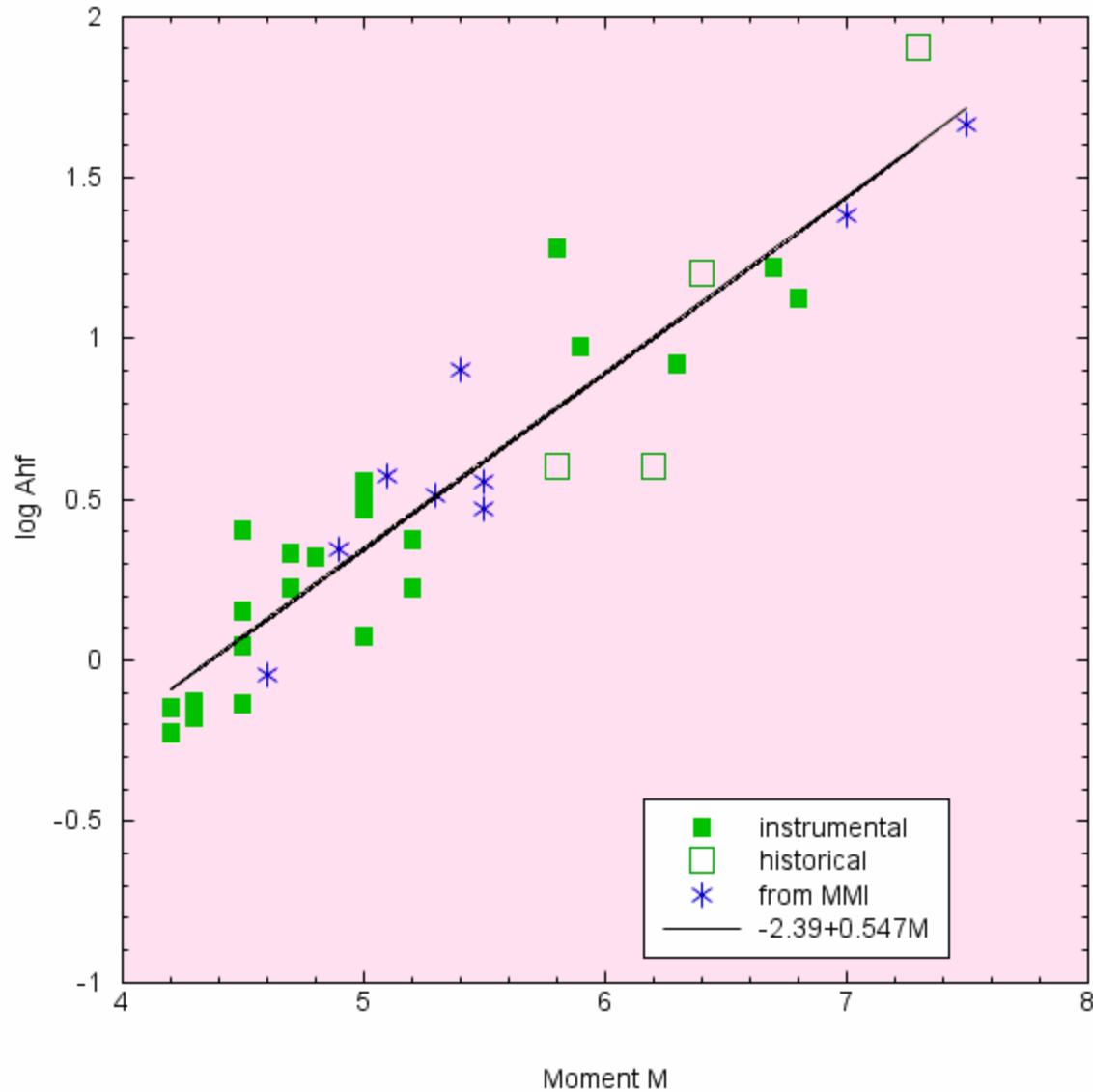
Felt area vs. High-Frequency FACCN at R=20km

Relationship between felt area and high-frequency spectral acceleration level (at a reference distance of 20 km). Symbols show data from Atkinson (1993a) (filled squares), data from Atkinson (2004) (open squares) and historical seismogram data of Atkinson and Chen (1997). Lines show least-squares fit.

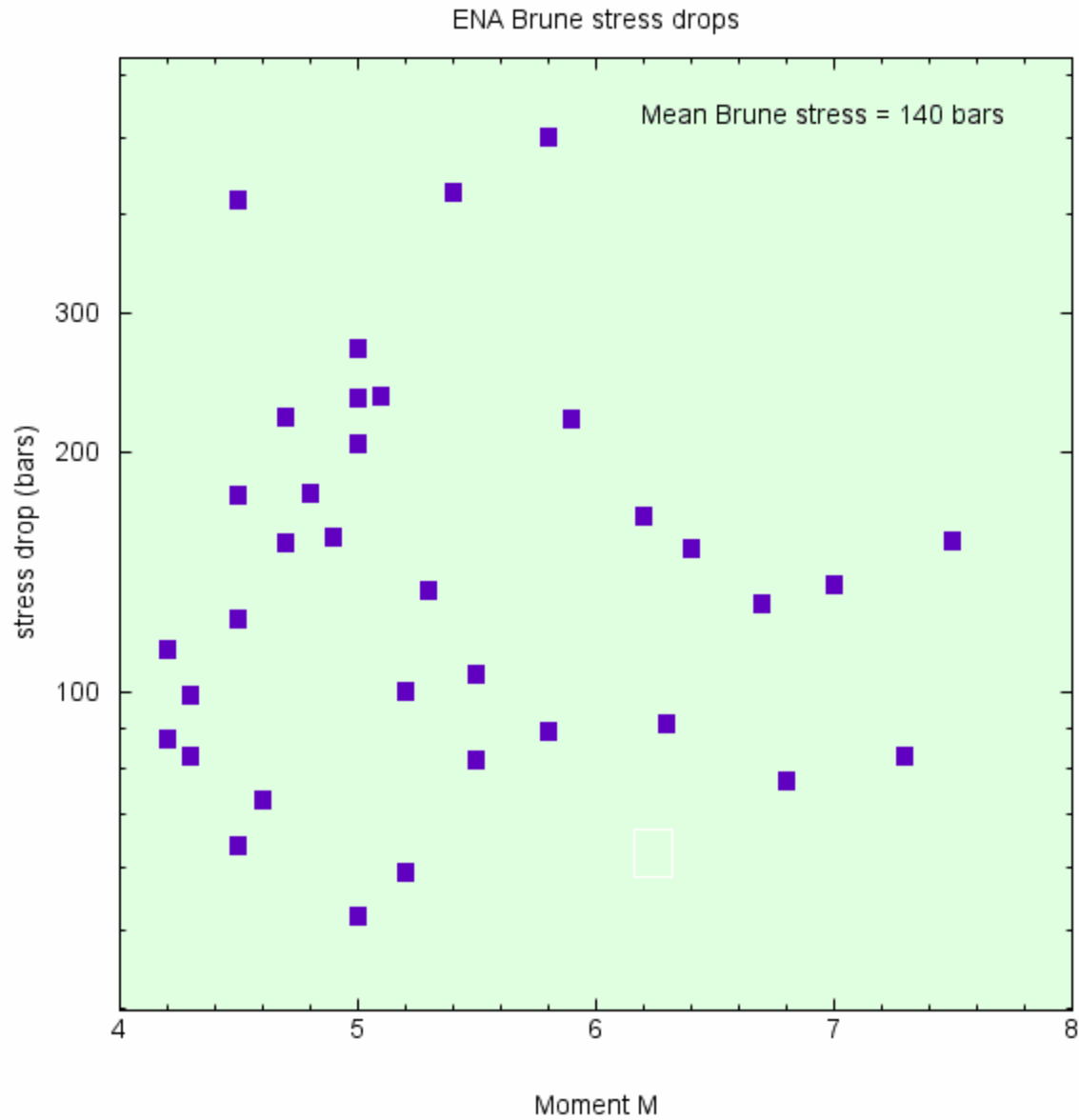




High-Frequency FACCN at R=20km vs. Moment M



Compilation of ENA data on high-frequency levels, from both instrumental and historical data: this information can be used to infer stress drop

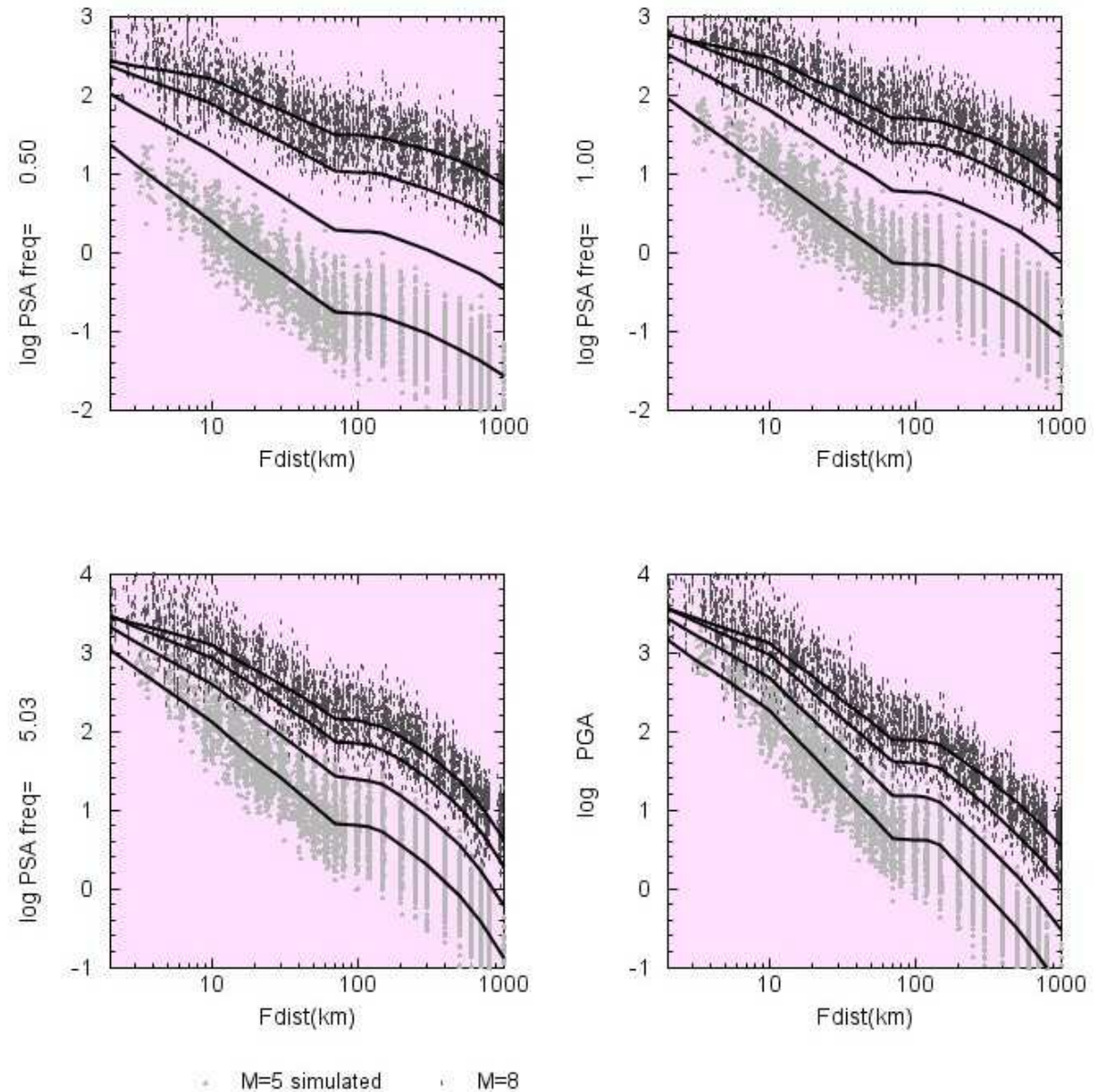


**ENA stress drops,
based on high-
frequency spectral
level. Mean = 140
bars.**

This shows simulations with aleatory uncertainty: Nov. 2005

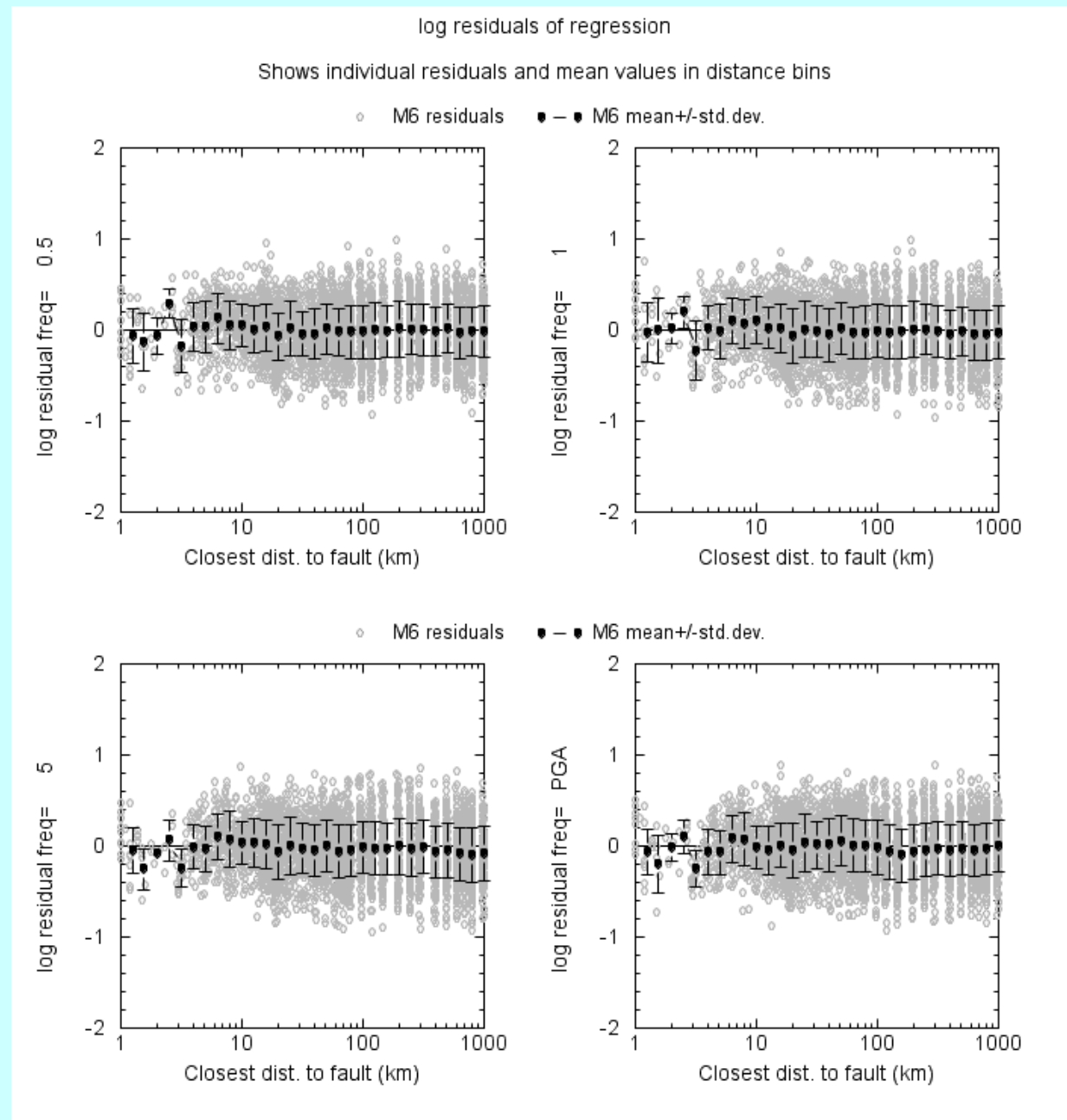
Generic ENA rock simulations for M=5, 8

AB05 simulations:
Log values of horiz,
component 5% PSA at
frequencies 0.5, 1, 5 Hz,
and PGA, for ENA rock
sites. Dots show PSA
from simulations,
including aleatory
uncertainty, for M 5
(light) and M 8 (dark).
Solid lines show
predicted amplitudes
from regression
equations developed
from simulated
database, for M5, 6, 7,
8



Example of regression residuals versus distance for M=6. Gray dots are individual residuals (where $\log \text{residual} = \log \text{simulated PSA} - \log \text{PSA}$ predicted by Equation 5). Black symbols show mean residuals and standard deviation in distance bins.

Sigma based on model is 0.3 log units for all frequencies (this is 0.69 In units --- compare to WNA 2005 empirical value of 0.60 In units)

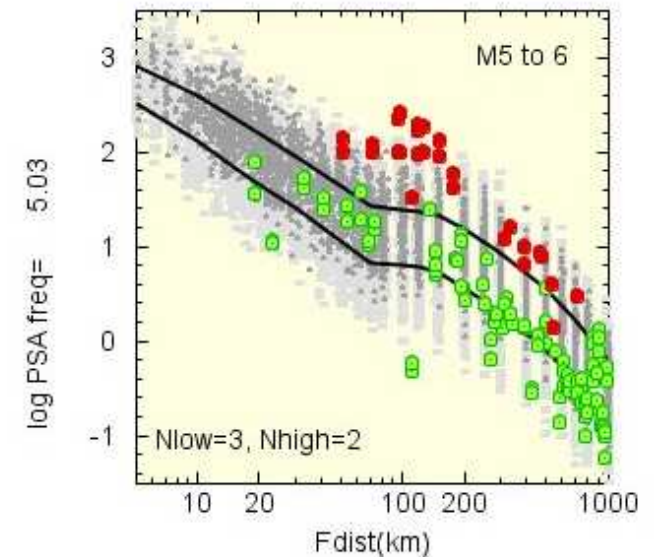
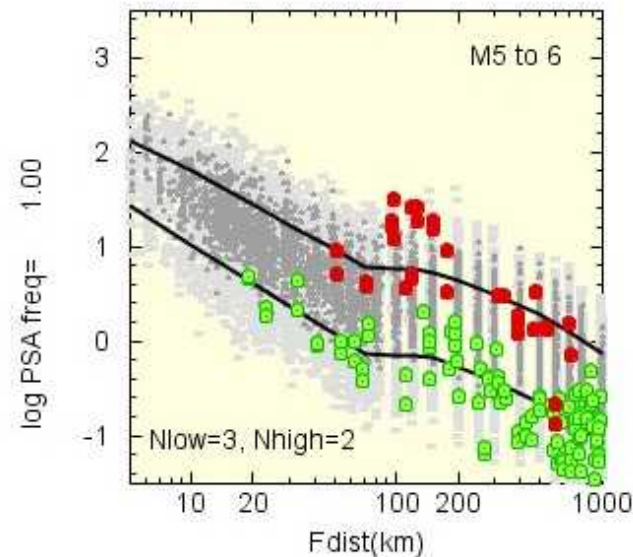
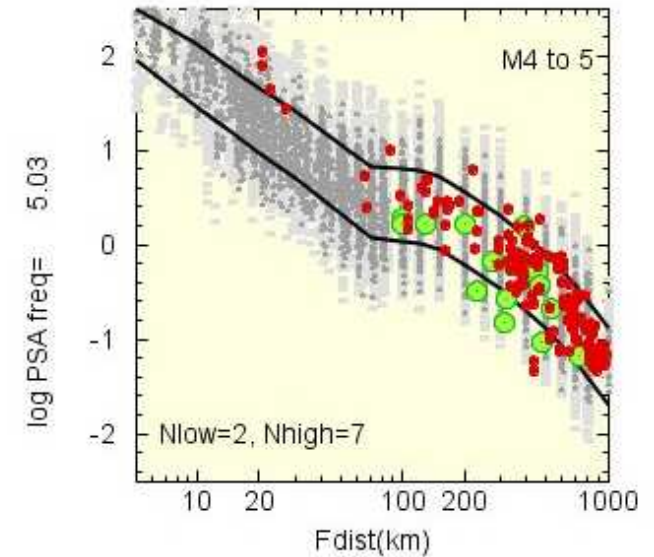
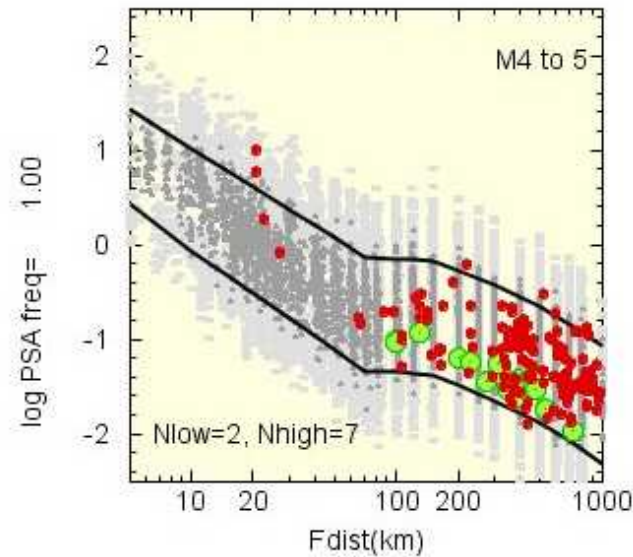


stress=140 (file ENA10). Data are rock PSA +/- 0.5 M units

**AB05 rock
simulations
(dark
grey=mid-
point M,
light
grey=+/-
0.5M);**

**equations
(black) ;**

**data (M-0.5
green,
M+0.5 red)**

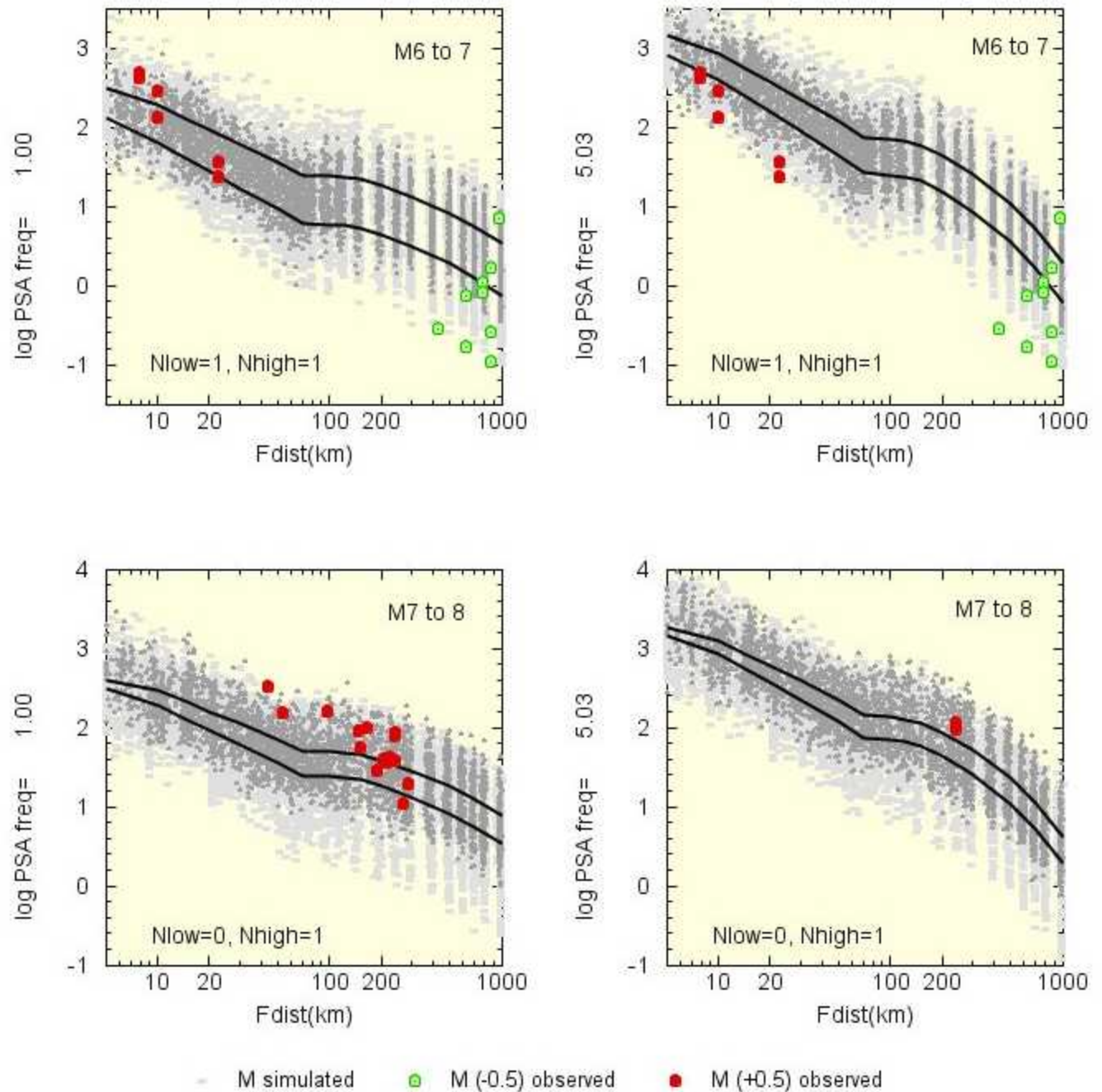


● M simulated ● M (-0.5) observed ● M (+0.5) observed

**AB05 rock
simulations
(dark
grey=mid-
point M,
light
grey=+/-
0.5M);**

**equations
(black) ;**

**data (M-0.5
green,
M+0.5 red)**

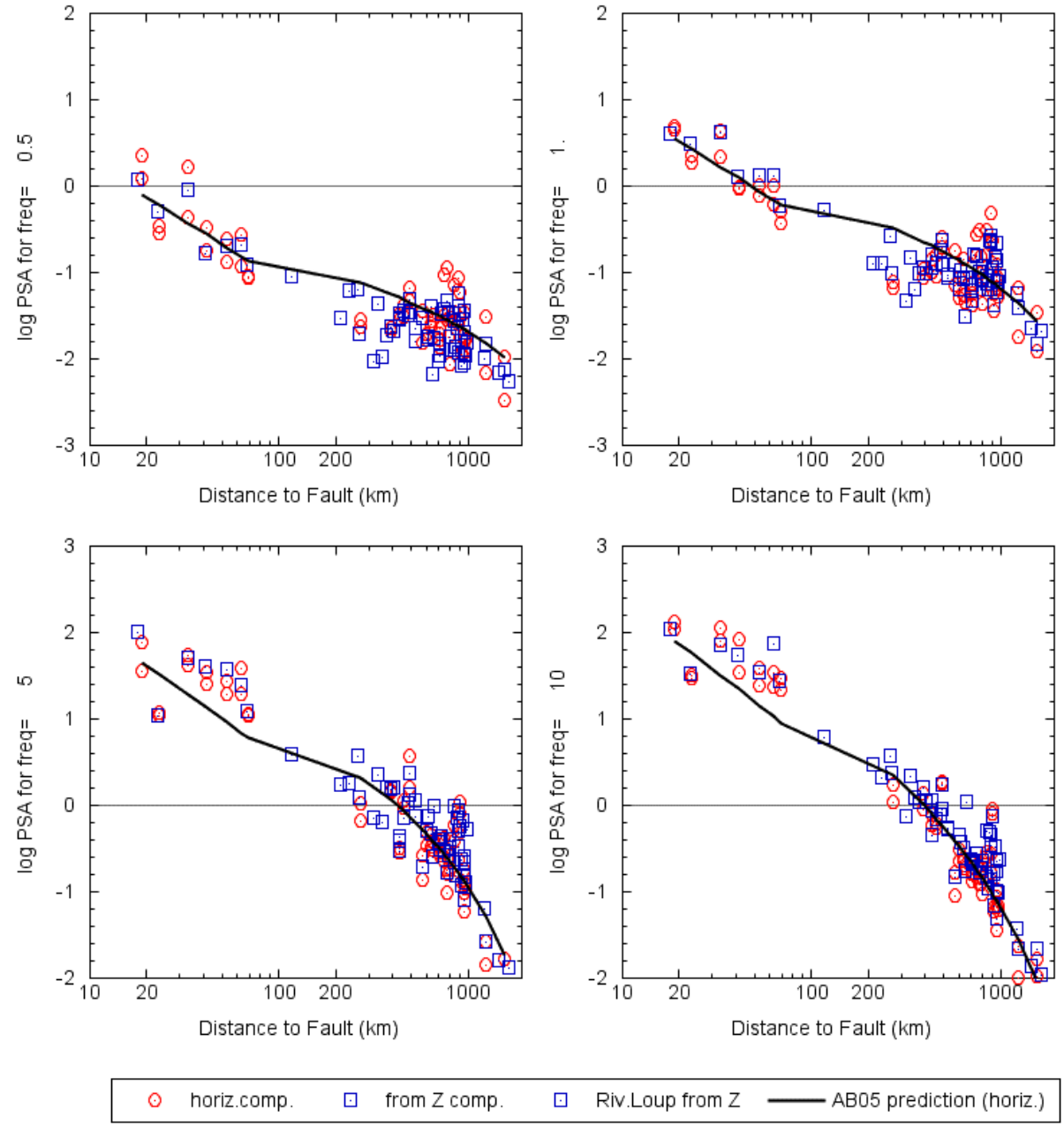


Residuals of ENA data relative to AB05

- Can compute residuals of ENA data relative to AB05 (=log obs. – log predicted)
- Keep in mind that these may not be = 0 as they represent only a subset of the information used in the model
- Overall average sigma within 0.06 log units of 0.0 over all frequencies from 0.5 to 5 Hz
- significant residuals are observed in some magnitude-distance ranges

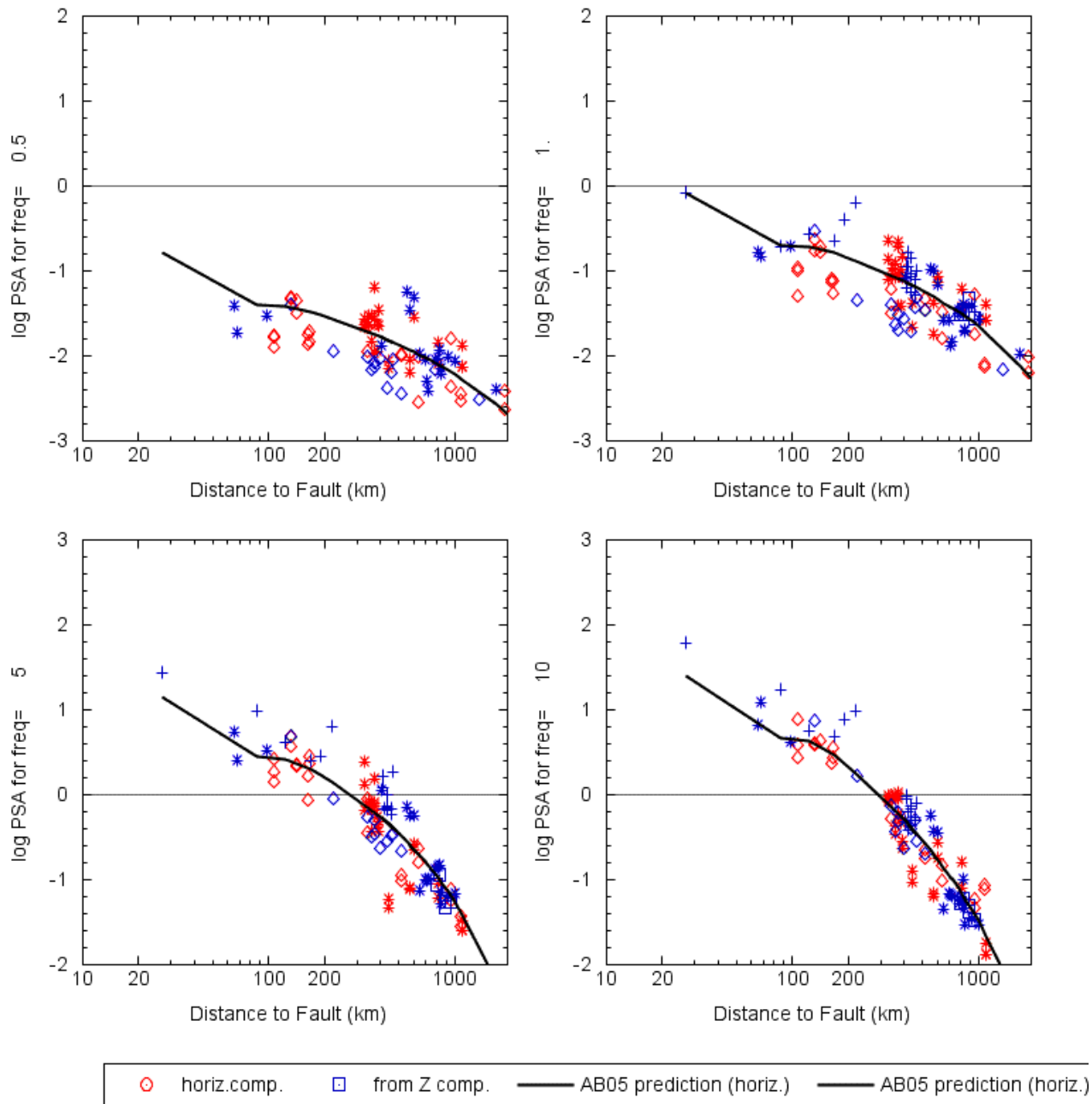
Comparison of AB05 eqns to M4.9 2005 Riviere du Loup data

PSA for rock sites compared to AB05
M4.9 (2005/03/06)



Comparison of AB05 eqns to several M4.5 events

PSA for rock sites compared to AB05
M4.5 events: (1986/12/07,+ 1990/10/19, 1997/11/06,1998/09/25)



Comparison of ground-motion equations of this study (solid red lines) for M 5.5 and 7.5, with previous predictions (Atkinson and Boore, 1995, black), and mean and standard deviation of alternative EPRI (2004) predictions (blue), all for hard-rock site conditions in ENA.

